



UNIVERSITY of
BRADFORD
Celebrating 50 years



COMPARING DIFFERENT SOLAR FLARE PREDICTION METHODS

Where are we, and how far can we go?

Manolis K. Georgoulis¹ & Rami Qahwaji²

1 RCAAM of the Academy of Athens, Greece

2 Bradford University, United Kingdom



Oostende, Belgium, Nov 14 - 18, 2016

OUTLINE

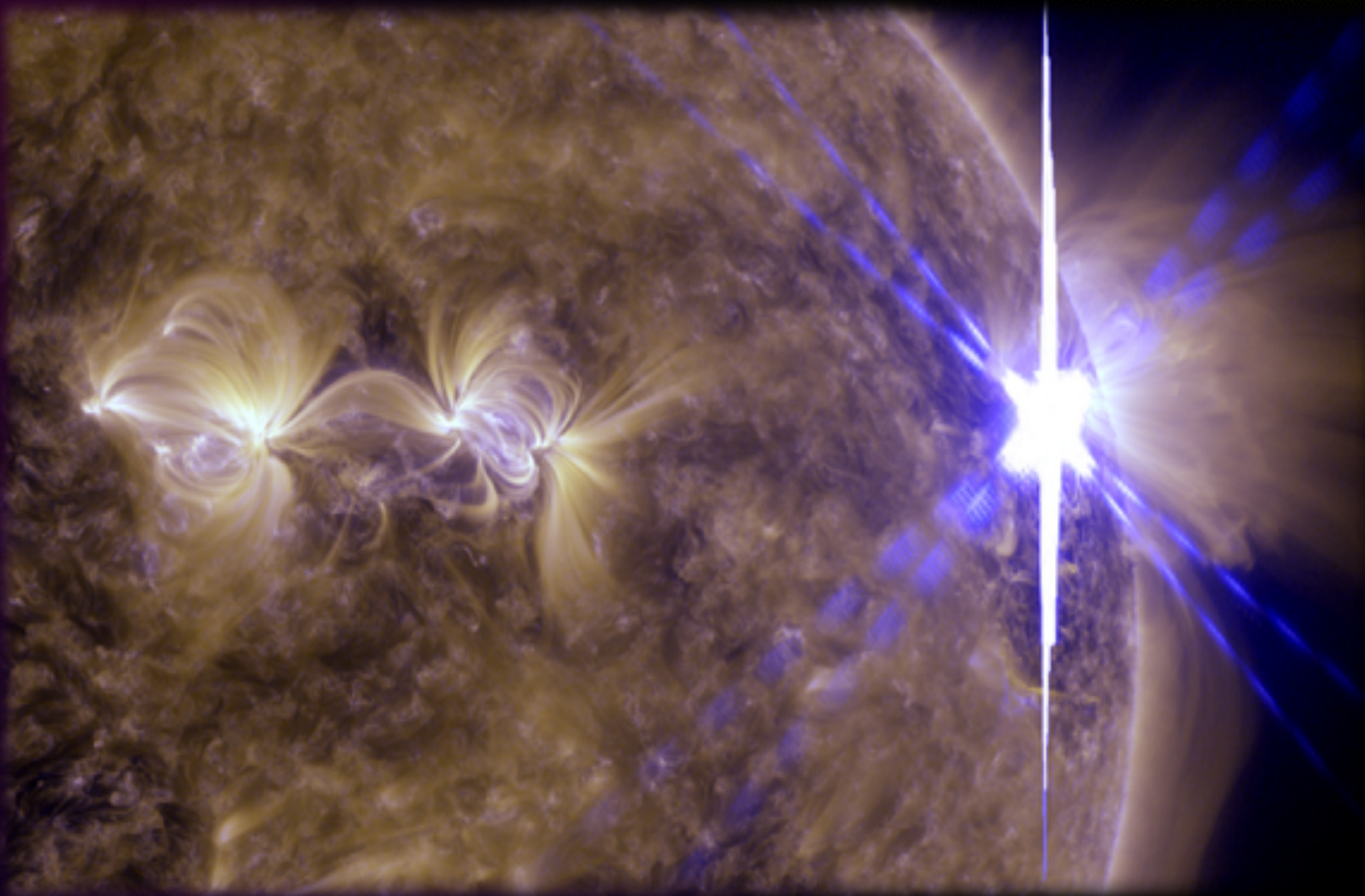
- ★ Why do we need flare prediction?
- ★ The nature of flare occurrence - are flares random?
- ★ Can flares be predicted? — different methods
- ★ Recent trends in solar flare prediction
- ★ Validation : process and intrinsic
- ★ From a method to an operational forecasting service
- ★ Conclusion



WHY PREDICT SOLAR FLARES?



WHY PREDICT SOLAR FLARES?



WHY PREDICT SOLAR FLARES?



Hard flare photons and non-thermal particulate (mostly protons $> 10 \text{ MeV}$) affect humans beyond LEO and on solar system bodies lacking an atmosphere. Damages in space-based electronics, radio blackouts, etc., can occur as a result of flares



WHY PREDICT SOLAR FLARES?

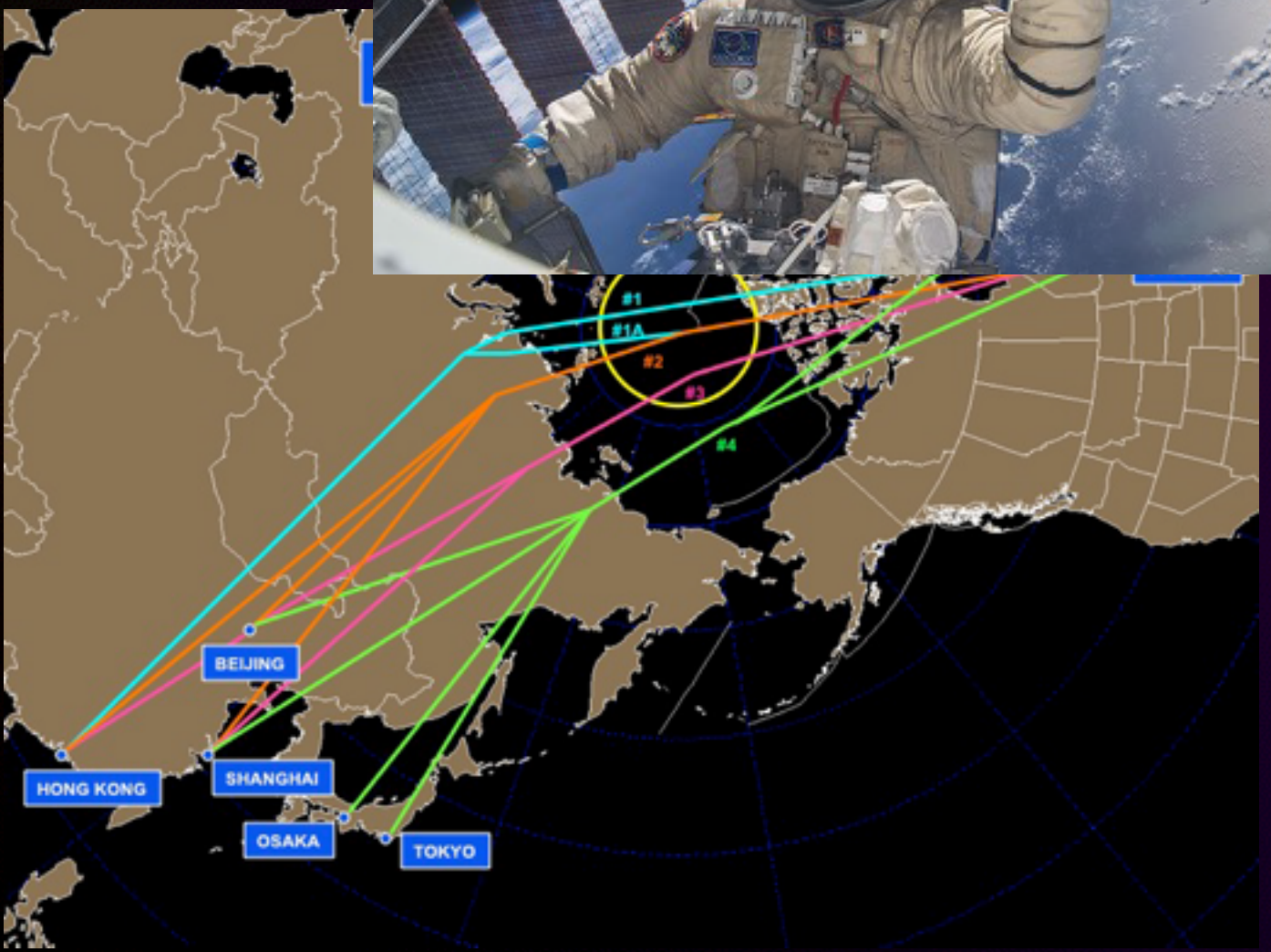
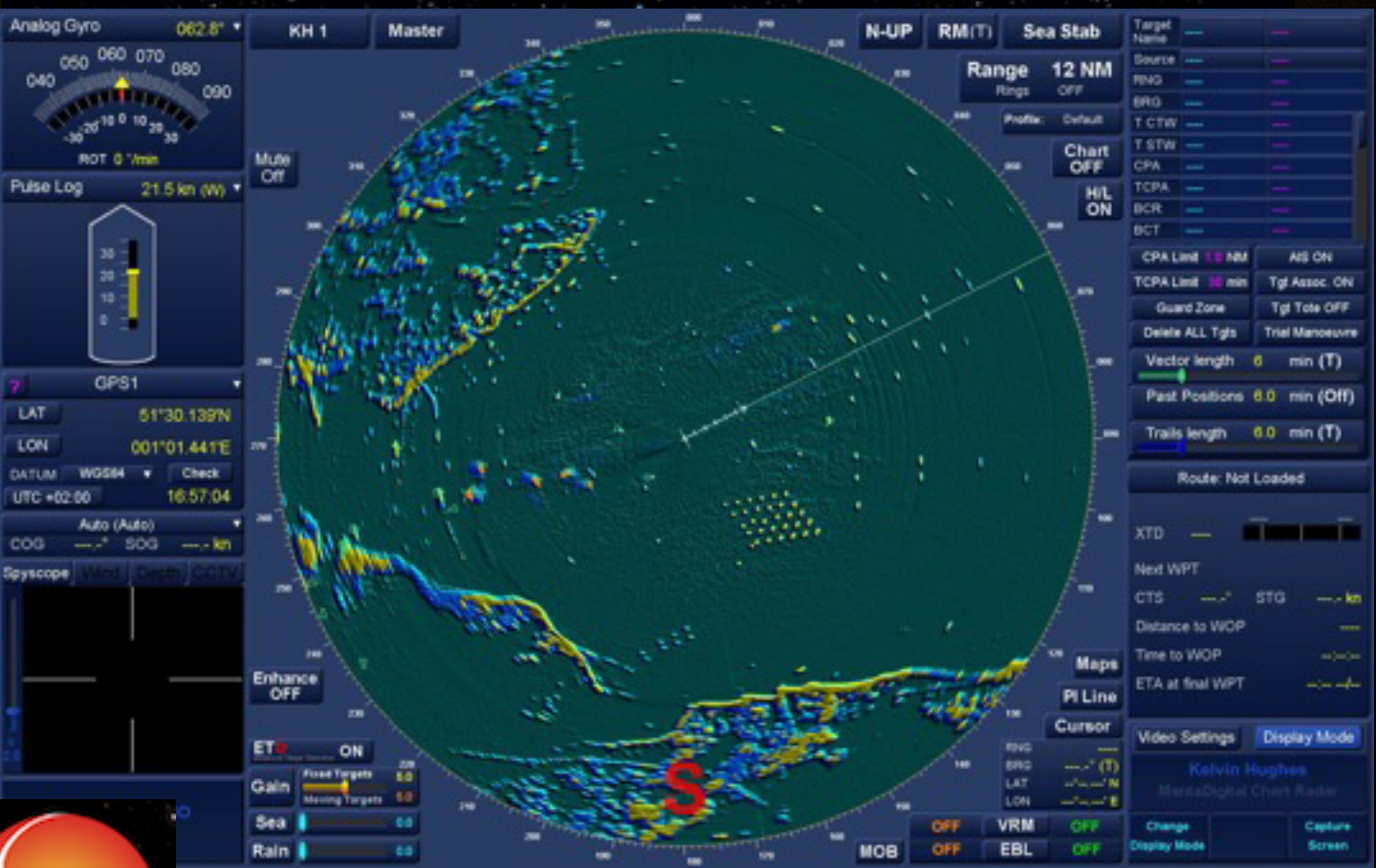
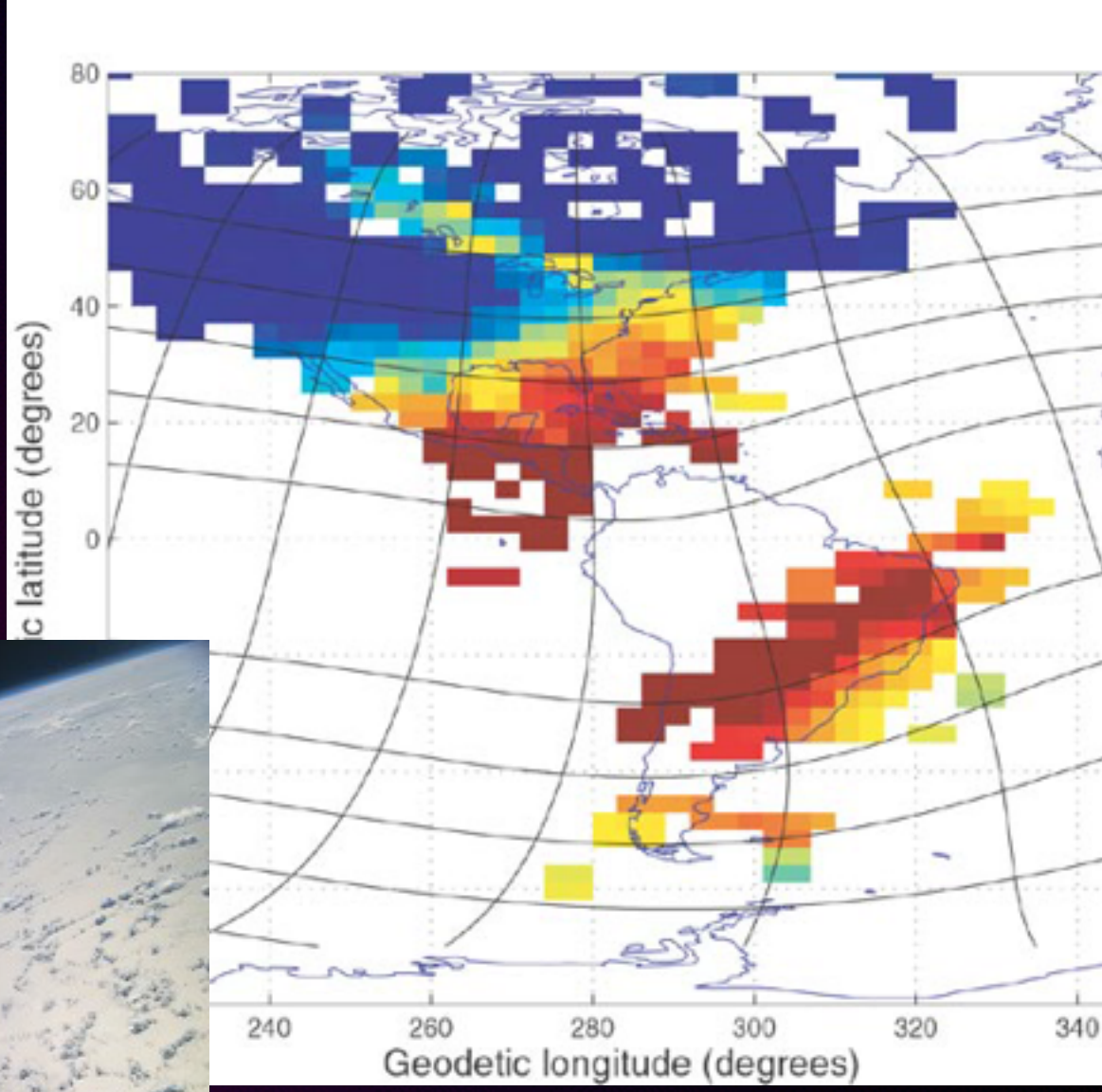
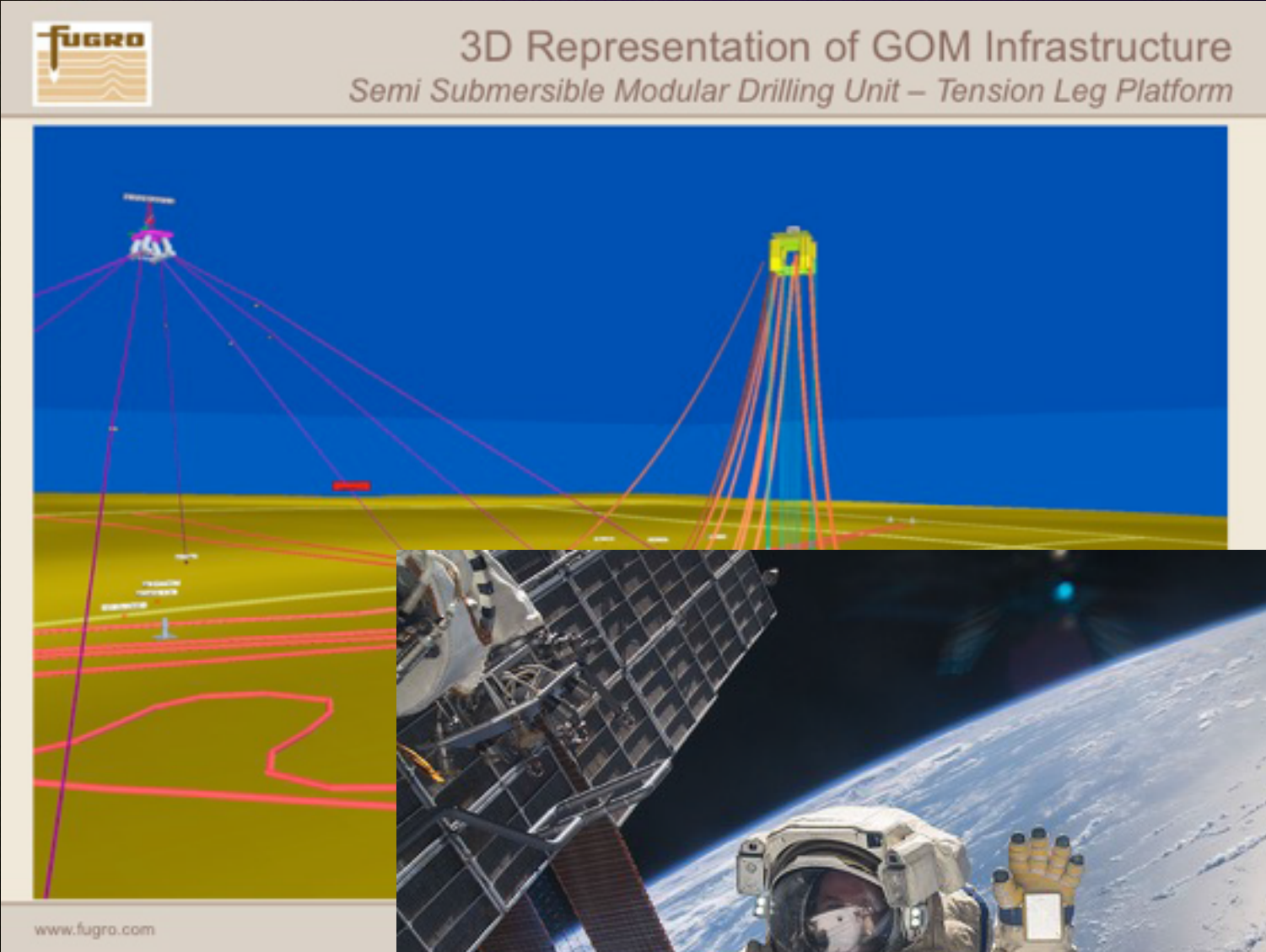
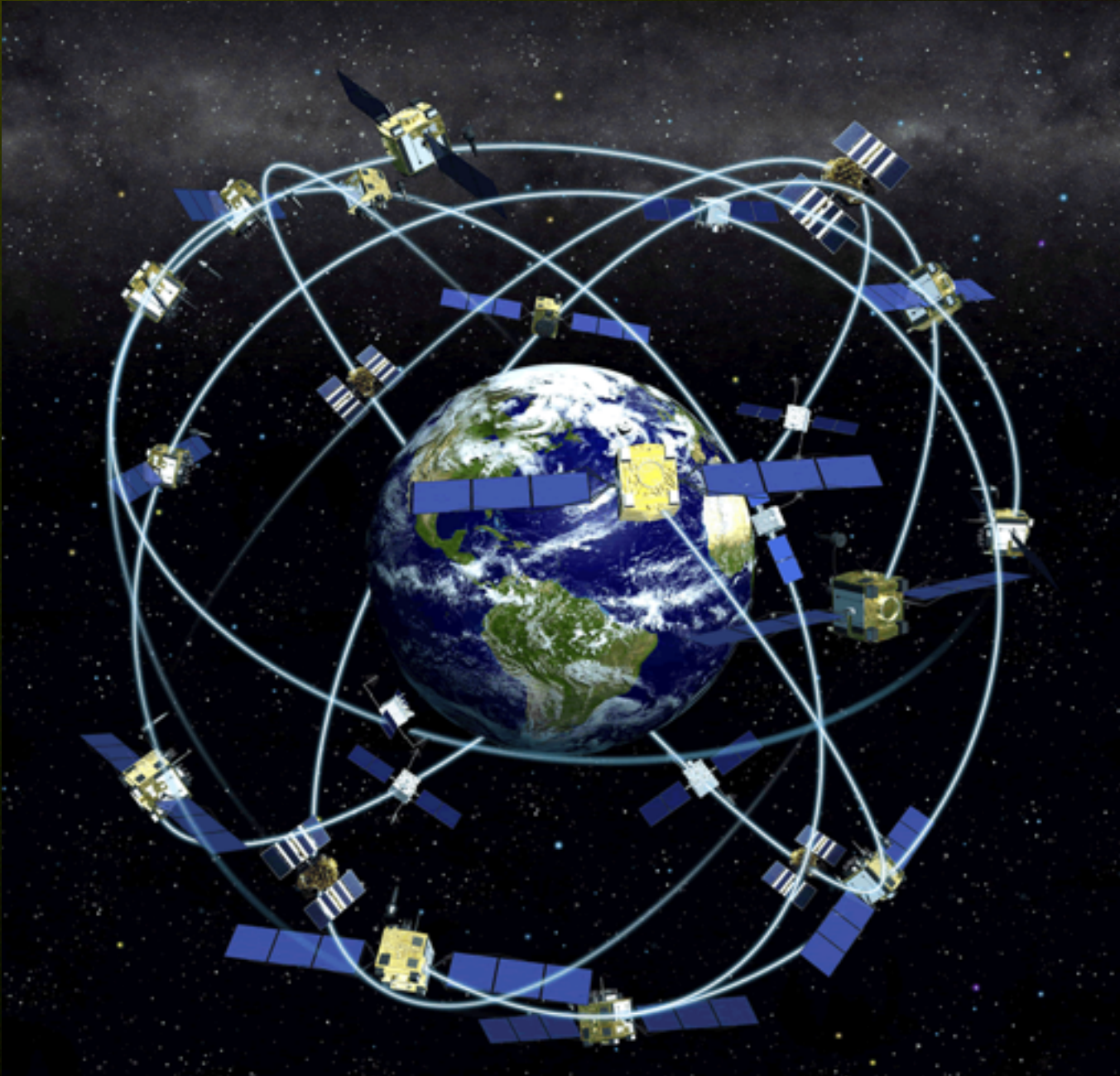


Hard flare photons and non-thermal particulate (mostly protons $> 10 \text{ MeV}$) affect humans beyond LEO and on solar system bodies lacking an atmosphere. Damages in space-based electronics, radio blackouts, etc., can occur as a result of flares

No early warning time for flare photons - slim window for particulate in worst case!



MAJOR FLARE REPERCUSSIONS: EVERYTHING UNDER THE SUN



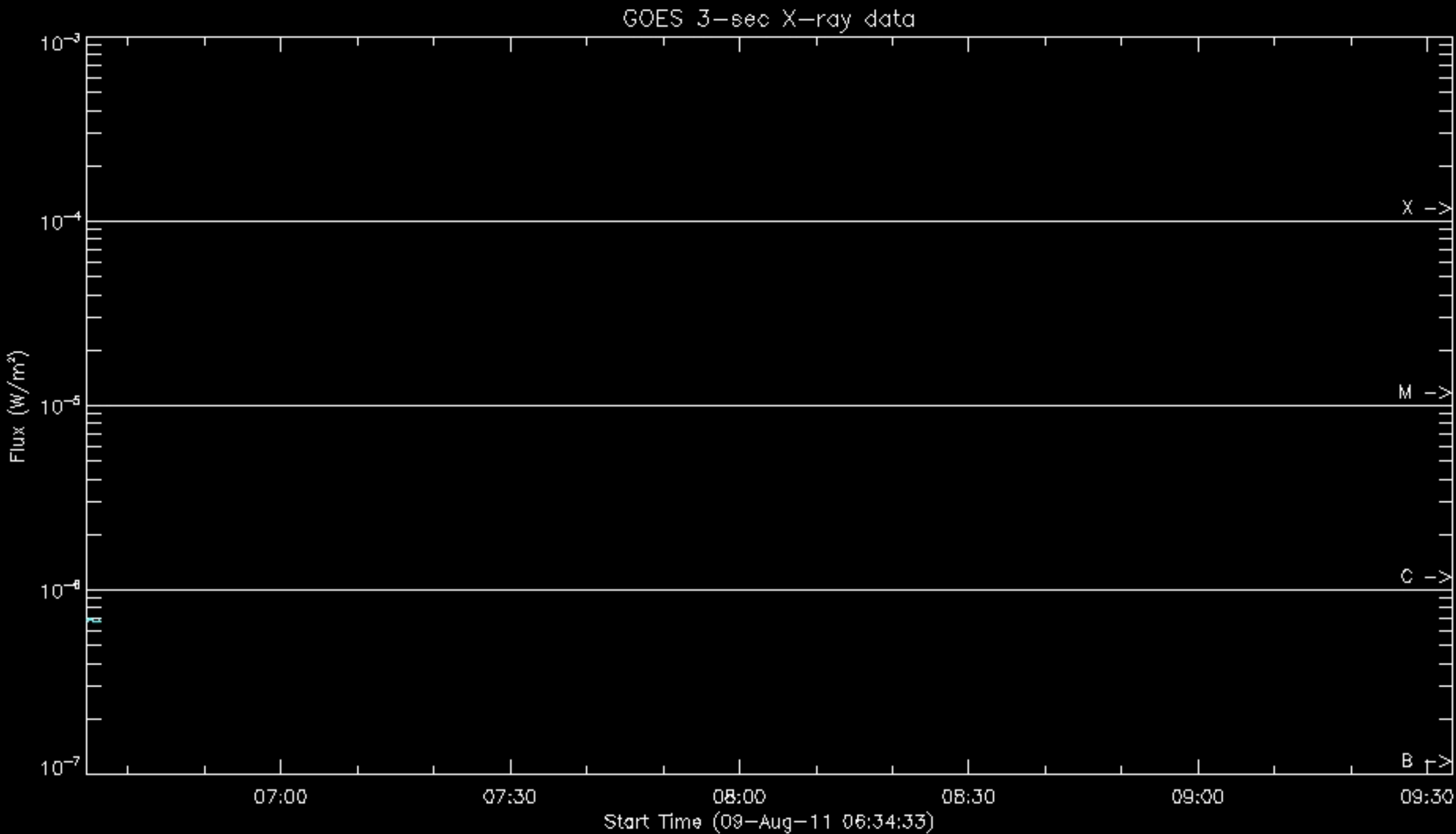
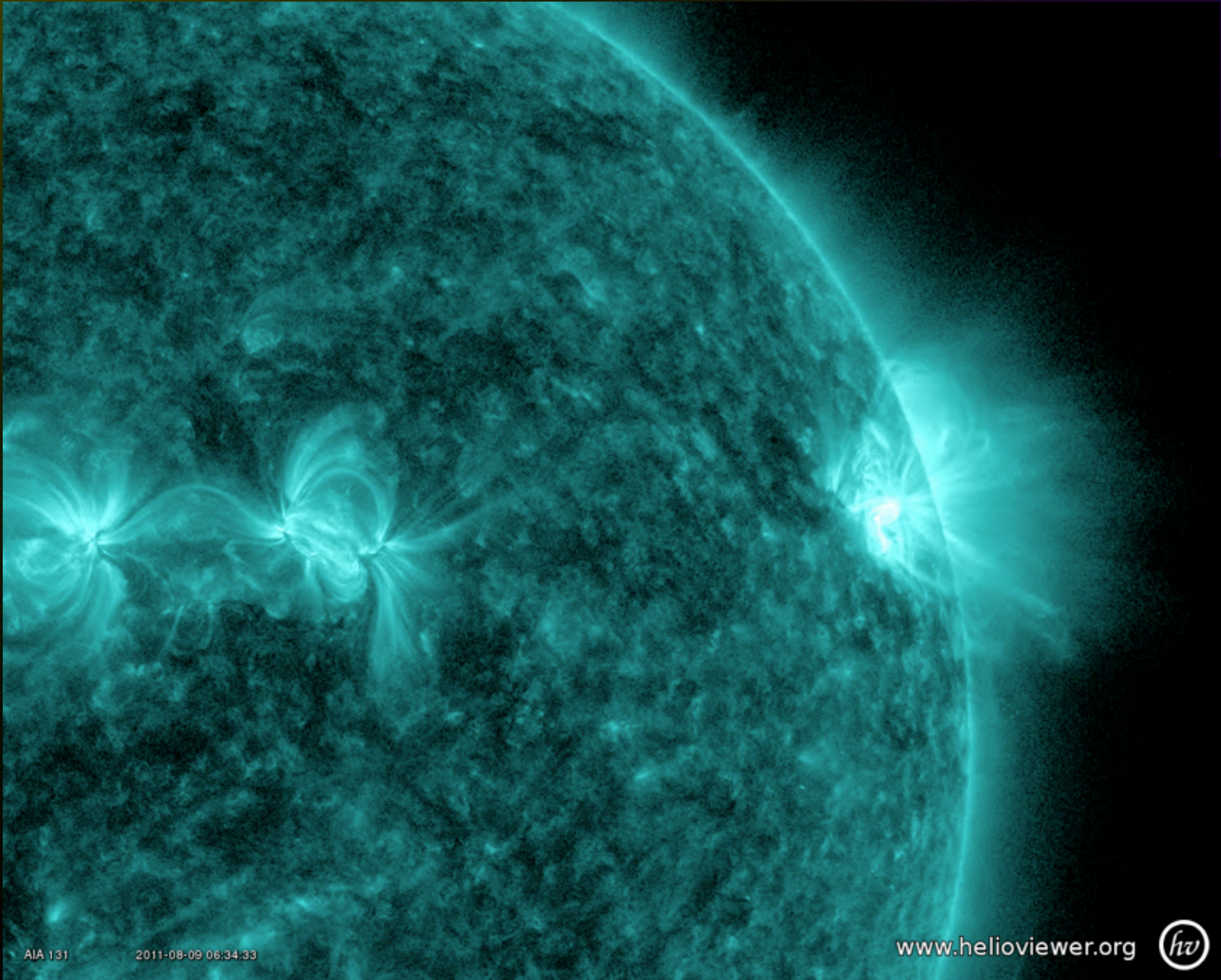
ESWW13

M. K. Georgoulis & R. Qahwaji

Oostende, November 18, 2016



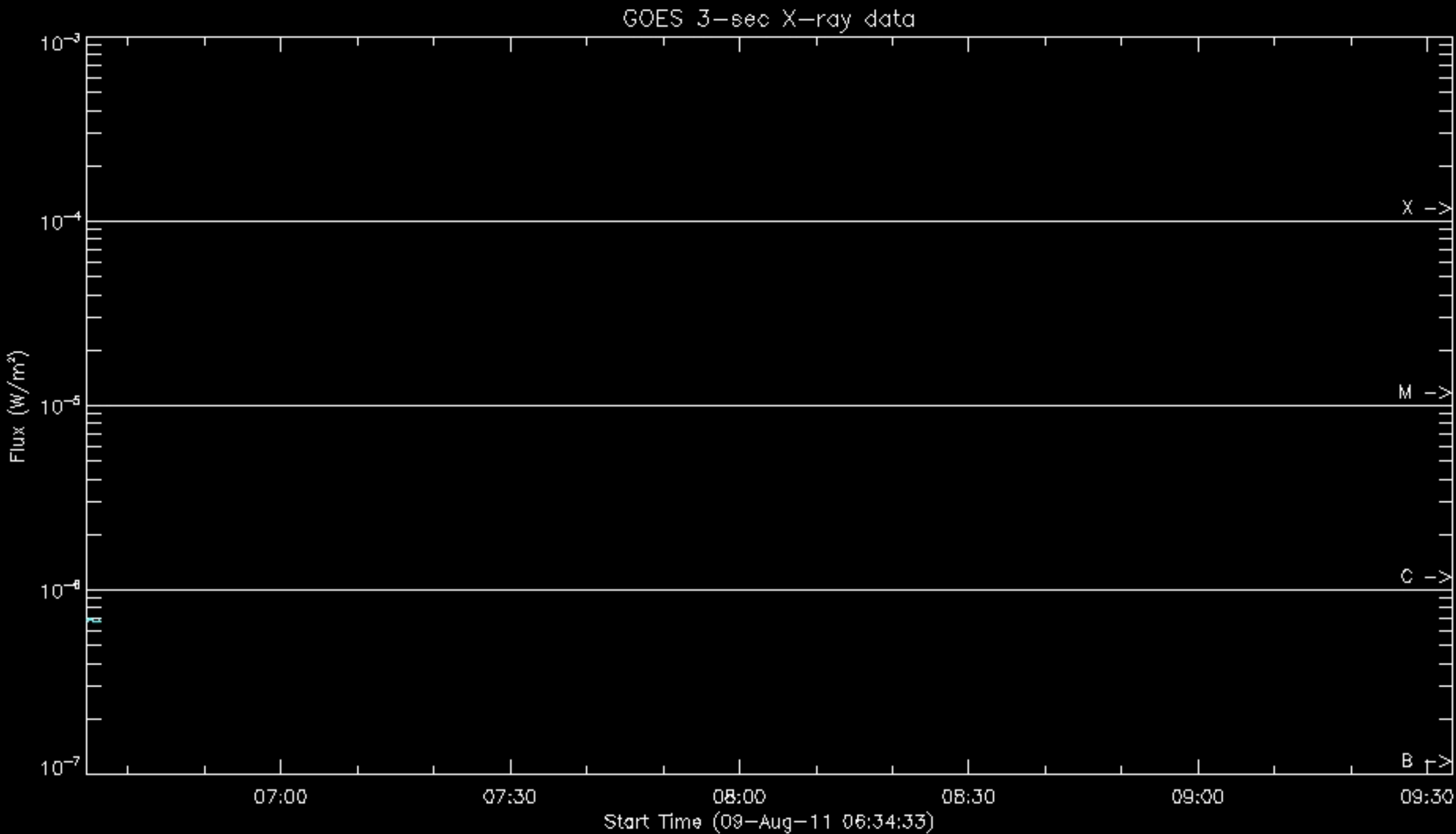
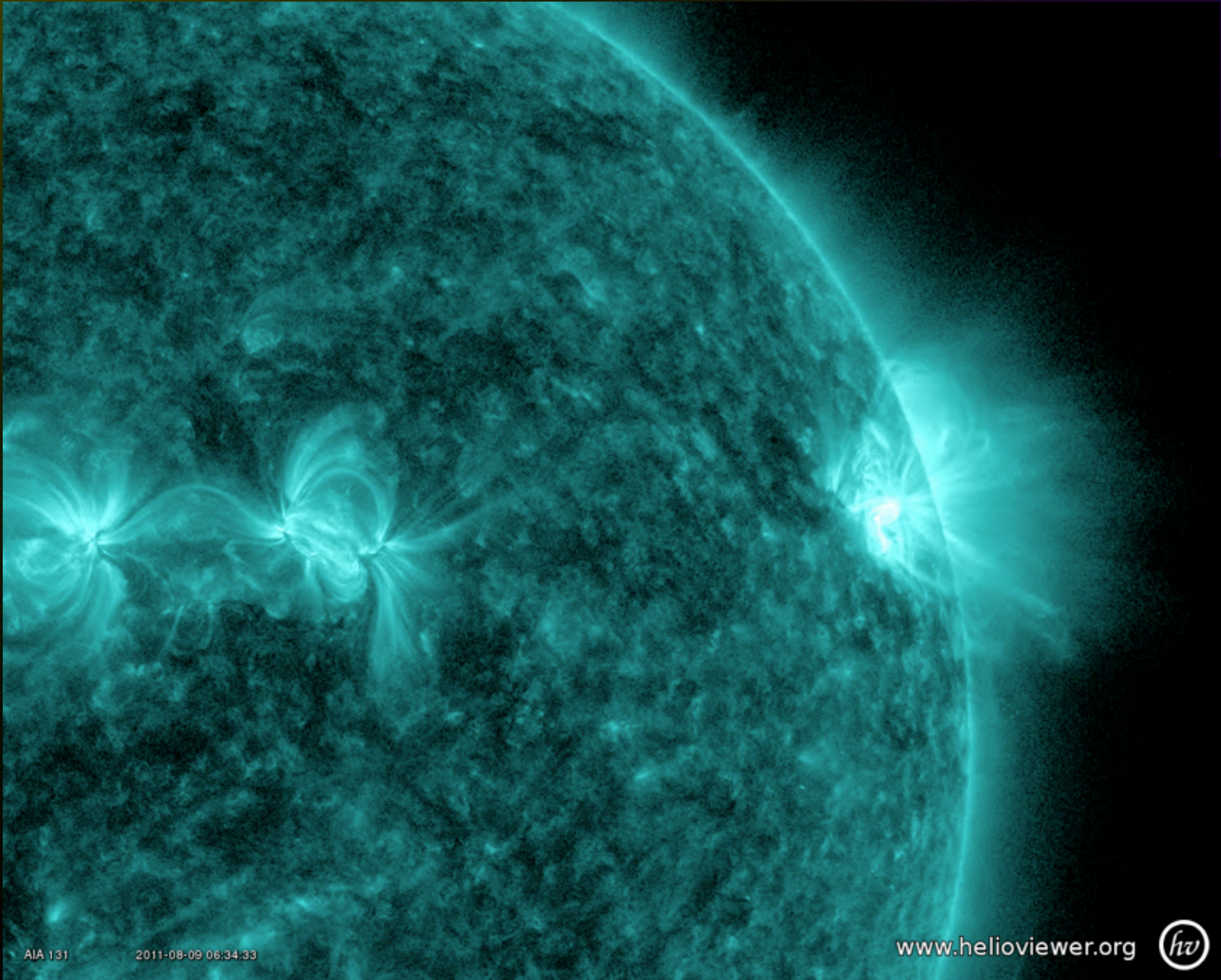
A PHENOMENOLOGY DEFINITION ...



A sudden commencement of enhanced, localized electromagnetic emission extending over practically the entire range of the electromagnetic spectrum. Typically measured in 1 - 8 Å SXR



A PHENOMENOLOGY DEFINITION ...

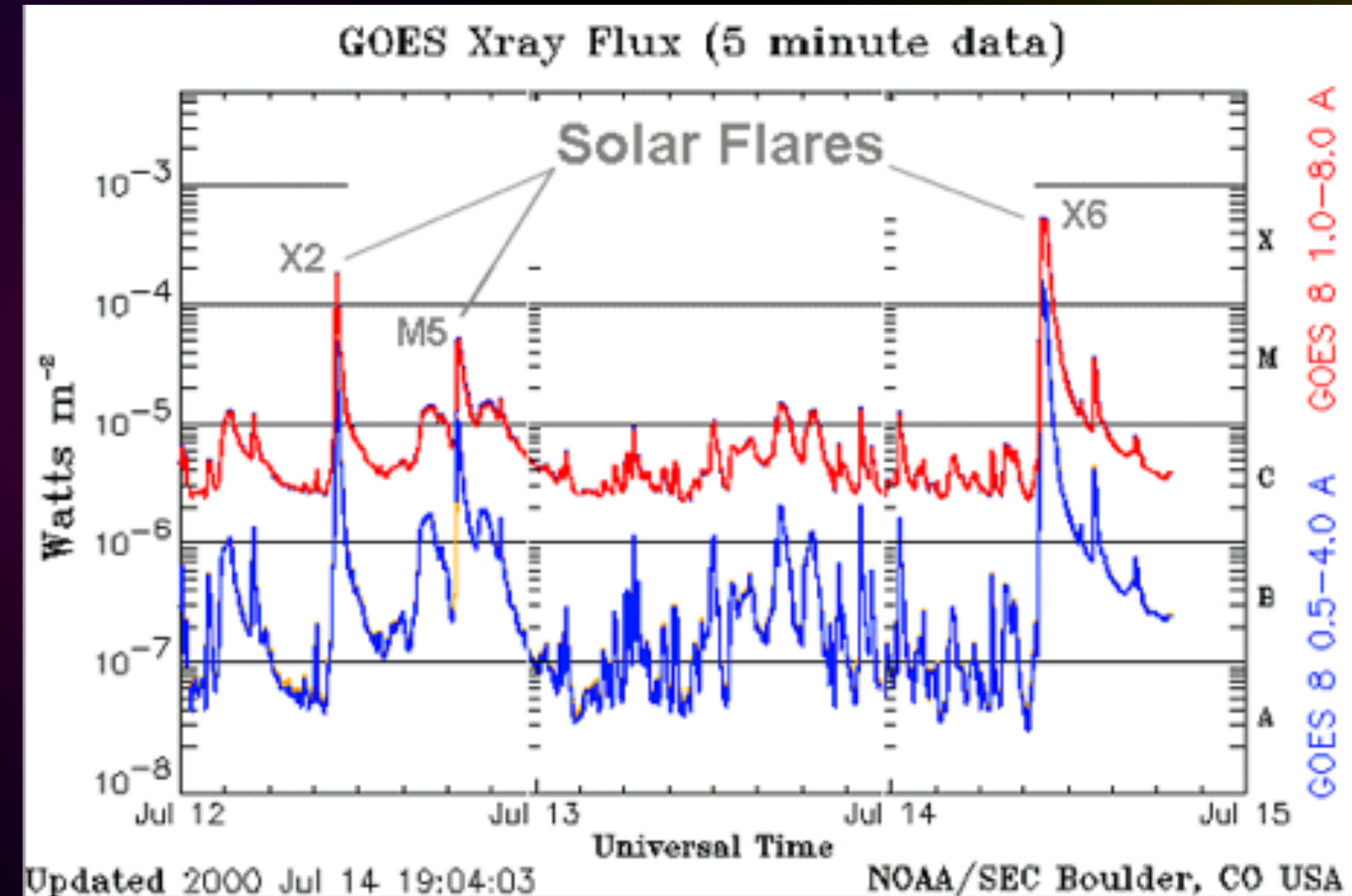
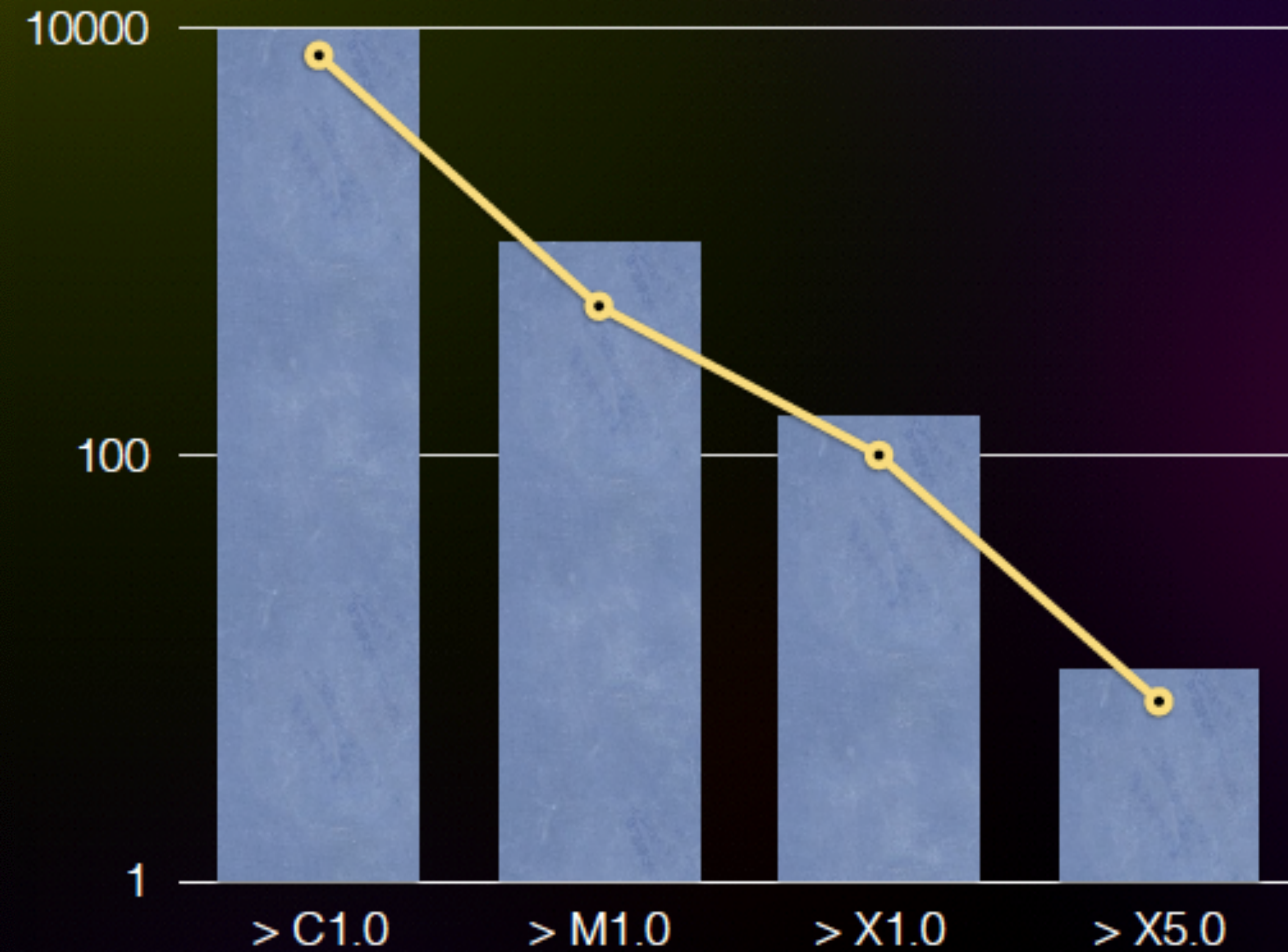


A sudden commencement of enhanced, localized electromagnetic emission extending over practically the entire range of the electromagnetic spectrum. Typically measured in 1 - 8 Å SXR



...AND STATISTICAL BEHAVIOR

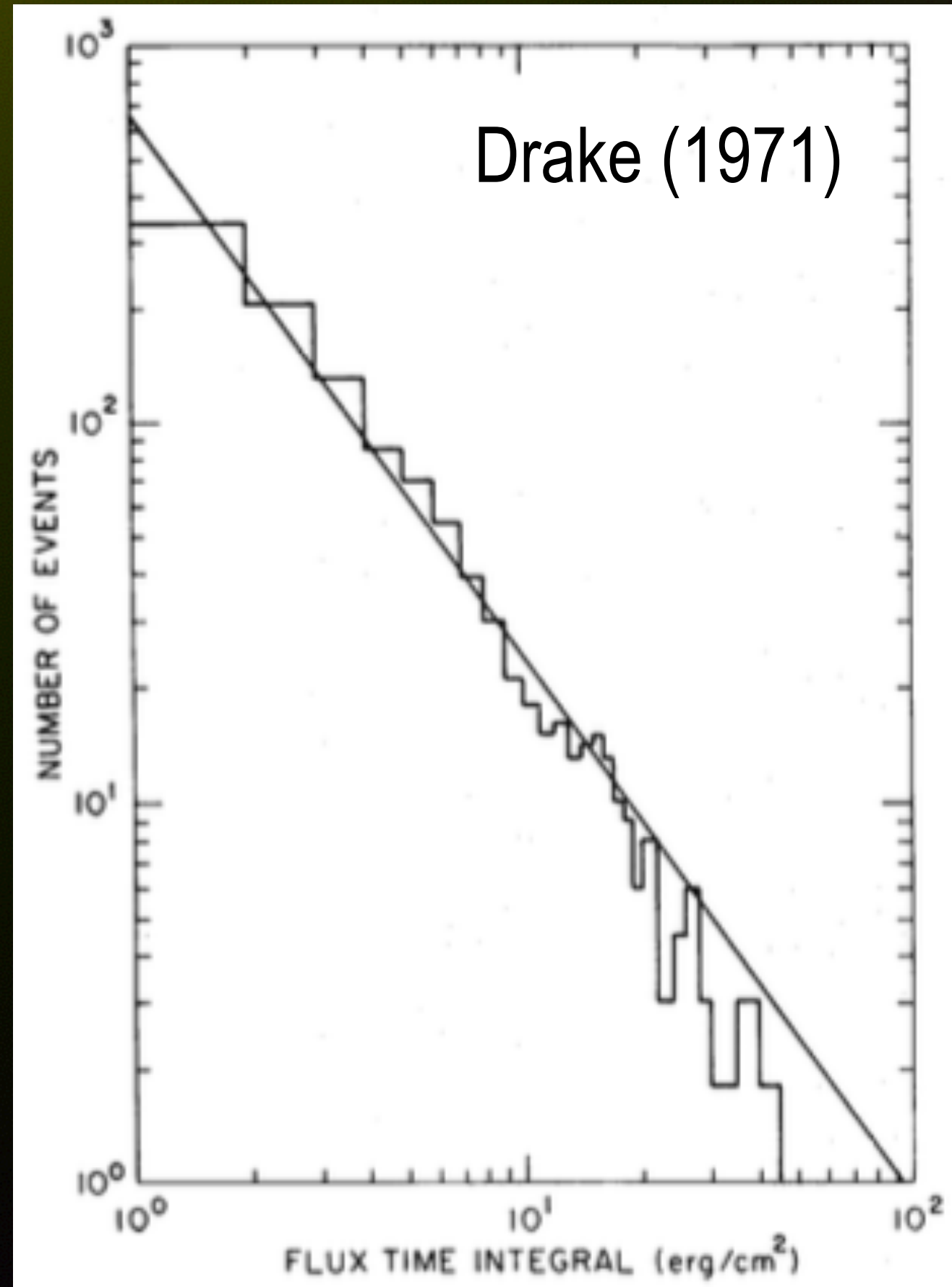
No. of flares per class over typical solar cycle



“Active” solar conditions over a 3-day period in July 2000



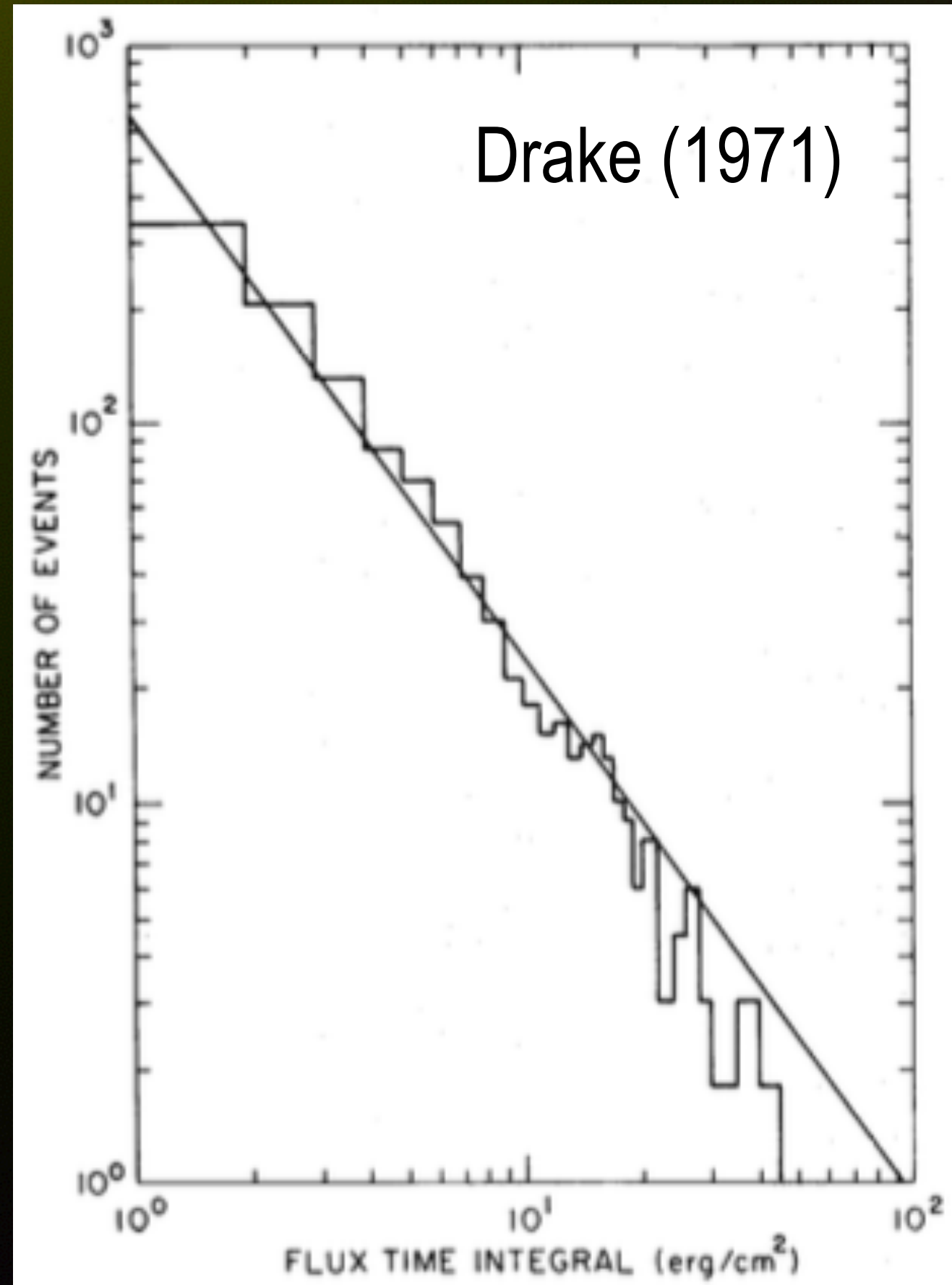
NATURE OF FLARE OCCURRENCE



Flare occurrence number vs.
integrated photon flux



NATURE OF FLARE OCCURRENCE



Flare occurrence number vs.
integrated photon flux

Flares are (Rosner & Vaiana 1978):

- Stochastic relaxation (storage and release) processes
- Physically uncoupled / independent
- Brief, comparing to intermediate times between flares

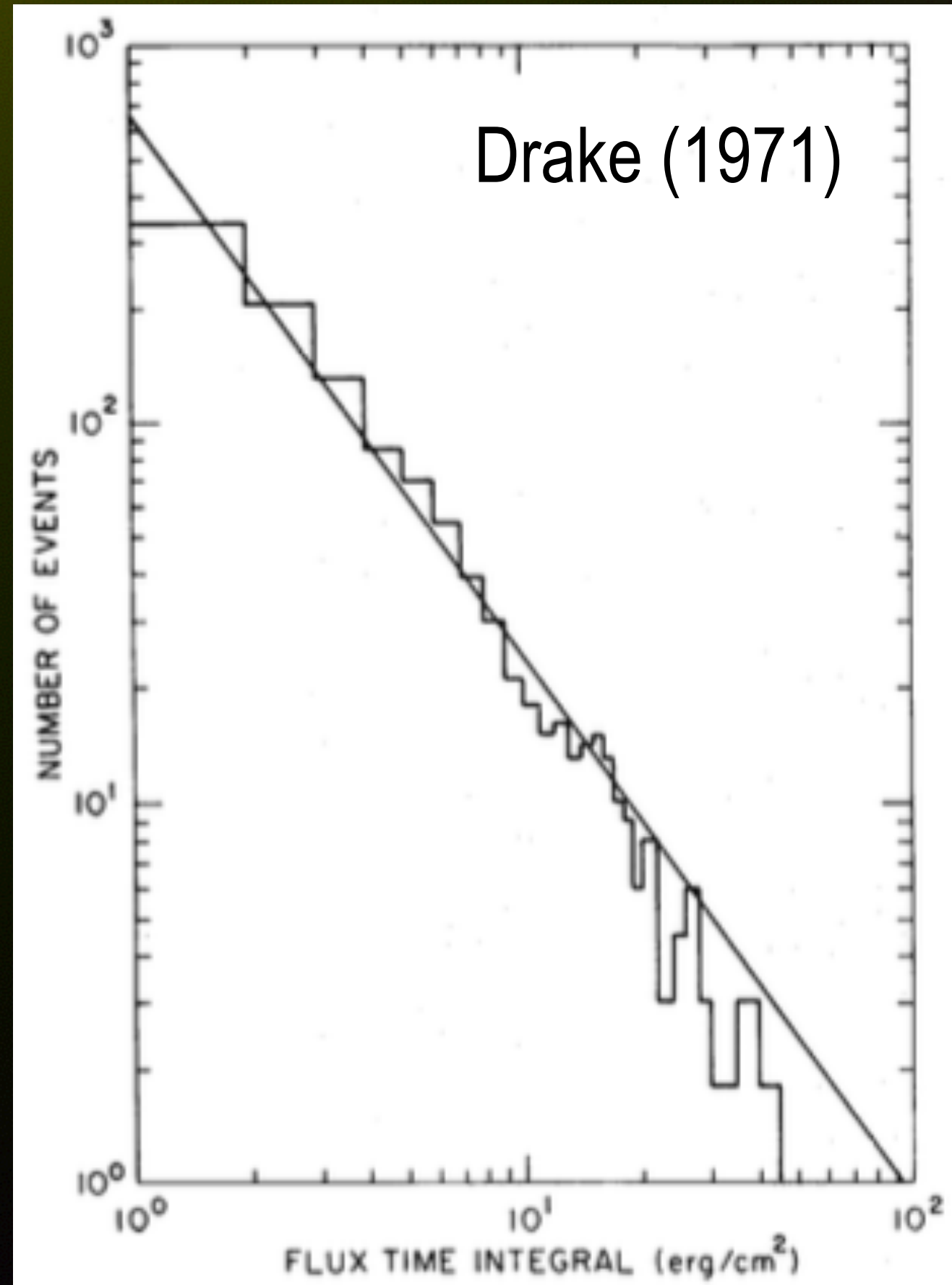
$$P(t) = \bar{\nu} e^{-\bar{\nu}t}$$

- Leading to a power-law occurrence frequency for flare energies

$$P(E) \sim \left(1 + \frac{E}{E_0}\right)^{-\gamma}$$



NATURE OF FLARE OCCURRENCE



Flare occurrence number vs. integrated photon flux

Flares are (Rosner & Vaiana 1978):

- Stochastic relaxation (storage and release) processes
- Physically uncoupled / independent
- Brief, comparing to intermediate times between flares

$$P(t) = \bar{\nu} e^{-\bar{\nu}t}$$

- Leading to a power-law occurrence frequency for flare energies

$$P(E) \sim \left(1 + \frac{E}{E_0}\right)^{-\gamma}$$

Power-law distribution of flare size later attributed to the concept of self-organized criticality (1990s)



A RATHER GRAPHIC EXAMPLE OF MARGINAL STABILITY

Credit: Aaron Mak - YouTube



A RATHER GRAPHIC EXAMPLE OF MARGINAL STABILITY

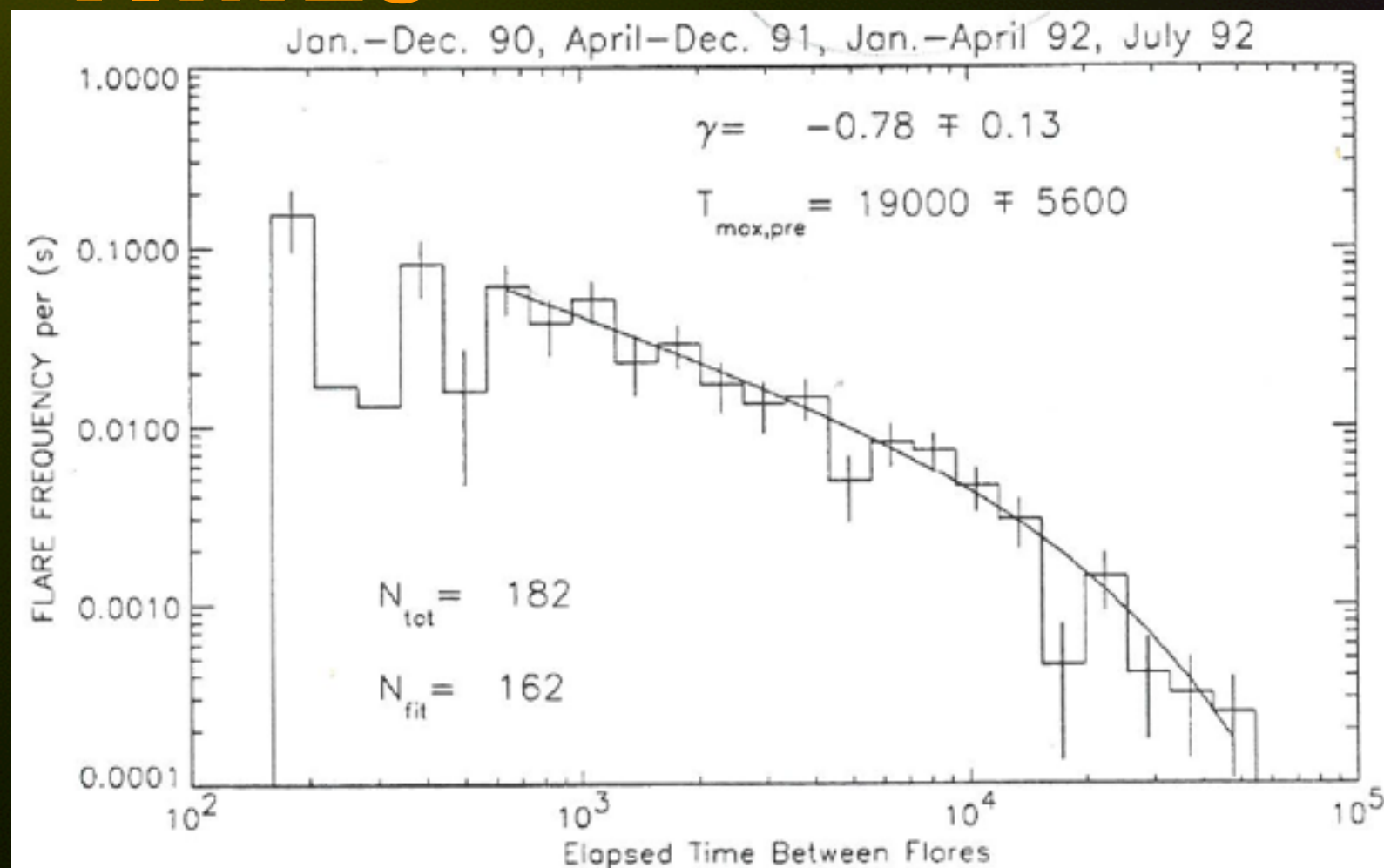
Credit: Aaron Mak - YouTube



HOWEVER, ARE FLARES RANDOM? - DISTRIBUTION OF WAITING TIMES



HOWEVER, ARE FLARES RANDOM? - DISTRIBUTION OF WAITING TIMES



Crosby, PhD Thesis (1996)

Exponential law of waiting times: a totally random, memoryless flare occurrence along the classical self-organized criticality concept



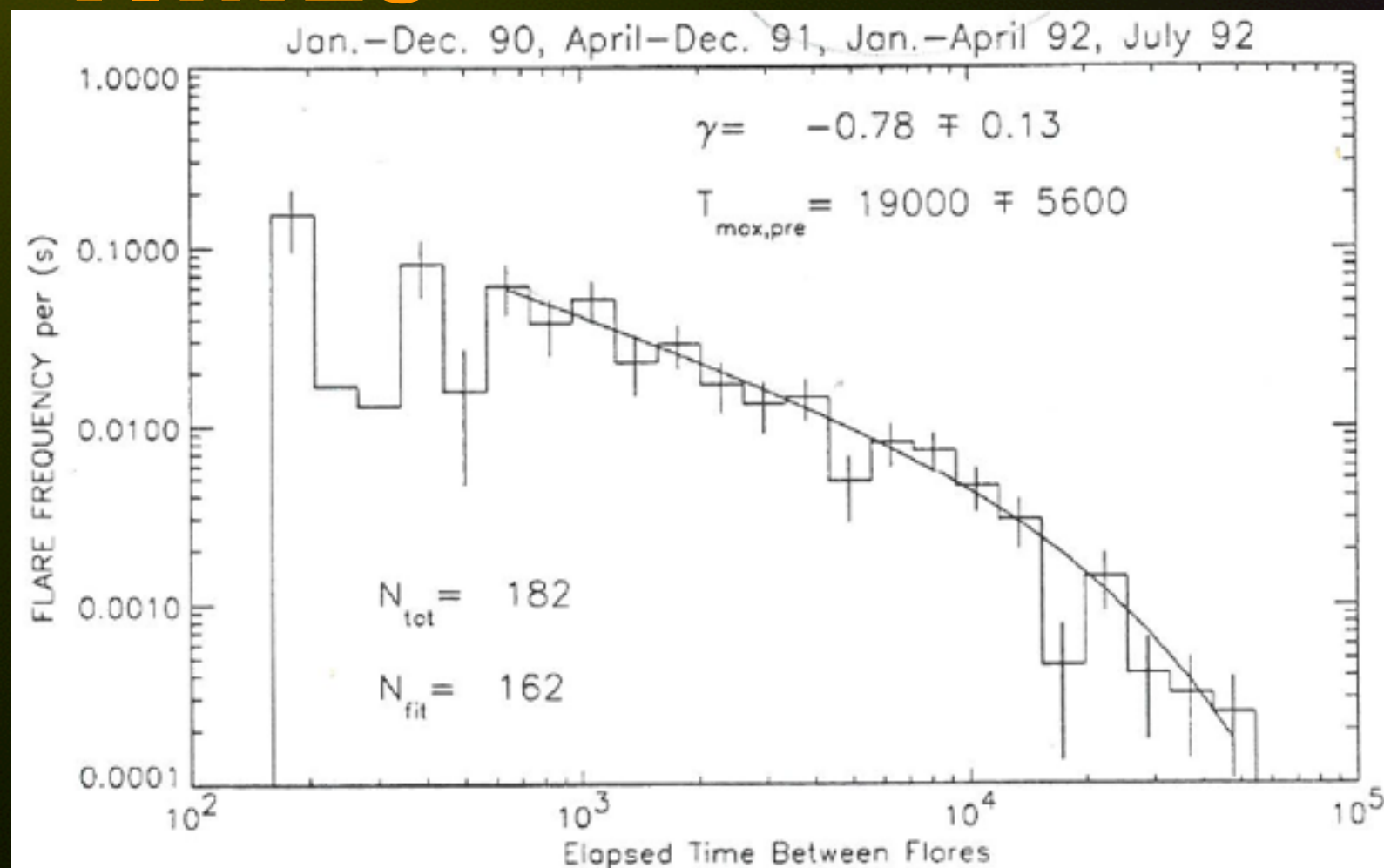
ESWW13

M. K. Georgoulis & R. Qahwaji

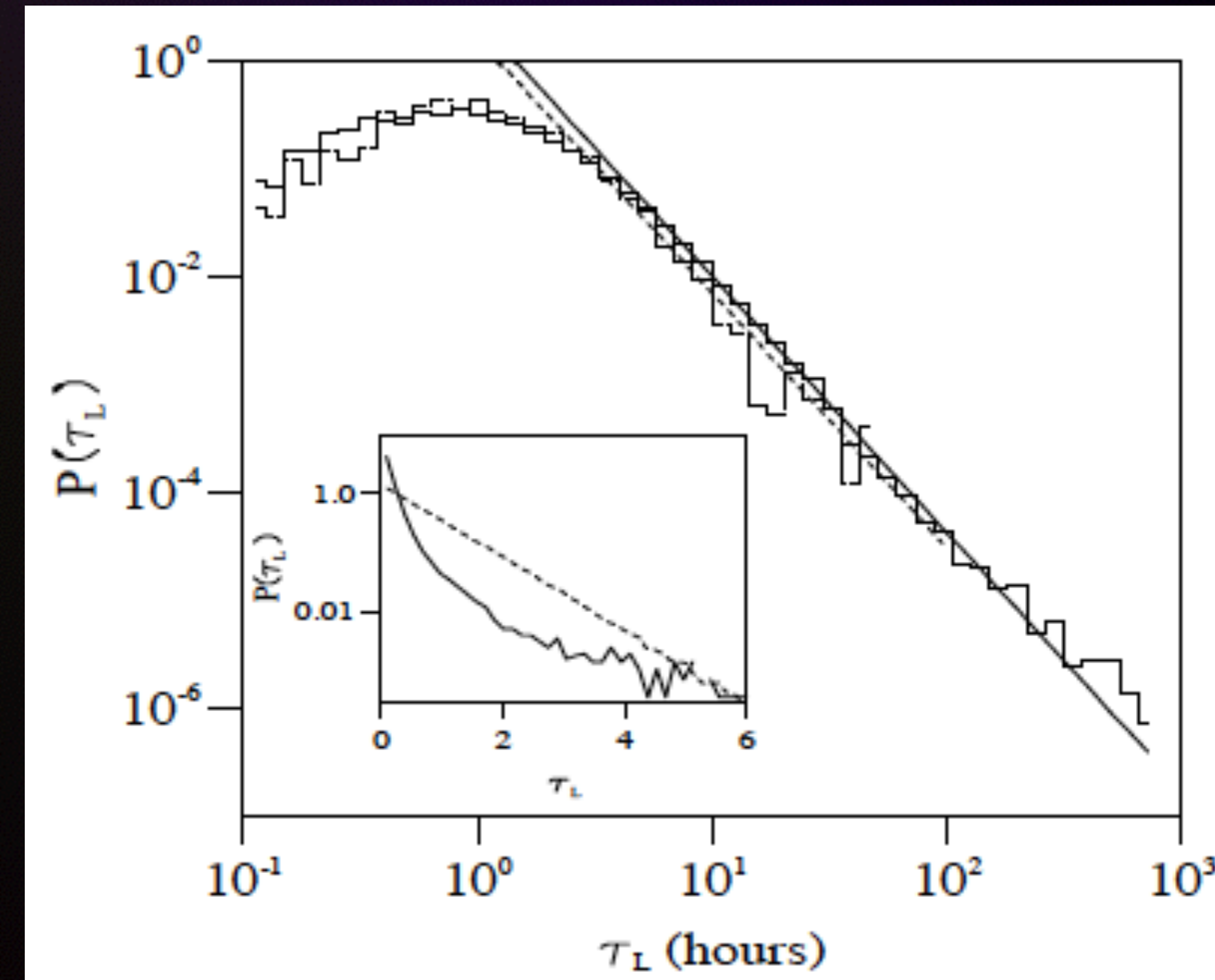
Oostende, November 18, 2016



HOWEVER, ARE FLARES RANDOM? - DISTRIBUTION OF WAITING TIMES



Crosby, PhD Thesis (1996)



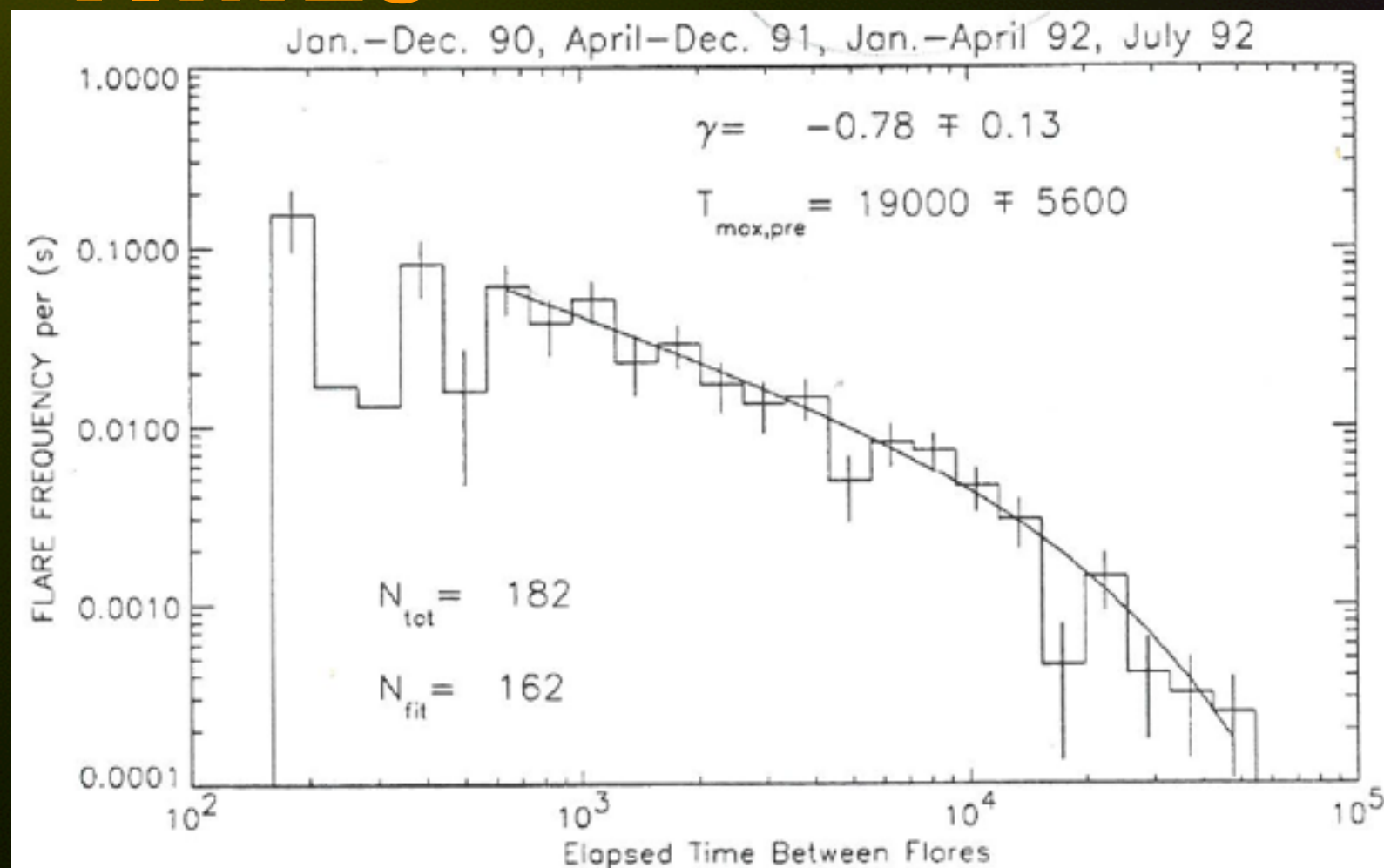
Bofetta et al., (1999)

Exponential law of waiting times: a totally random, memoryless flare occurrence along the classical self-organized criticality concept

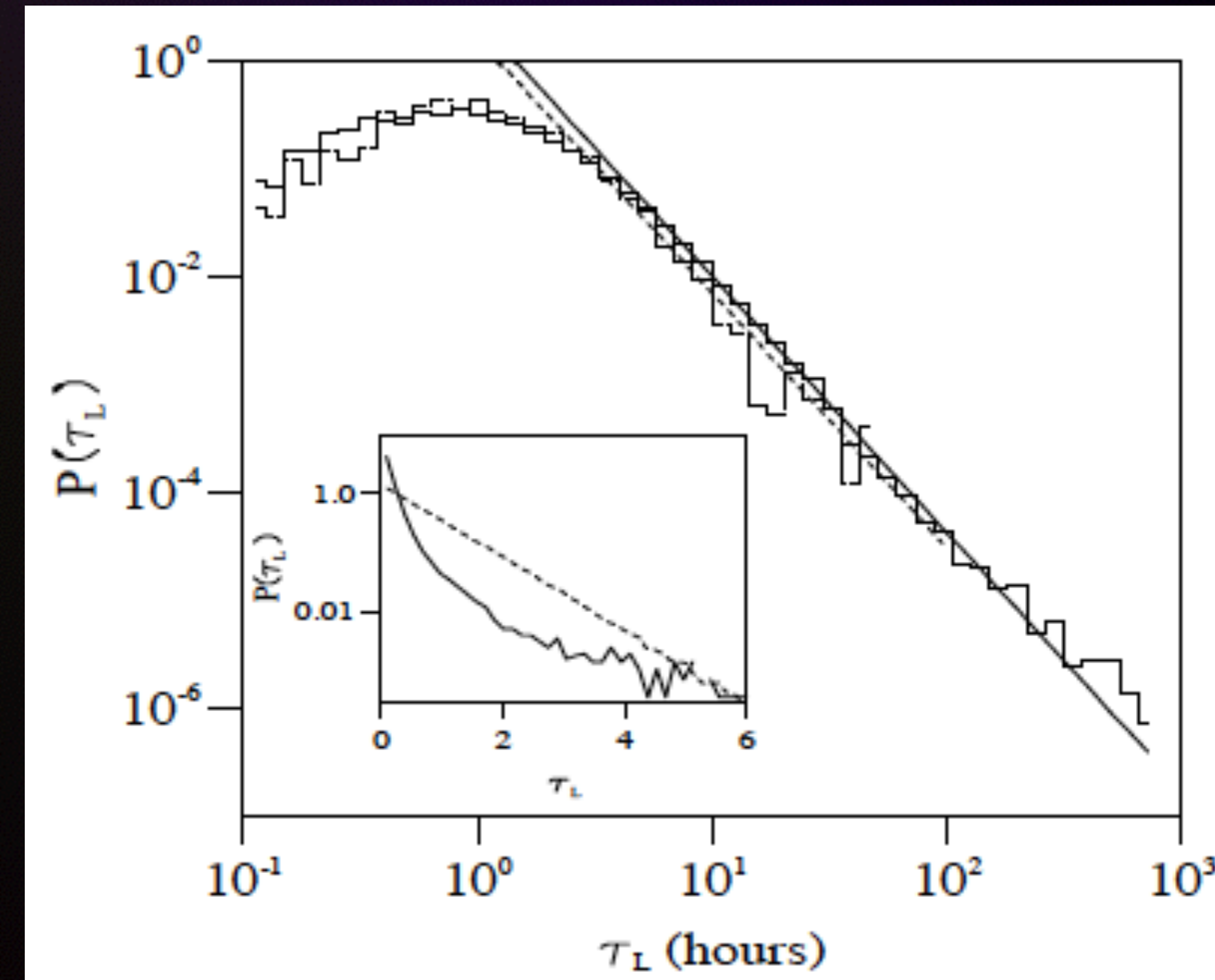
Robust power-law of waiting times: a system perfectly keeping a memory in giving flares



HOWEVER, ARE FLARES RANDOM? - DISTRIBUTION OF WAITING TIMES

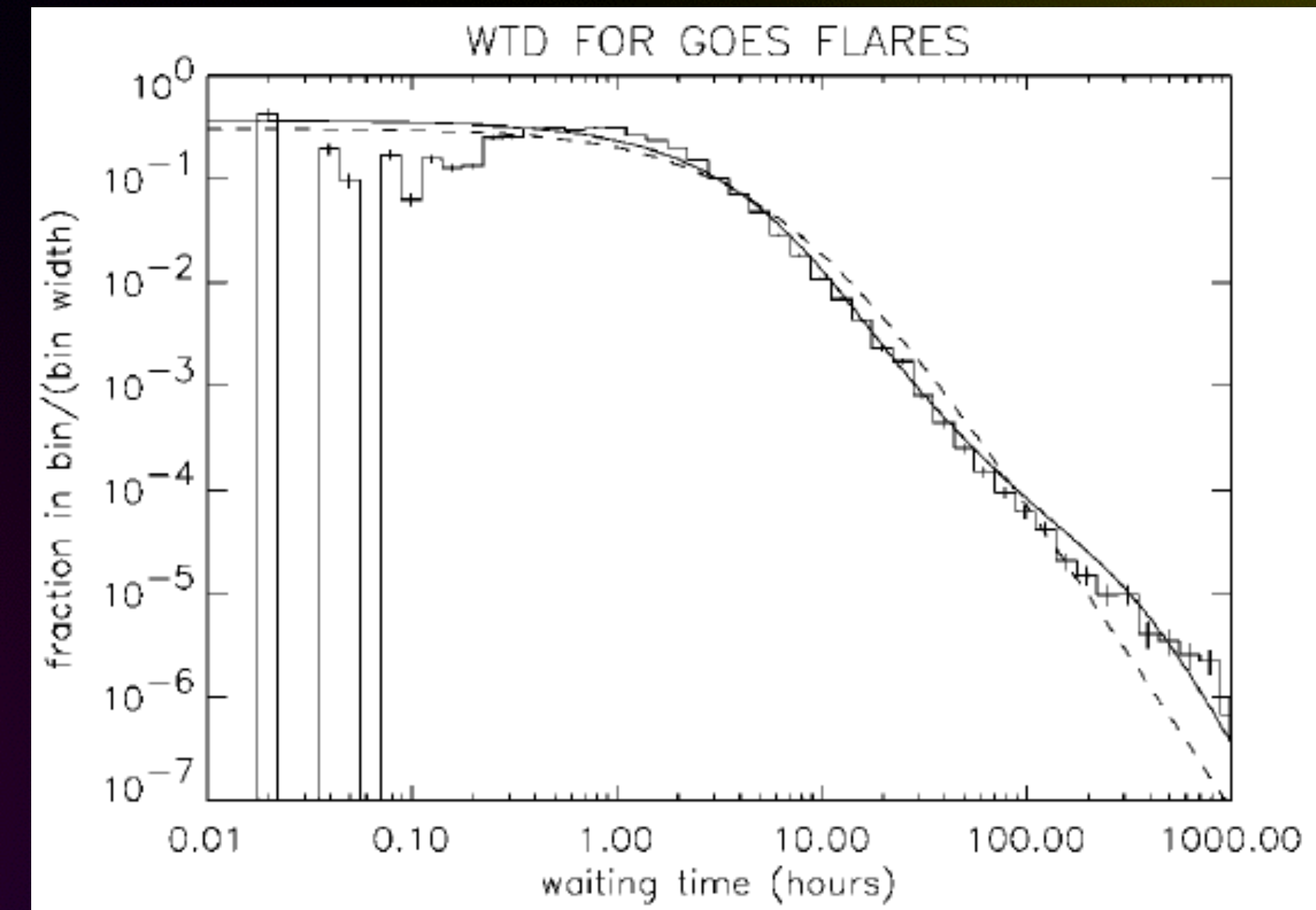


Crosby, PhD Thesis (1996)



Bofetta et al., (1999)

Robust power-law of waiting times: a system perfectly keeping a memory in giving flares



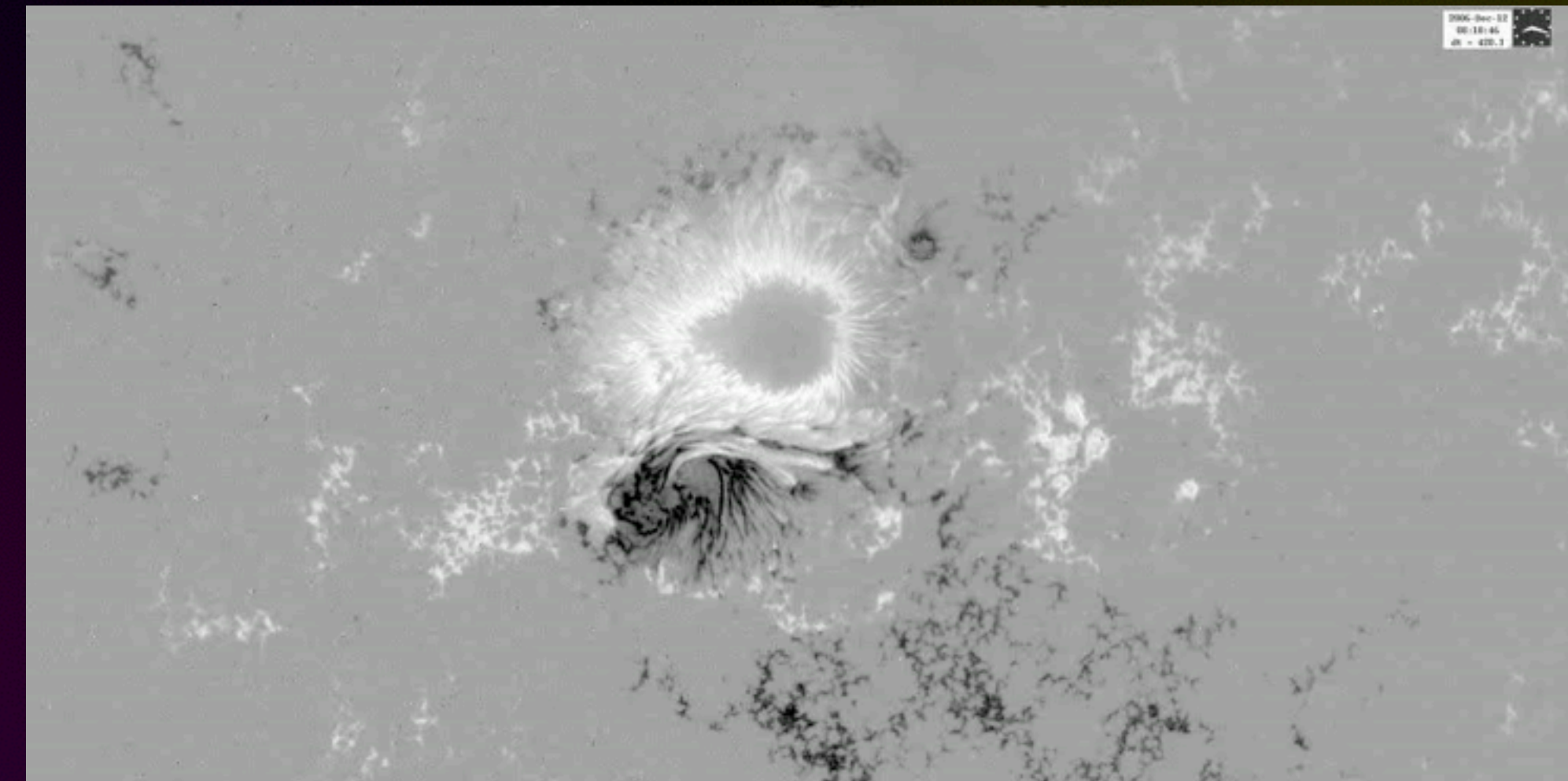
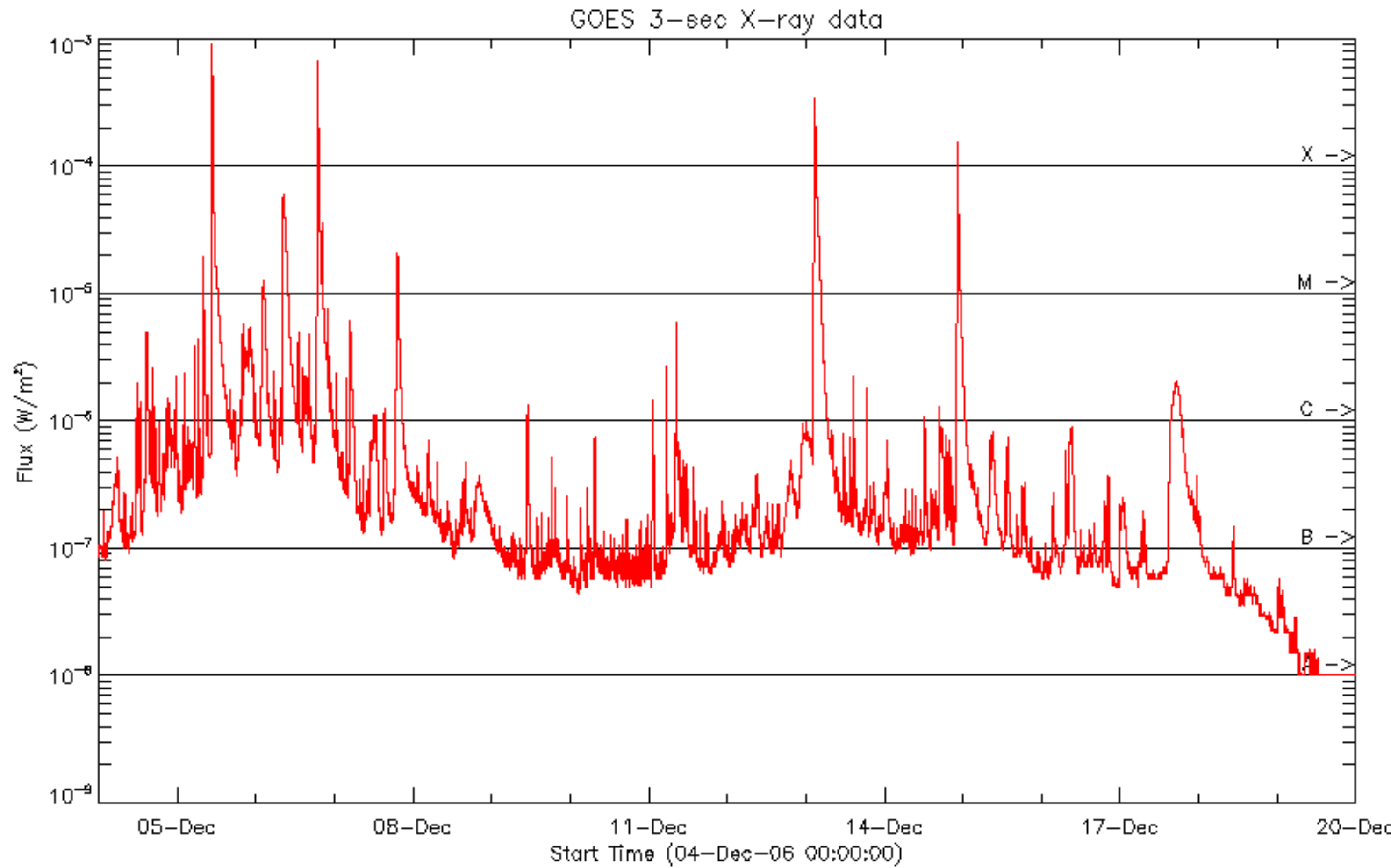
Wheatland (2000)

Time-dependent Poisson scaling in waiting times: some memory kept, with stochasticity demonstrated in an exponential distribution of different flaring rates



A MIX OF STOCHASTICITY AND MEMORY

- NOAA AR 10930
- Period observed: ~16 days



- Clustering of flares in a flaring active region
- Flaring features of active regions, i.e., complex magnetic PILs, continuously and consistently driven
- Typical situation of a pink-noise dynamical response timeseries

Response of NOAA AR 10930 over a two-week period in Dec 2006



ESWW13

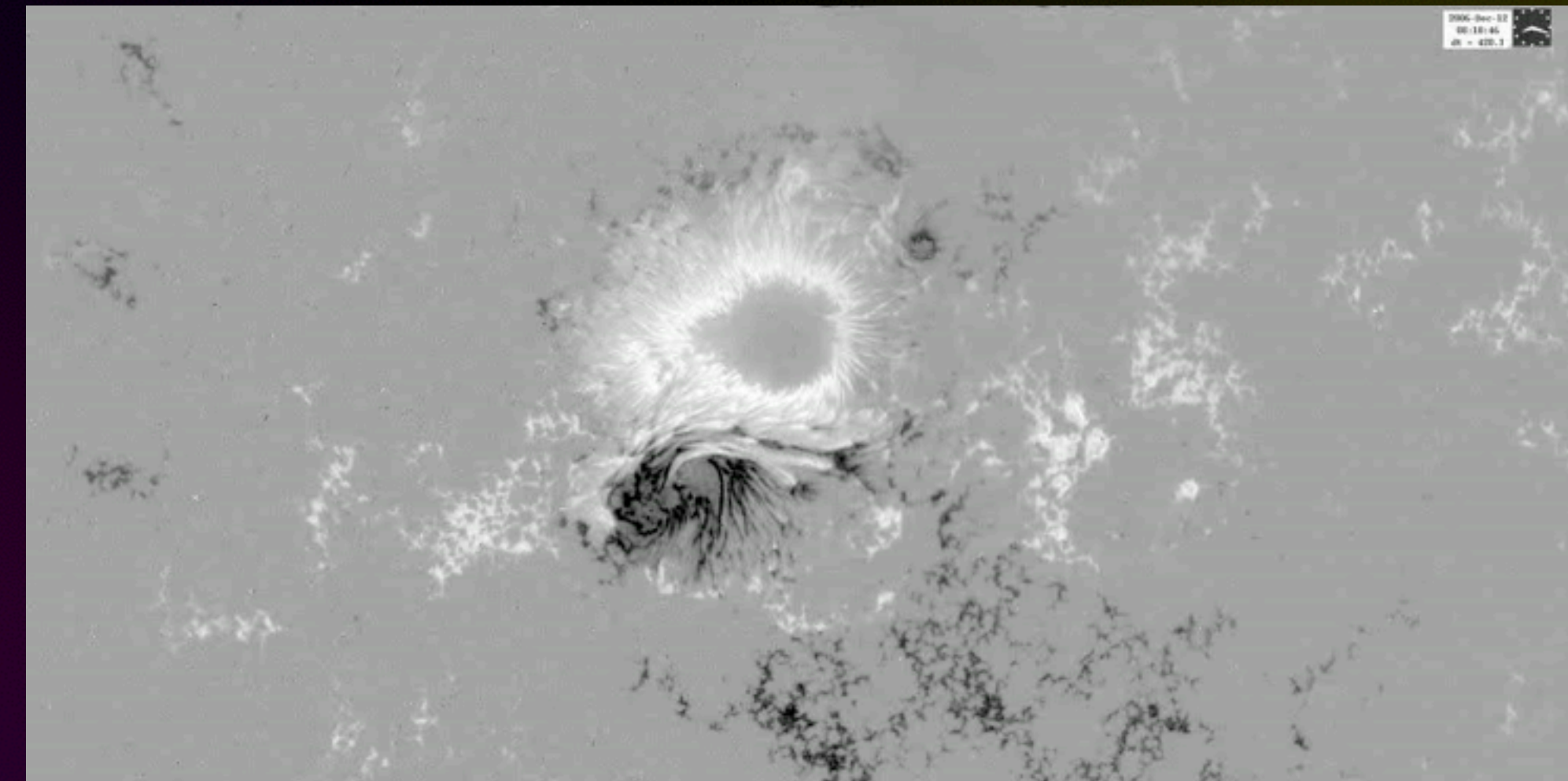
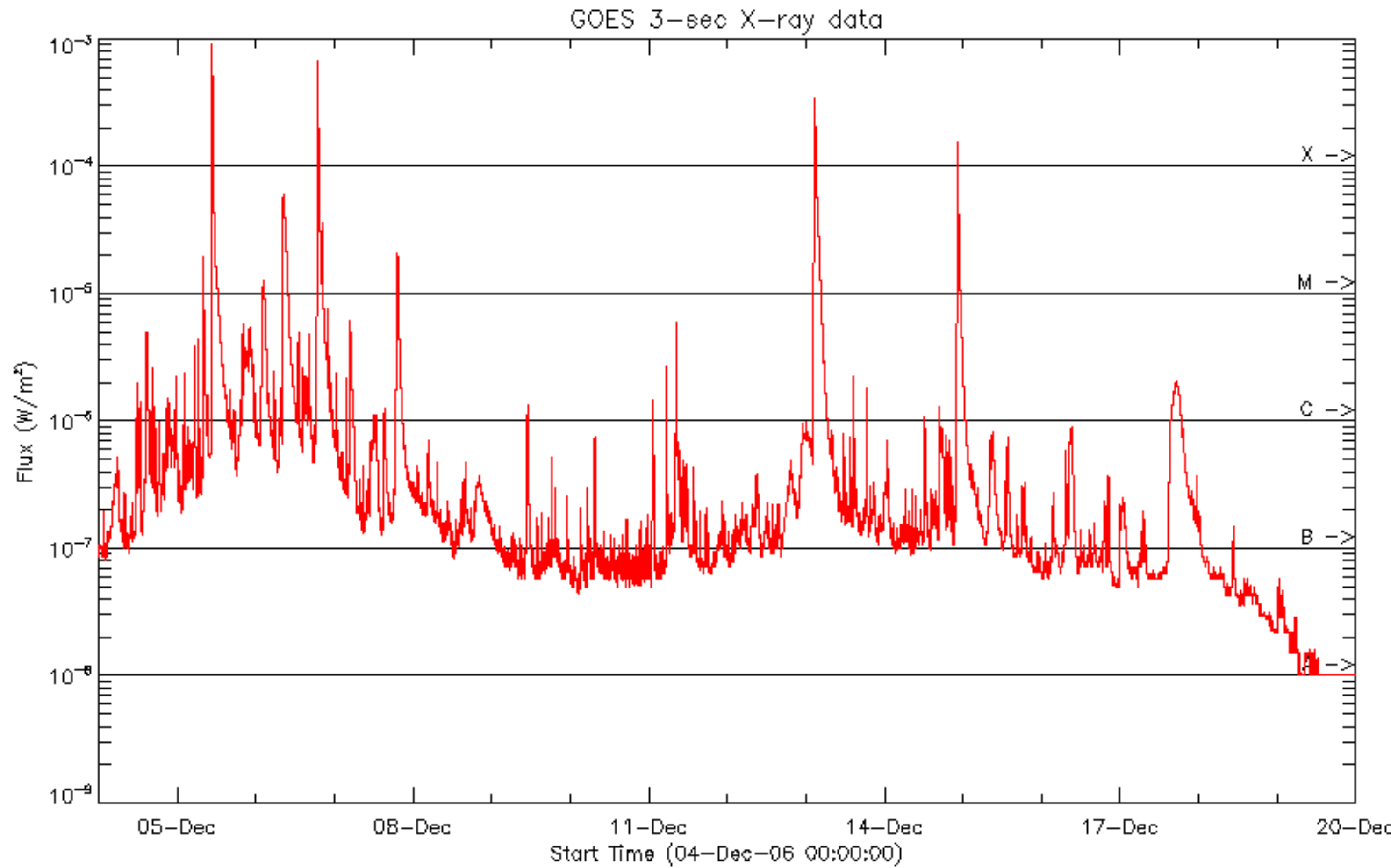
M. K. Georgoulis & R. Qahwaji

Oostende, November 18, 2016



A MIX OF STOCHASTICITY AND MEMORY

- NOAA AR 10930
- Period observed: ~16 days



- Clustering of flares in a flaring active region
- Flaring features of active regions, i.e., complex magnetic PILs, continuously and consistently driven
- Typical situation of a pink-noise dynamical response timeseries

Response of NOAA AR 10930 over a two-week period in Dec 2006



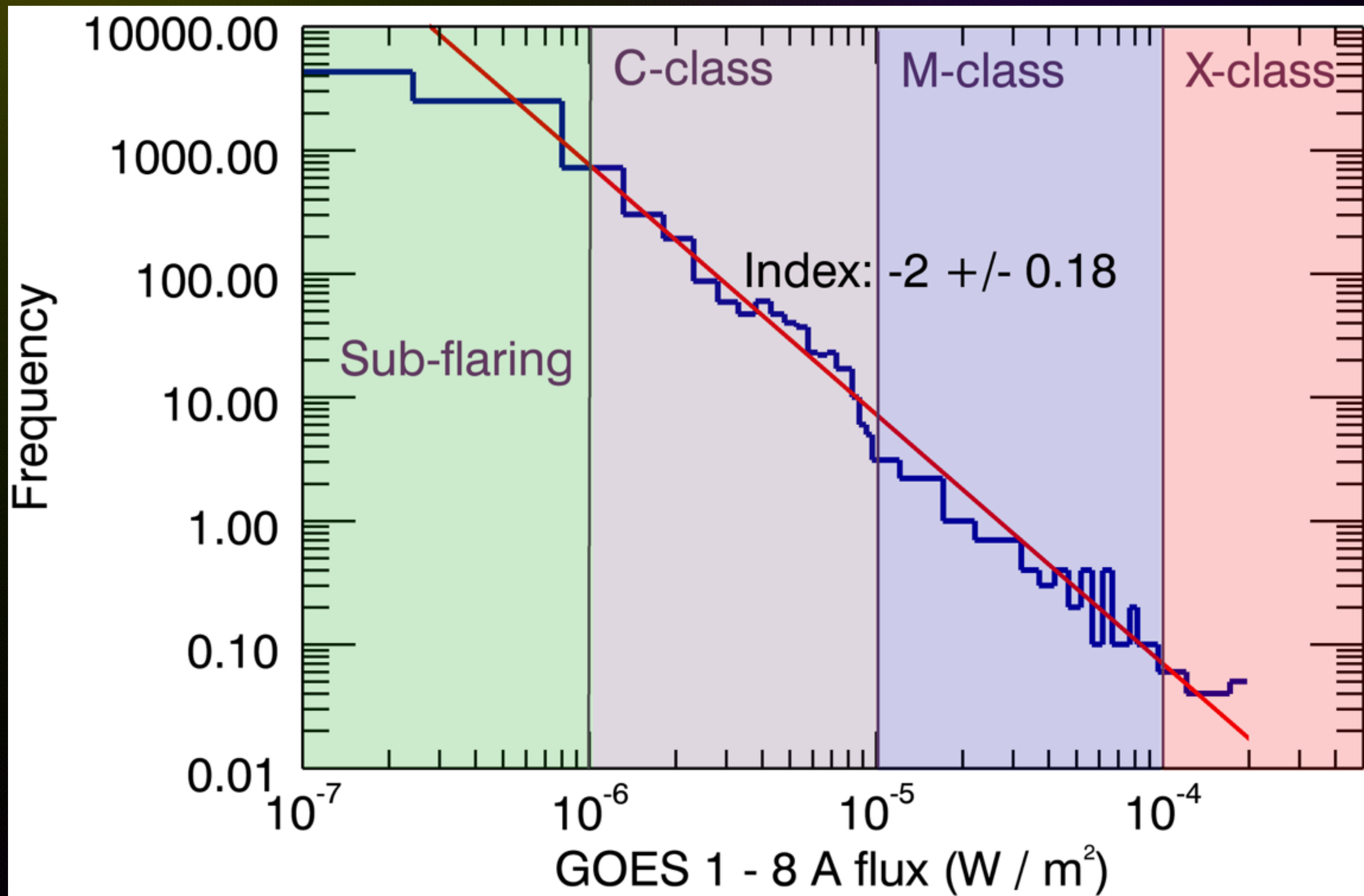
ESWW13

M. K. Georgoulis & R. Qahwaji

Oostende, November 18, 2016

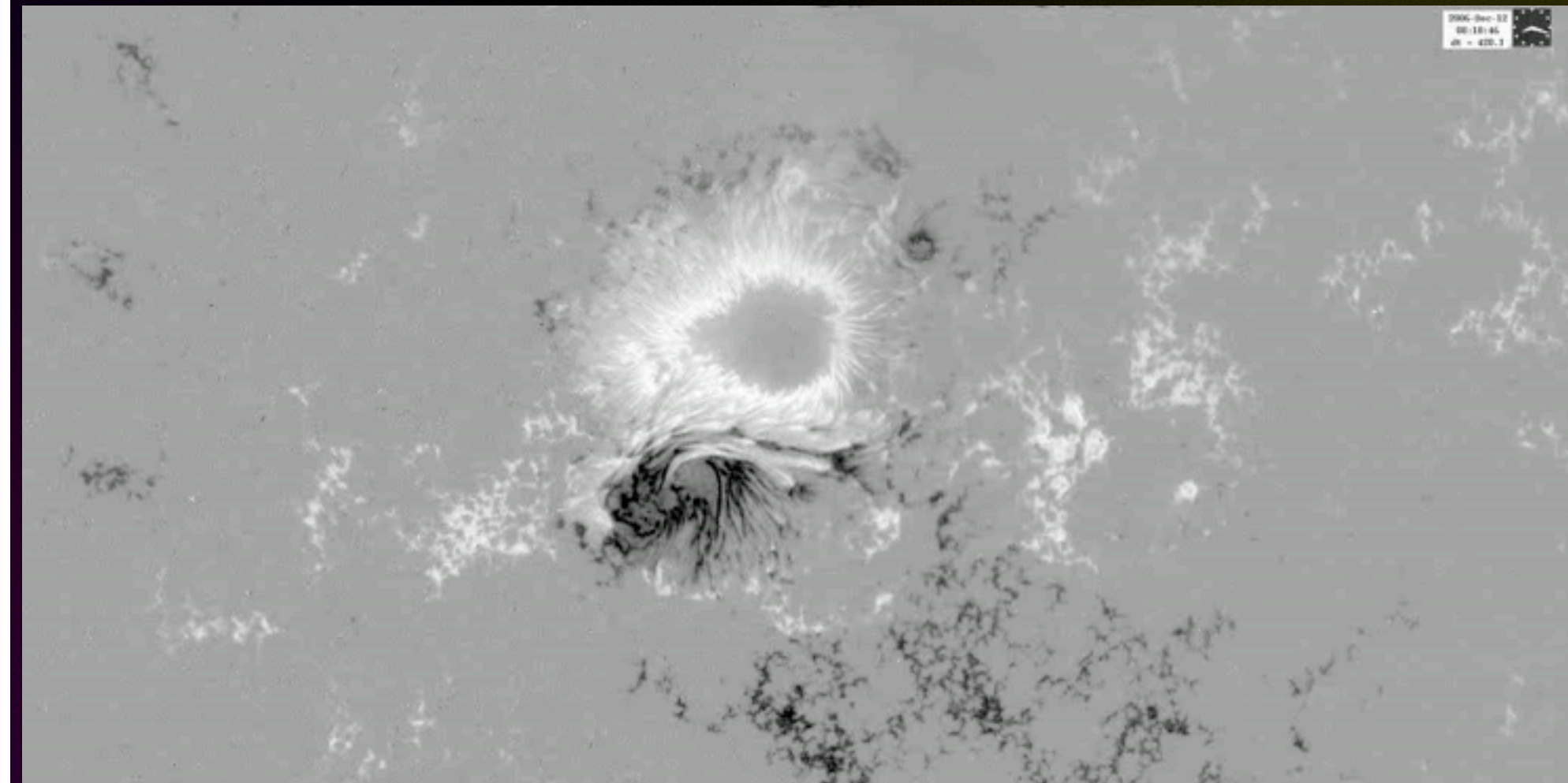


A MIX OF STOCHASTICITY AND MEMORY



Response of NOAA AR 10930 over a two-week period in Dec 2006

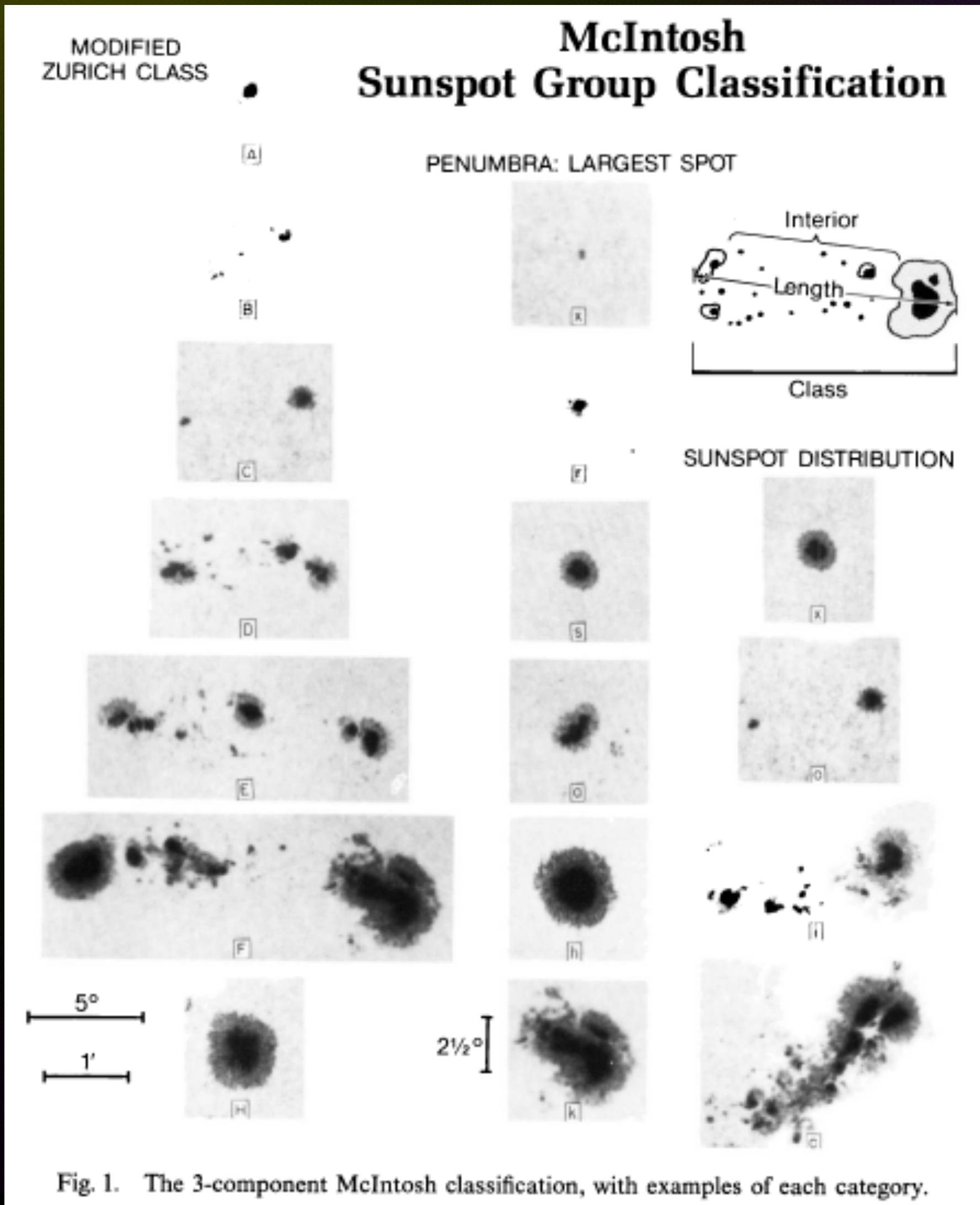
- NOAA AR 10930
- Period observed: ~16 days



- Clustering of flares in a flaring active region
- Flaring features of active regions, i.e., complex magnetic PILs, continuously and consistently driven
- Typical situation of a pink-noise dynamical response timeseries



QUALITATIVE COMPLEXITY CLASSIFICATION



McIntosh (1990)

Mount Wilson classification

alpha: A unipolar sunspot group.

beta: A sunspot group having both positive and negative magnetic polarities (bipolar), with a simple and distinct division between the polarities.

gamma: A complex active region in which the positive and negative polarities are so irregularly distributed as to prevent classification as a bipolar group.

beta-gamma: A sunspot group that is bipolar but which is sufficiently complex that no single, continuous line can be drawn between spots of opposite polarities.

delta: A qualifier to magnetic classes (see below) indicating that umbrae separated by less than 2 degrees within one penumbra have opposite polarity.

beta-delta: A sunspot group of general beta magnetic classification but containing one (or more) delta spot(s).

beta-gamma-delta: A sunspot group of beta-gamma magnetic classification but containing one (or more) delta spot(s).

gamma-delta: A sunspot group of gamma magnetic classification but containing one (or more) delta spot(s).

Source: spaceweather.com



QUALITATIVE COMPLEXITY CLASSIFICATION



McIntosh (1990)

Mount Wilson classification

alpha: A unipolar sunspot group.

beta: A sunspot group having both positive and negative magnetic polarities (bipolar), with a simple and distinct division between the polarities.

gamma: A complex active region in which the positive and negative polarities are so irregularly distributed as to prevent classification as a bipolar group.

beta-gamma: A sunspot group that is bipolar but which is sufficiently complex that no single, continuous line can be drawn between spots of opposite polarities.

delta: A qualifier to magnetic classes (see below) indicating that umbrae separated by less than 1 degree within one penumbra have opposite polarity.

beta-delta: A sunspot group of general beta magnetic classification but containing one (or more) delta spot(s).

beta-gamma-delta: A sunspot group of beta-gamma magnetic classification but containing one (or more) delta spot(s).

gamma-delta: A sunspot group of gamma magnetic classification but containing one (or more) delta spot(s).

Source: spaceweather.com



QUANTITATIVE COMPLEXITY CLASSIFICATION

Numerous methods over the past 20 years. An effort to categorize them results in the following (*Georgoulis, 2012*):



QUANTITATIVE COMPLEXITY CLASSIFICATION

Numerous methods over the past 20 years. An effort to categorize them results in the following (*Georgoulis, 2012*):

- Monoscale / multiscale methods
- Morphological methods
- Statistical methods (on historical & archived data)
- Machine-learning, combinatorial, & assimilation methods
- Analytical methods
- Local helioseismology methods
- Other (slightly exotic) methods

QUANTITATIVE COMPLEXITY CLASSIFICATION

Numerous methods over the past 20 years. An effort to categorize them results in the following (*Georgoulis, 2012*):

- Monoscale / multiscale methods
- Morphological methods
- Statistical methods (on historical & archived data)
- Machine-learning, combinatorial, & assimilation methods
- Analytical methods
- Local helioseismology methods
- Other (slightly exotic) methods

Abramenko et al. (2002, 2003); McAteer et al. (2005); Georgoulis (2005, 2012); Uritsky et al. (2007, 2013); Hewett et al. (2008); Conlon et al. (2010); Kestener et al. (2010), McAteer (2015)

Falconer et al. (2001, 2002, 2003, 2008, 2009, 2011); Georgoulis & Rust (2007); Schrijver (2007); Mason & Hoeksema (2010); Leka & Barnes (2003a; b); Cabnfield et al. (1999); Barnes & Leka (2008), Korsos et al. (2015)

Wheatland (2001); Moon et al. (2001); Gallagher et al. (2002); Wheatland (2004, 2005a, b)

Belanger et al. (2007); Qahwaji & Colak (2007); Colak & Qahwaji (2008, 2009); Qahwaji et al. (2008); Al-Omari et al. (2010); Yu et al. (2009; 2010a, b); Huang et al. (2010); Bobra & Couvidat (2014); Bobra & Ilonidis (2015); Boucheron et al., (2015); Nishizuka et al., (2016)

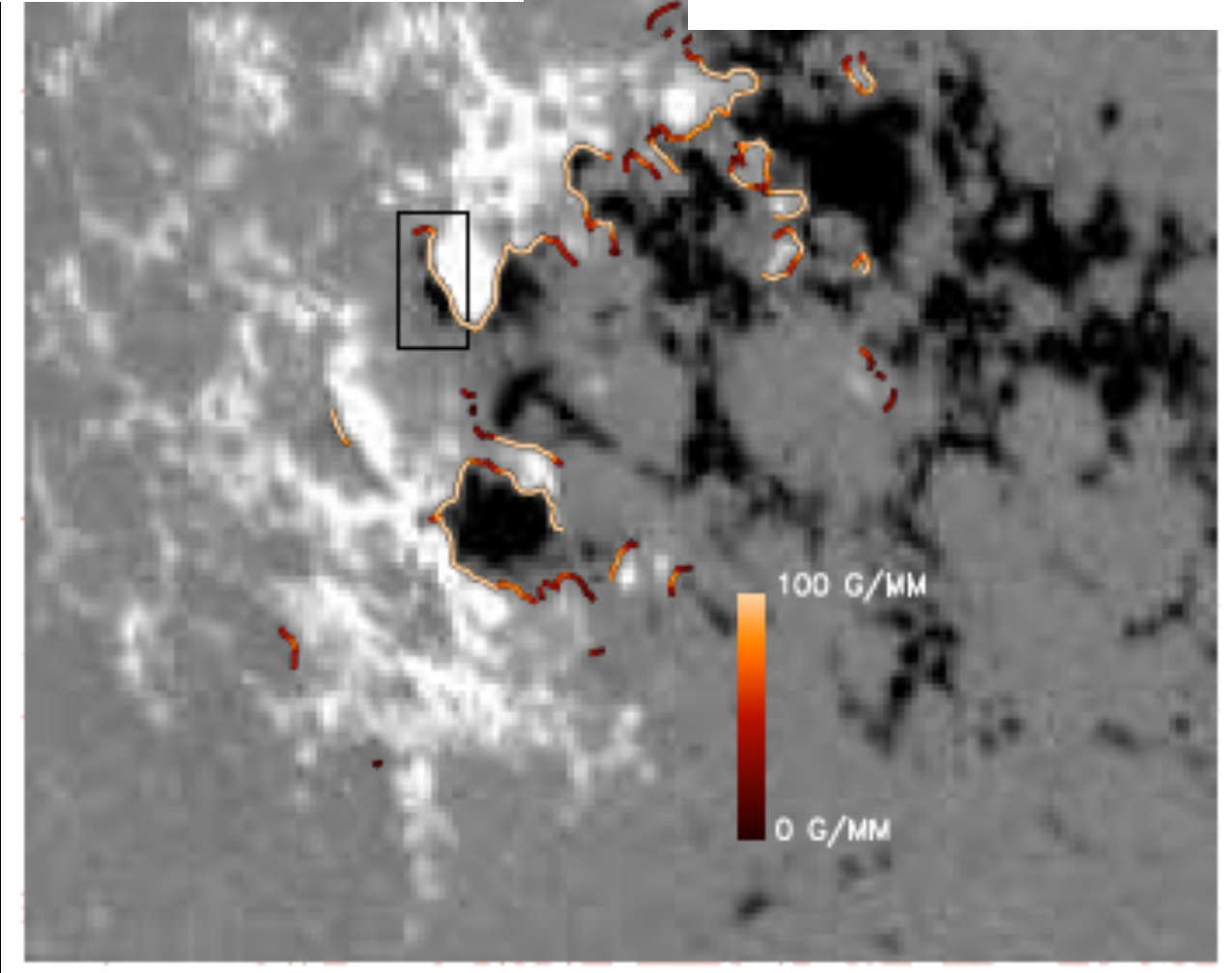
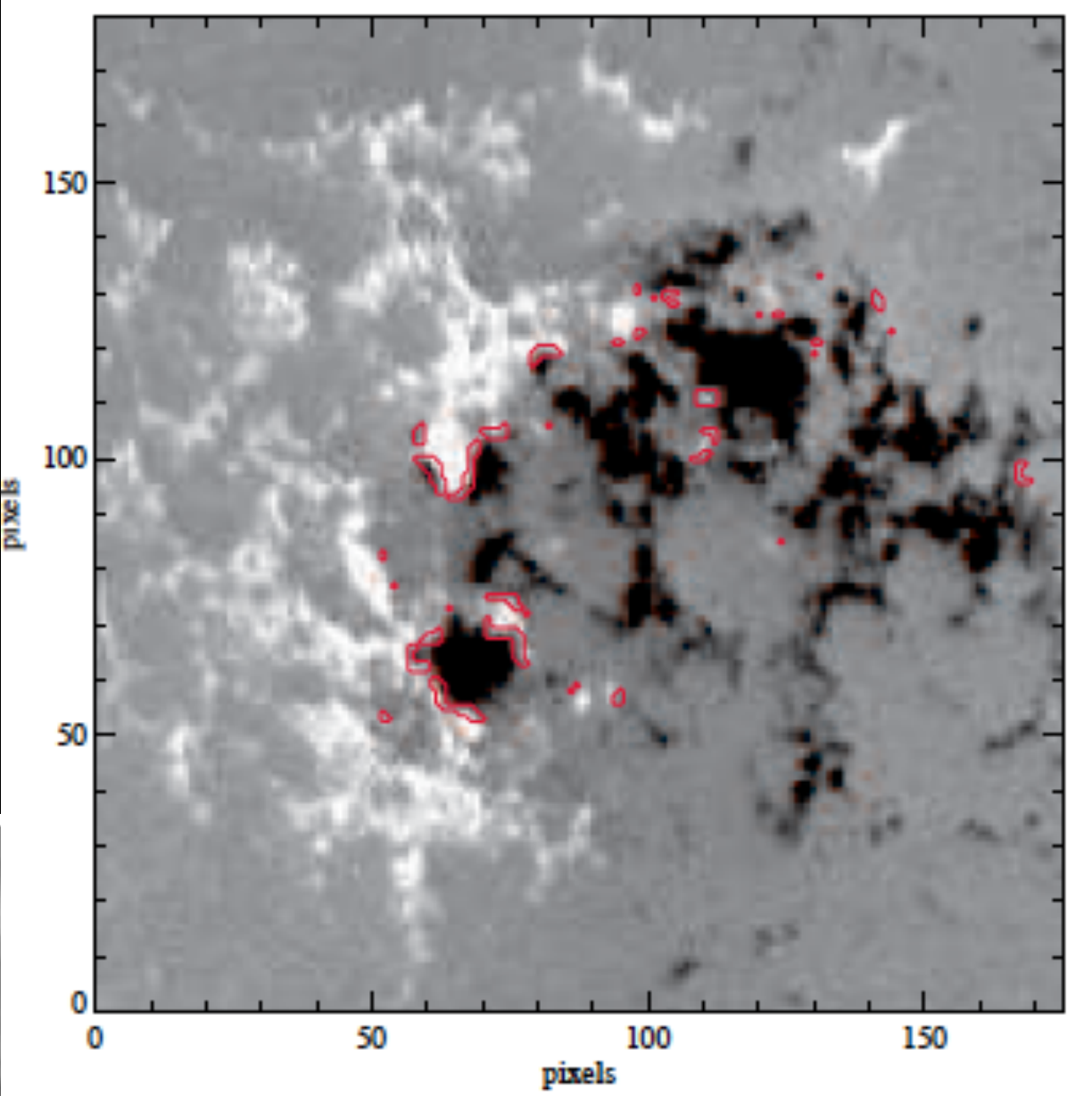
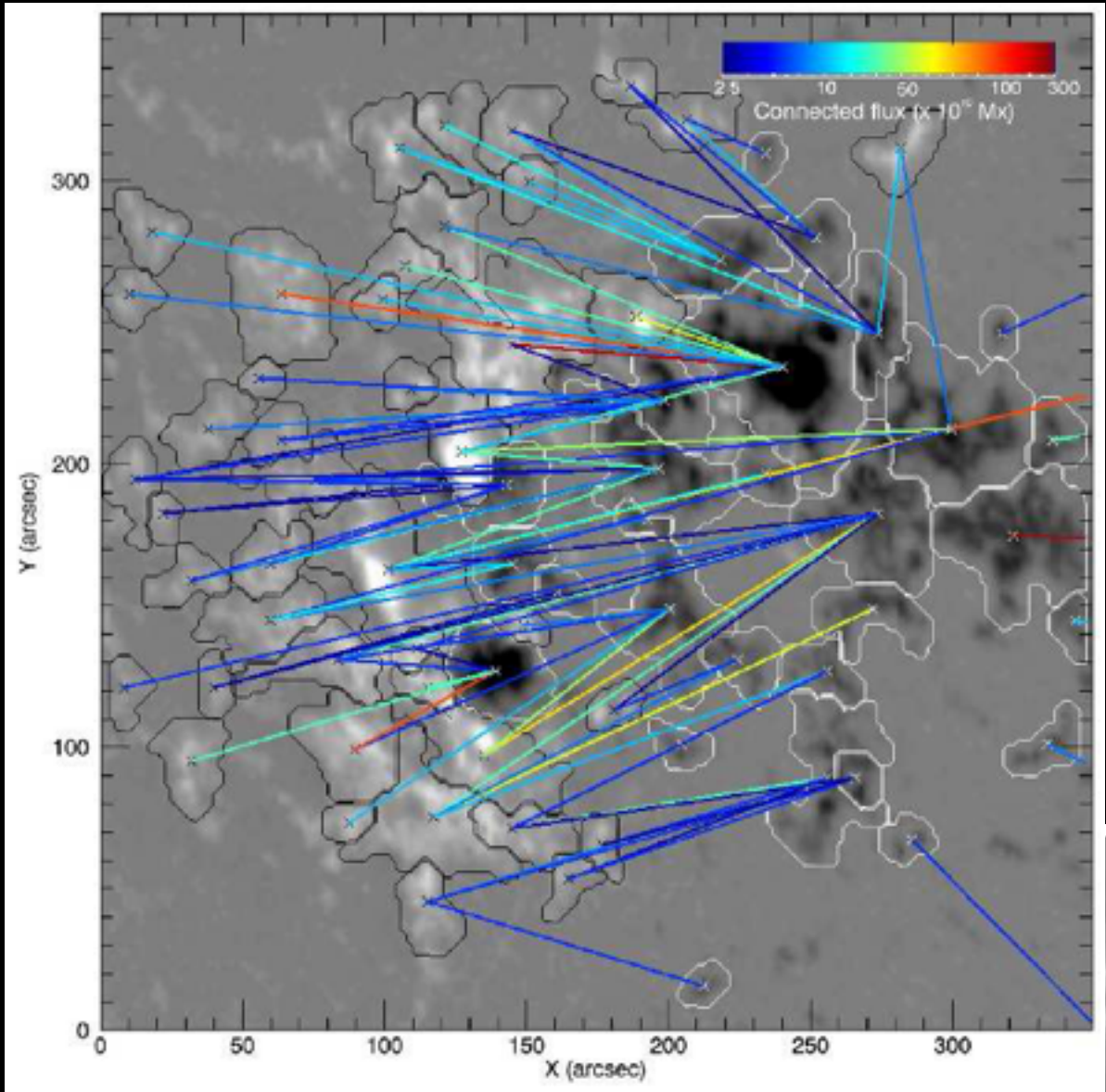
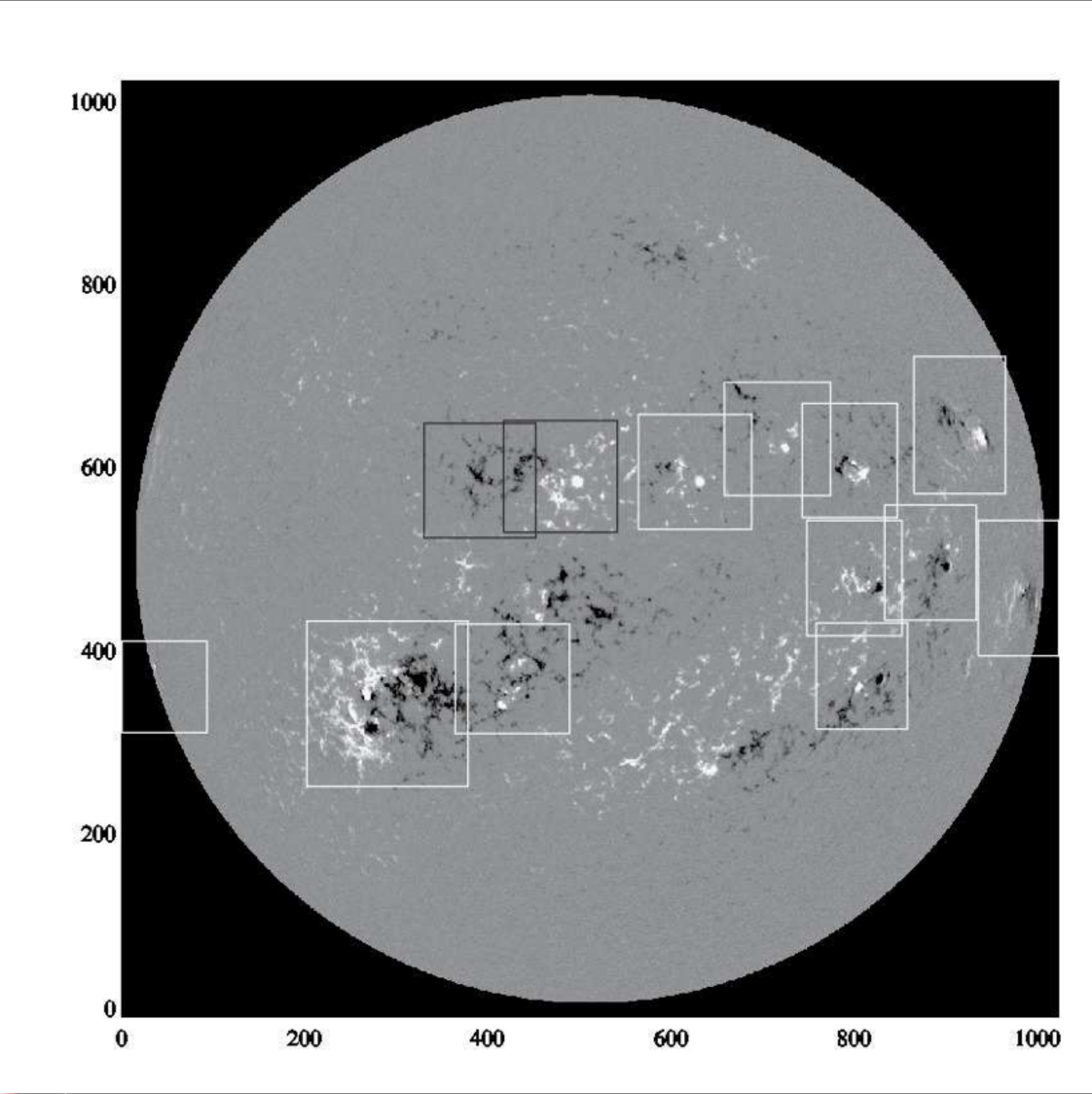
Wheatland & Glukhov (1998); Wheatland (2008)

Reinard et al. (2010); Komm et al. (2011), etc.

Jenkins & Fischbach (2009); Javorsek et al. (2012); Strugarek & Charbonneau (2014)



ANALYSIS OF PHOTOSPHERIC ACTIVE-REGION MAGNETOGRAMS

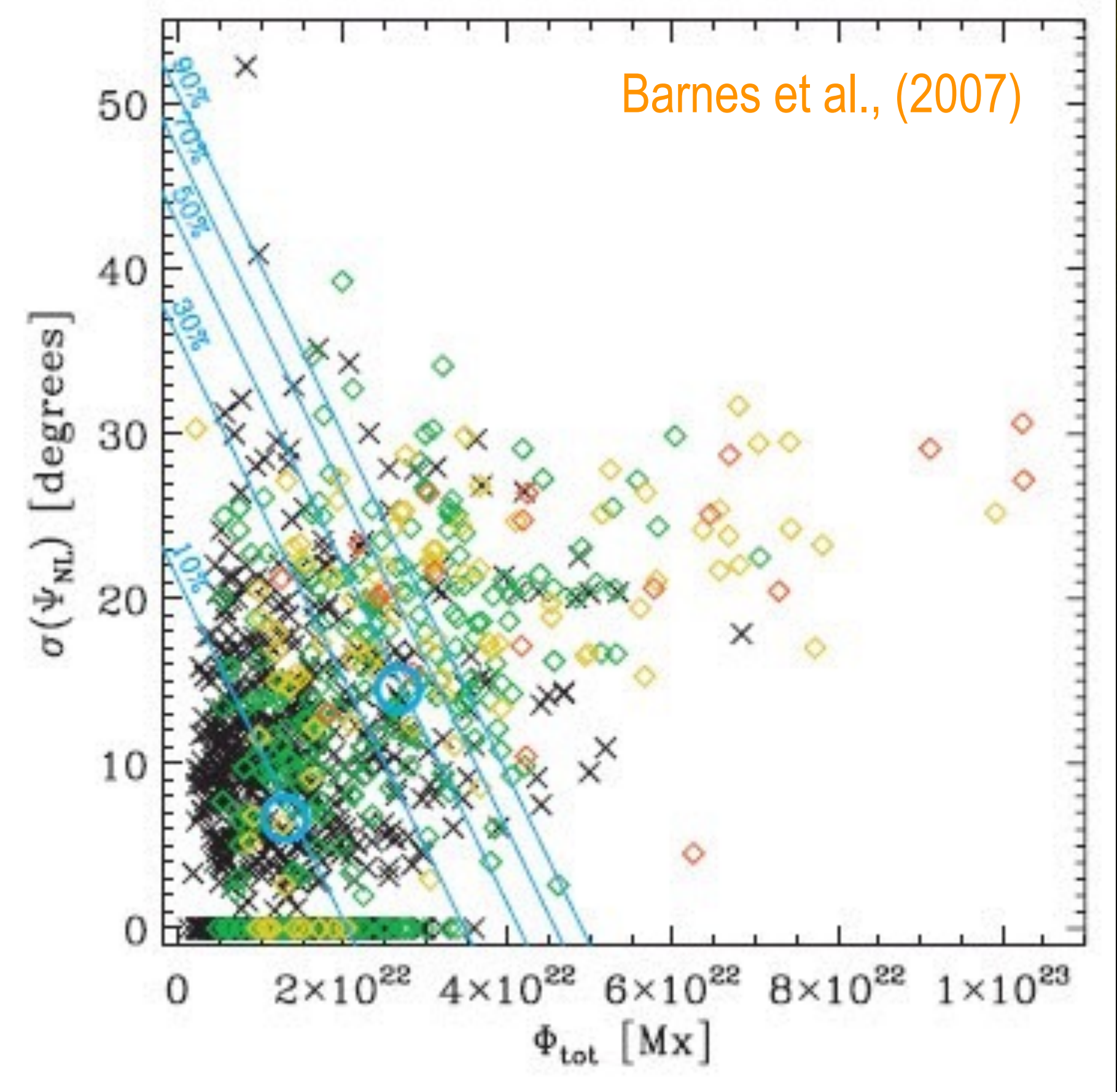


Barnes et al., (2016)



PROPERTIES TRANSLATED TO PREDICTIVE PROBABILITIES

Keyword	Description	Formula	F-Score	Selection
TOTUSJH	Total unsigned current helicity	$H_{c\text{total}} \propto \sum B_z \cdot J_z $	3560	Included
TOTBSQ	Total magnitude of Lorentz force	$F \propto \sum B^2$	3051	Included
TOTPOT	Total photospheric magnetic free energy density	$\rho_{\text{tot}} \propto \sum (B^{\text{Obs}} - B^{\text{Pot}})^2 dA$	2996	Included
TOTUSJZ	Total unsigned vertical current	$J_{z\text{total}} = \sum J_z dA$	2733	Included
ABSNJZH	Absolute value of the net current helicity	$H_{c\text{abs}} \propto \sum B_z \cdot J_z $	2618	Included
SAVNCPP	Sum of the modulus of the net current per polarity	$J_{z\text{sum}} \propto \left \sum_{B_z^+} J_z dA \right + \left \sum_{B_z^-} J_z dA \right $	2448	Included
USFLUX	Total unsigned flux	$\Phi = \sum B_z dA$	2437	Included
AREA_ACR	Area of strong field pixels in the active region	$\text{Area} = \sum \text{Pixels}$	2047	Included
TOTFZ	Sum of z-component of Lorentz force	$F_z \propto \sum (B_x^2 + B_y^2 - B_z^2) dA$	1371	Included
MEANPOT	Mean photospheric magnetic free energy	$\bar{\rho} \propto \frac{1}{N} \sum (B^{\text{Obs}} - B^{\text{Pot}})^2$	1064	Included
R_VALUE	Sum of flux near polarity inversion line	$\Phi = \sum B_{\text{LoS}} dA \text{ within } R \text{ mask}$	1057	Included
EPSZ	Sum of z-component of normalized Lorentz force	$\delta F_z \propto \frac{\sum (B_x^2 + B_y^2 - B_z^2)}{\sum B^2}$	864.1	Included
SHRGT45	Fraction of Area with shear > 45°	$\text{Area with shear} > 45^\circ / \text{total area}$	740.8	Included
MEANSHR	Mean shear angle	$\bar{\Gamma} = \frac{1}{N} \sum \arccos \left(\frac{B^{\text{Obs}} \cdot B^{\text{Pot}}}{ B^{\text{Obs}} B^{\text{Pot}} } \right)$	727.9	Discarded
MEANGAM	Mean angle of field from radial	$\bar{\gamma} = \frac{1}{N} \sum \arctan \left(\frac{B_h}{B_z} \right)$	573.3	Discarded
MEANGBT	Mean gradient of total field	$ \nabla B_{\text{tot}} = \frac{1}{N} \sum \sqrt{\left(\frac{\partial B}{\partial x} \right)^2 + \left(\frac{\partial B}{\partial y} \right)^2}$	192.3	Discarded
MEANGBZ	Mean gradient of vertical field	$ \nabla B_z = \frac{1}{N} \sum \sqrt{\left(\frac{\partial B_z}{\partial x} \right)^2 + \left(\frac{\partial B_z}{\partial y} \right)^2}$	88.40	Discarded
MEANGBH	Mean gradient of horizontal field	$ \nabla B_h = \frac{1}{N} \sum \sqrt{\left(\frac{\partial B_h}{\partial x} \right)^2 + \left(\frac{\partial B_h}{\partial y} \right)^2}$	79.40	Discarded
MEANJZH	Mean current helicity (B_z contribution)	$\bar{H}_c \propto \frac{1}{N} \sum B_z \cdot J_z$	46.73	Discarded
TOTFY	Sum of y-component of Lorentz force	$F_y \propto \sum B_y B_z dA$	28.92	Discarded
MEANJZD	Mean vertical current density	$\bar{J}_z \propto \frac{1}{N} \sum \left(\frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} \right)$	17.44	Discarded
MEANALP	Mean characteristic twist parameter, α	$\alpha_{\text{total}} \propto \frac{\sum J_z \cdot B_z}{\sum B_z^2}$	10.41	Discarded
TOTFX	Sum of x-component of Lorentz force	$F_x \propto -\sum B_x B_z dA$	6.147	Discarded
EPSY	Sum of y-component of normalized Lorentz force	$\delta F_y \propto \frac{-\sum B_y B_z}{\sum B^2}$	0.647	Discarded
EPSX	Sum of x-component of normalized Lorentz force	$\delta F_x \propto \frac{\sum B_x B_z}{\sum B^2}$	0.366	Discarded



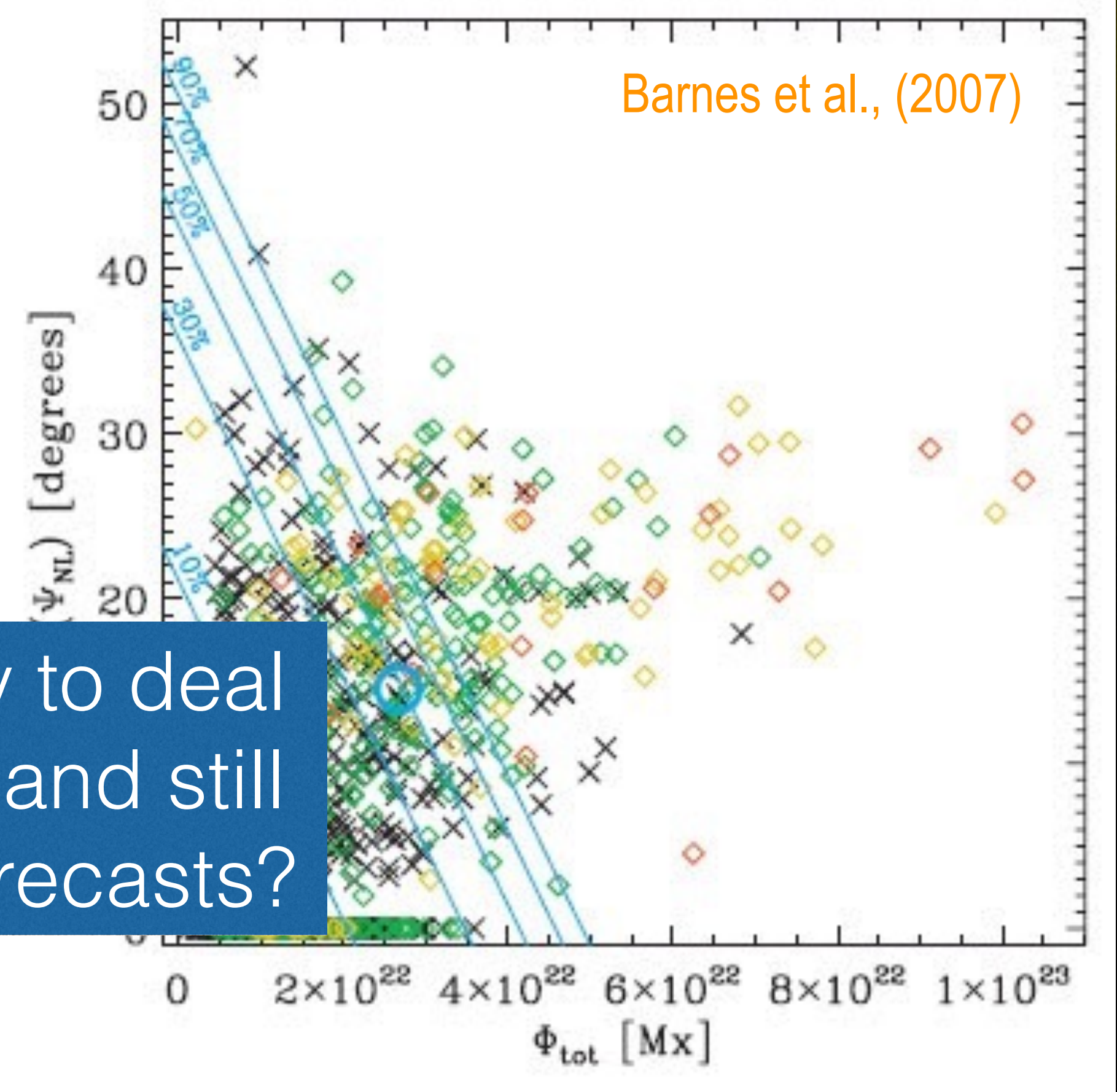
Discriminant analysis: Two-function, linear DA for four-class prediction (non-flaring, C, M, and X-class)



PROPERTIES TRANSLATED TO PREDICTIVE PROBABILITIES

Keyword	Description	Formula	F-Score	Selection
TOTUSJH	Total unsigned current helicity	$H_{c\text{total}} \propto \sum B_z \cdot J_z $	3560	Included
TOTBSQ	Total magnitude of Lorentz force	$F \propto \sum B^2$	3051	Included
TOTPOT	Total photospheric magnetic free energy density	$\rho_{\text{tot}} \propto \sum (B^{\text{Obs}} - B^{\text{Pot}})^2 dA$	2996	Included
TOTUSJZ	Total unsigned vertical current	$J_{z\text{total}} = \sum J_z dA$	2733	Included
ABSNJZH	Absolute value of the net current helicity	$H_{c\text{abs}} \propto \sum B_z \cdot J_z $	2618	Included
SAVNCPP	Sum of the modulus of the net current per polarity	$J_{z\text{sum}} \propto \left \sum_{B_z^+} J_z dA \right + \left \sum_{B_z^-} J_z dA \right $	2448	Included
USFLUX	Total unsigned flux	$\Phi = \sum B_z dA$	2437	Included
AREA_ACR	Area of strong field pixels in the active region	$\text{Area} = \sum \text{Pixels}$	2047	Included
TOTFZ	Sum of z-component of Lorentz force	$F_z \propto \sum (B_x^2 + B_y^2 - B_z^2) dA$	1371	Included
MEANPOT	Mean photospheric magnetic free energy	$\bar{\rho} \propto \frac{1}{N} \sum (B^{\text{Obs}} - B^{\text{Pot}})^2$	1064	Included
R_VALUE	Sum of flux near polarity inversion line	$\Phi = \sum B_{\text{LOS}} dA \text{ within } R \text{ mask}$	1057	Included
EPSZ	Sum of z-component of normalized Lorentz force	$\delta F_z \propto \frac{\sum (B_x^2 + B_y^2 - B_z^2)}{\sum B^2}$	864.1	Included
SHRGT45	Fraction of Area with shear > 45°	Area with shear > 45° / total area	718.8	Included
MEANSHR	Mean shear angle	$\bar{\Gamma} = \frac{1}{N} \sum \Gamma$	718.8	Included
MEANGAM	Mean angle of field from radial	$\bar{\gamma} = \frac{1}{N} \sum \gamma$	718.8	Included
MEANGBT	Mean gradient of total field	$ \nabla B_{\text{tot}} $	718.8	Included
MEANGBZ	Mean gradient of vertical field	$ \nabla B_z $	718.8	Included
MEANGBH	Mean gradient of horizontal field	$ \nabla B_h = \frac{1}{N} \sum \sqrt{\left(\frac{\partial B_x}{\partial x}\right)^2 + \left(\frac{\partial B_x}{\partial y}\right)^2}$	718.8	Discarded
MEANJZH	Mean current helicity (B_z contribution)	$\bar{H}_c \propto \frac{1}{N} \sum B_z \cdot J_z$	46.73	Discarded
TOTFY	Sum of y-component of Lorentz force	$F_y \propto \sum B_y B_z dA$	28.92	Discarded
MEANJZD	Mean vertical current density	$\bar{J}_z \propto \frac{1}{N} \sum \left(\frac{\partial B_y}{\partial x} - \frac{\partial B_x}{\partial y} \right)$	17.44	Discarded
MEANALP	Mean characteristic twist parameter, α	$\alpha_{\text{total}} \propto \frac{\sum J_z \cdot B_z}{\sum B_z^2}$	10.41	Discarded
TOTFX	Sum of x-component of Lorentz force	$F_x \propto -\sum B_x B_z dA$	6.147	Discarded
EPSY	Sum of y-component of normalized Lorentz force	$\delta F_y \propto \frac{-\sum B_y B_z}{\sum B^2}$	0.647	Discarded
EPSX	Sum of x-component of normalized Lorentz force	$\delta F_x \propto \frac{\sum B_x B_z}{\sum B^2}$	0.366	Discarded

What is the optimal way to deal with all this information and still achieve reliable NRT forecasts?



Discriminant analysis: Two-function, linear DA for four-class prediction (non-flaring, C, M, and X-class)



RECENT TRENDS IN FLARE PREDICTION

- Most (excluding machine-learning) methods use a univariate predictor.



RECENT TRENDS IN FLARE PREDICTION

- Most (excluding machine-learning) methods use a univariate predictor.
- Multivariate forecasting can also be used in the form of :
 - Synthetic predictors:

$$predictor = \omega_1 predictor_1 + \omega_2 predictor_2 + \dots + \omega_n predictor_n$$

$$\omega_1, \omega_2, \dots, \omega_n \text{ unrestricted}$$

- Ensemble forecasting:

$$P(flare) = \omega_1 P_1(flare) + \omega_2 P_2(flare) + \dots + \omega_n P_n(flare)$$

$$\sum_{i=1}^n \omega_i = 1$$



RECENT TRENDS IN FLARE PREDICTION

- Most (excluding machine-learning) methods use a univariate predictor.
- Multivariate forecasting can also be used in the form of :
 - Synthetic predictors:

$$predictor = \omega_1 predictor_1 + \omega_2 predictor_2 + \dots + \omega_n predictor_n$$

$$\omega_1, \omega_2, \dots, \omega_n \text{ unrestricted}$$

- Ensemble forecasting:

$$P(flare) = \omega_1 P_1(flare) + \omega_2 P_2(flare) + \dots + \omega_n P_n(flare)$$

$$\sum_{i=1}^n \omega_i = 1$$

- **Task:** find $\omega_1, \omega_2, \dots, \omega_n$ such that validation results are optimized



RECENT TRENDS IN FLARE PREDICTION

- Most (excluding machine-learning) methods use a univariate predictor.
- Multivariate forecasting can also be used in the form of :
 - Synthetic predictors:

$$predictor = \omega_1 predictor_1 + \omega_2 predictor_2 + \dots + \omega_n predictor_n$$

$$\omega_1, \omega_2, \dots, \omega_n \text{ unrestricted}$$

- Ensemble forecasting:

$$P(flare) = \omega_1 P_1(flare) + \omega_2 P_2(flare) + \dots + \omega_n P_n(flare)$$

$$\sum_{i=1}^n \omega_i = 1$$

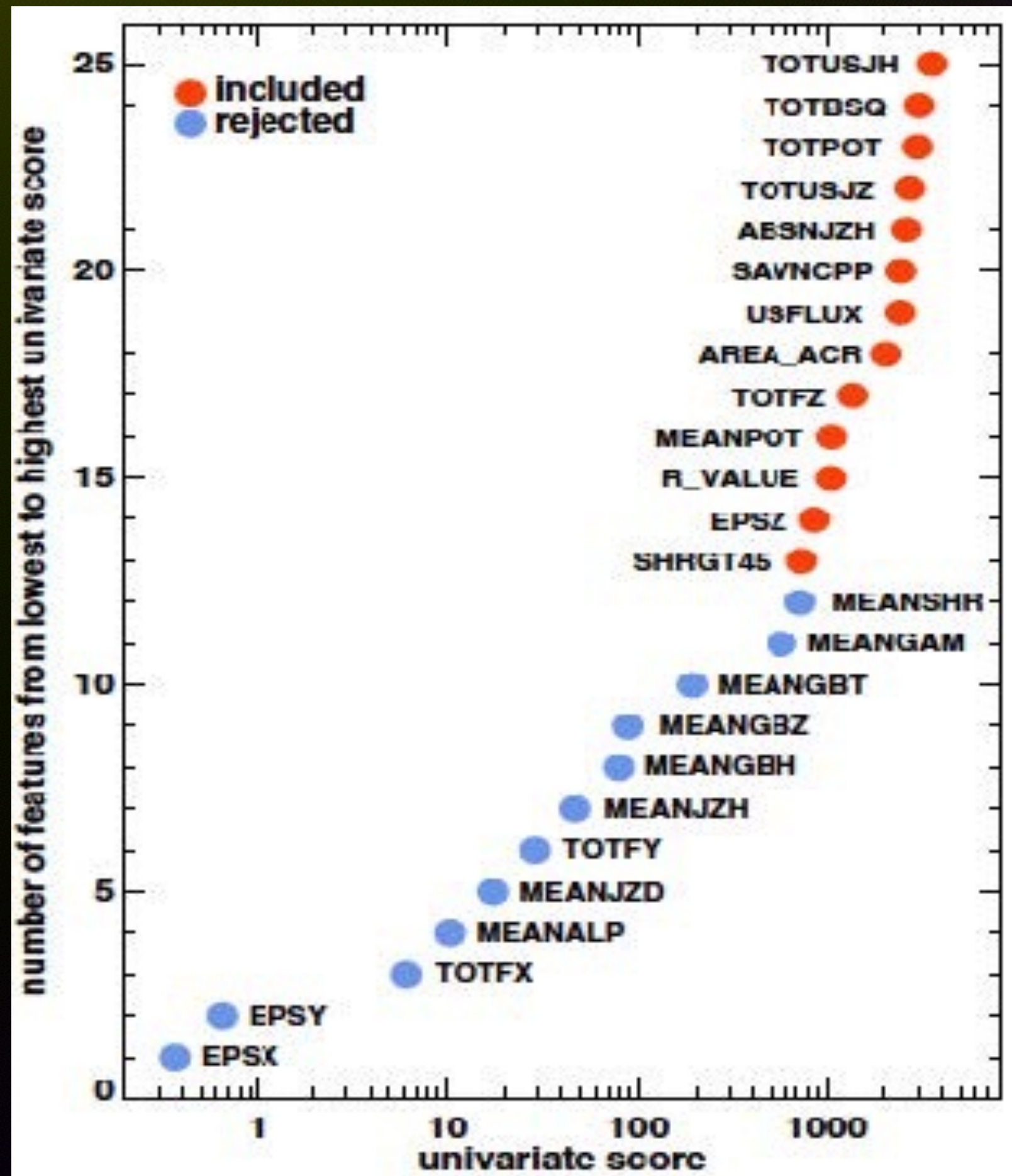
- **Task:** find $\omega_1, \omega_2, \dots, \omega_n$ such that validation results are optimized

However: optimization means different things to different communities!



INDICATIVE RESULTS

- Multivariate forecasting

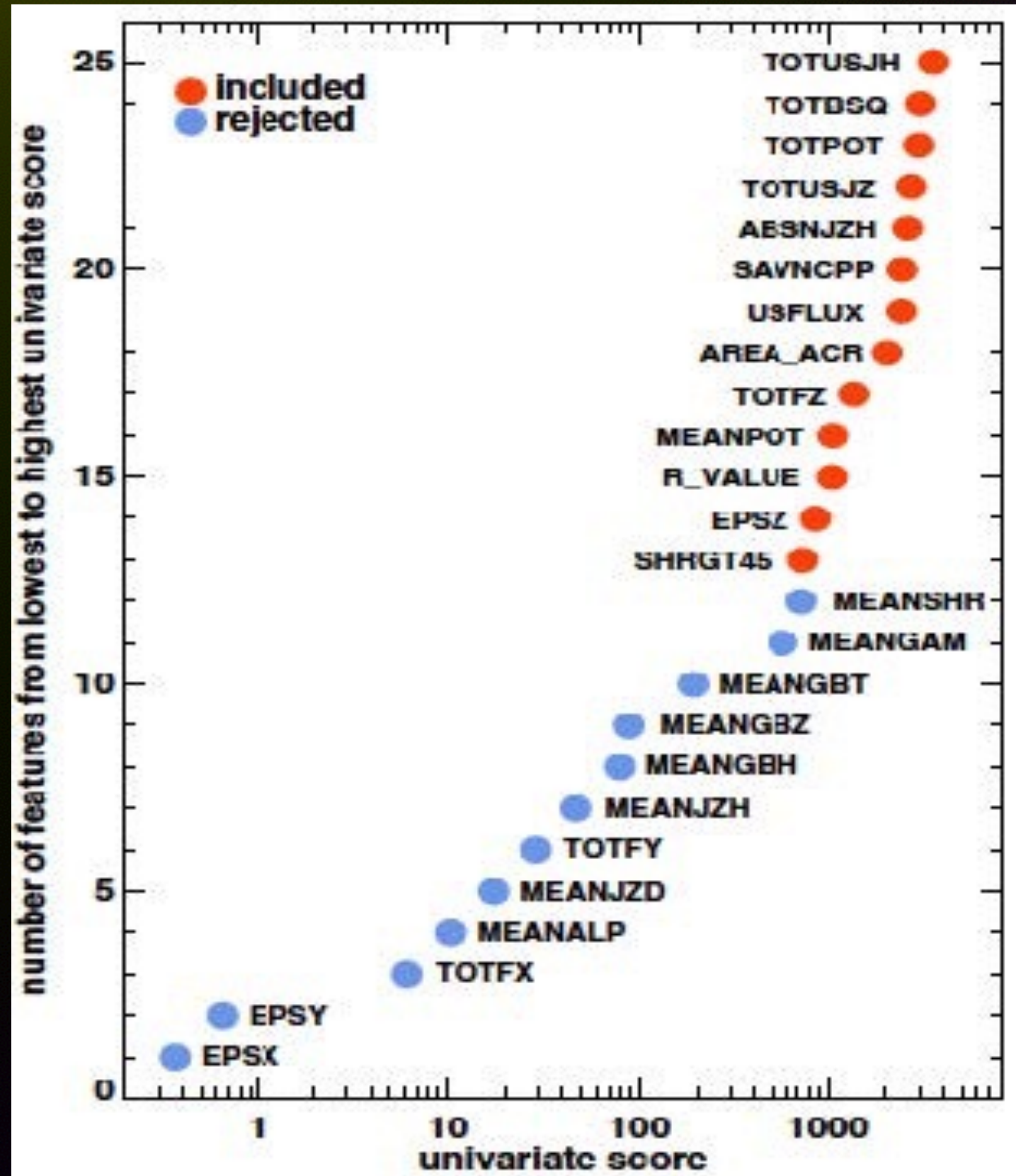


- Ordering of predictors by means of a univariate Fisher ranking score
- Machine-learning classifiers adopted

Bobra & Couvidat (2014)

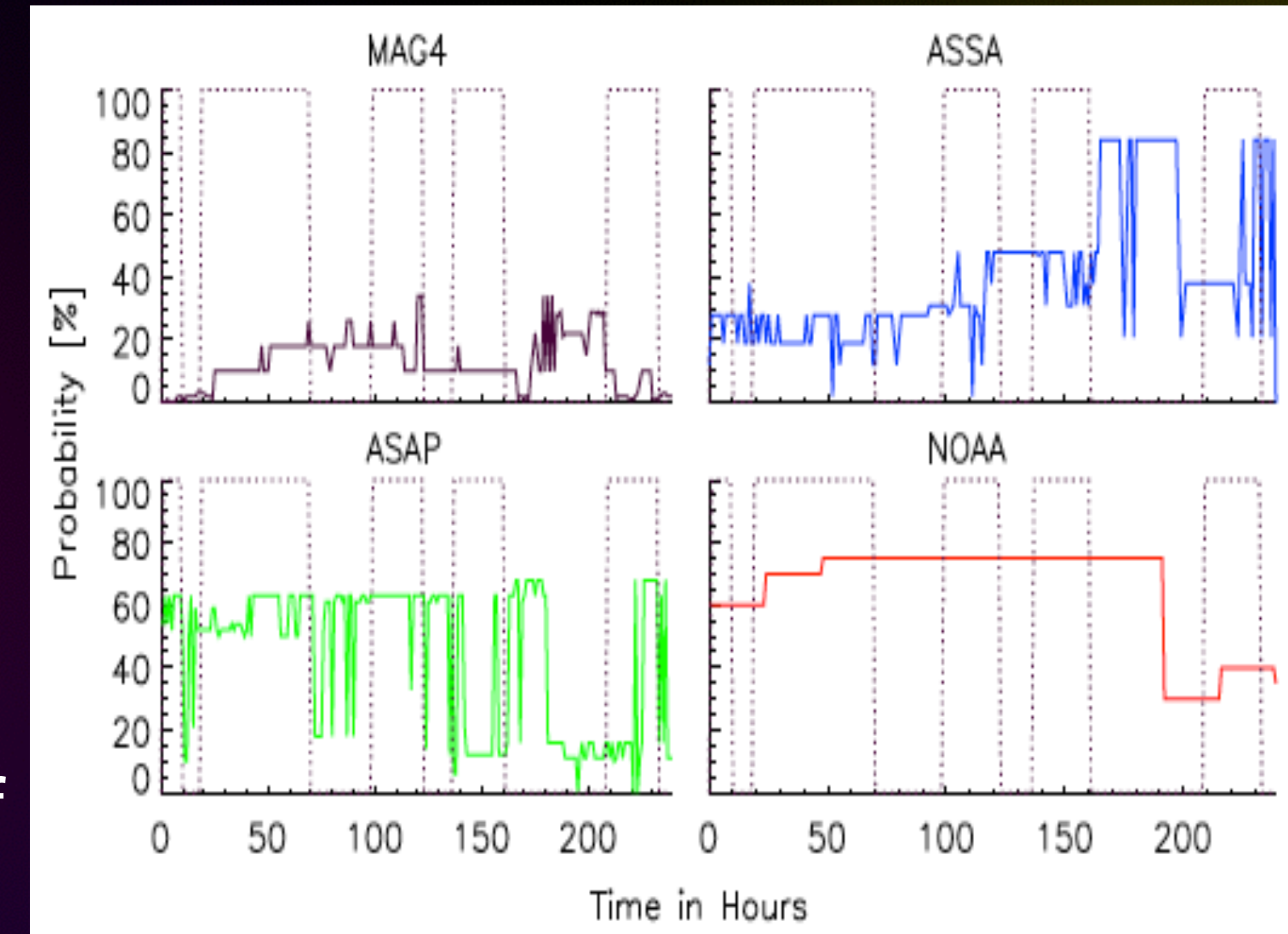
INDICATIVE RESULTS

- Multivariate forecasting



Bobra & Couvidat (2014)

- Ensemble forecasting

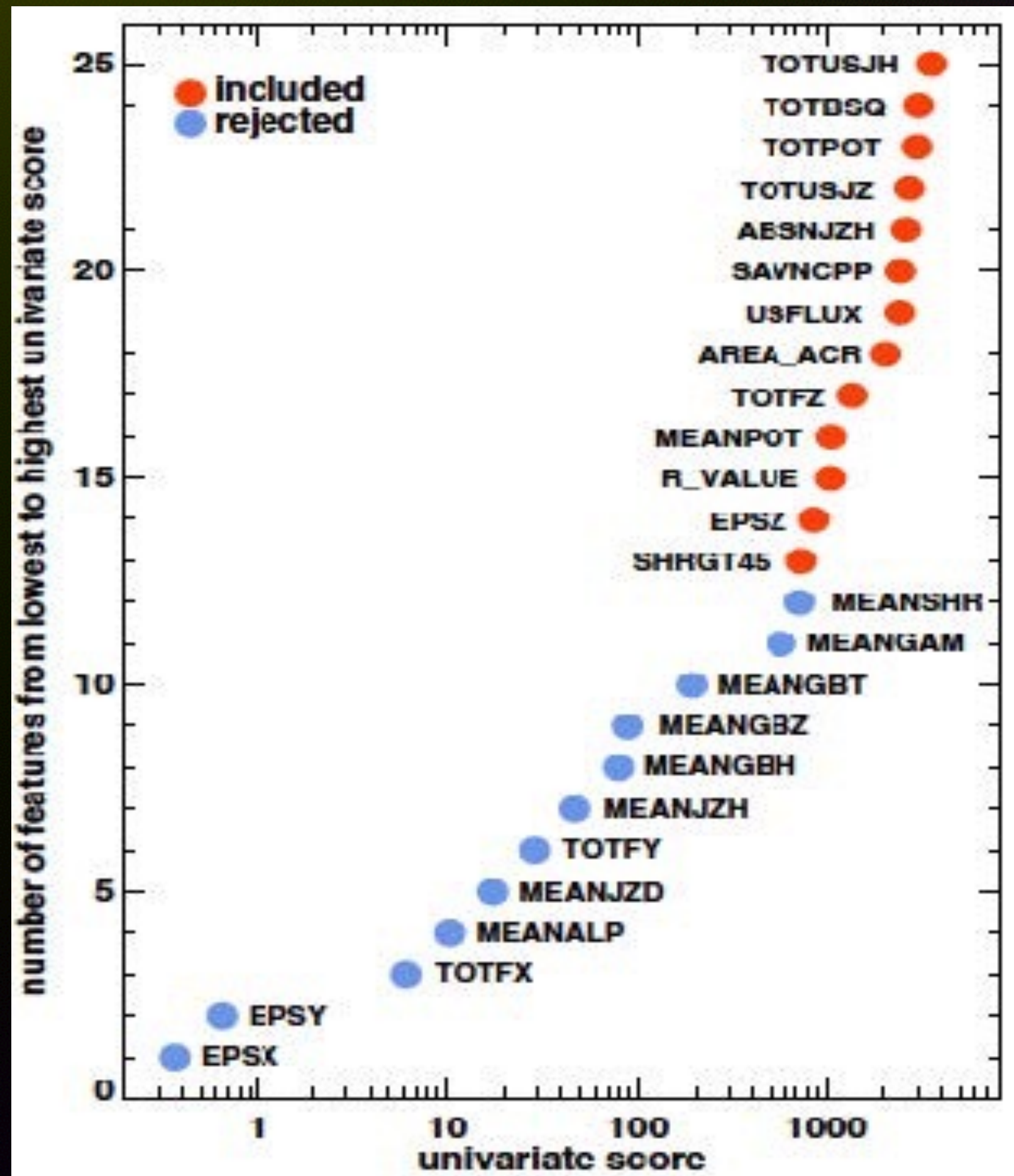


Guerra et al., (2015)

- Ordering of predictors by means of a univariate Fisher ranking score
- Machine-learning classifiers adopted
- Homogenizing the results of multiple flare prediction methods, using them with equal or non-equal weights for an ensemble forecasting

INDICATIVE RESULTS

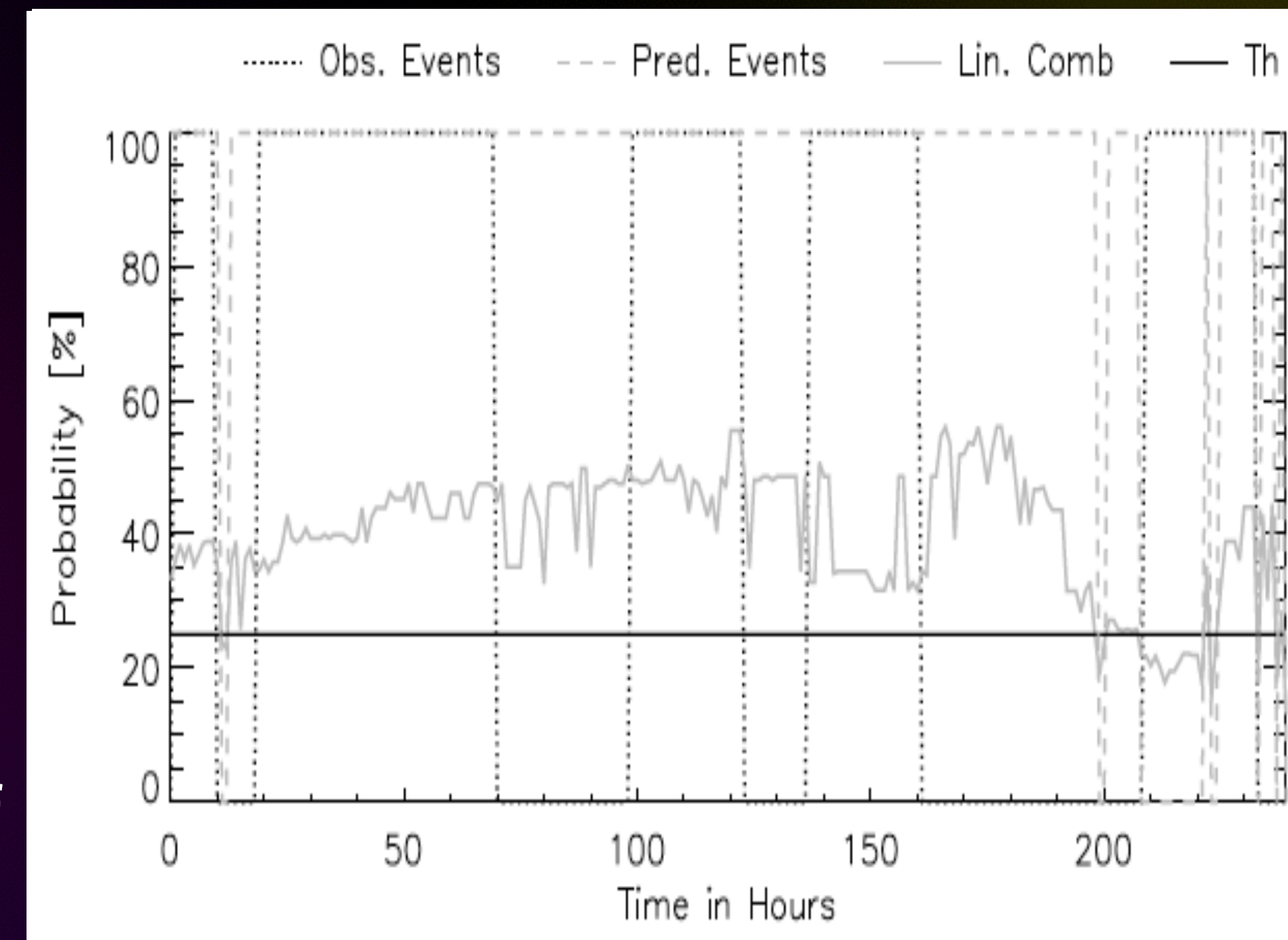
- Multivariate forecasting



Bobra & Couvidat (2014)

- Ordering of predictors by means of a univariate Fisher ranking score
- Machine-learning classifiers adopted
- Homogenizing the results of multiple flare prediction methods, using them with equal or non-equal weights for an ensemble forecasting

- Ensemble forecasting



Guerra et al., (2015)



JUDGING WHICH METHODS WORK: VALIDATION

- Existing methods are borrowed from terrestrial weather forecasting
- Two types of validation
 - On binary (YES / NO) prediction output
 - On probabilistic ($0 < p < 1$) prediction output
- **Both are used in flare prediction**



VALIDATION: BORROWED BY TERRESTRIAL WEATHER FORECASTING

Binary validation: Flare (YES) or No Flare (NO)

Tailoring according to different end user needs

	Forecast Flare	Forecast No-flare
Observed Flare	TP	FN
Observed No-flare	FP	TN

Table courtesy: Shaun Bloomfield

2 x 2 contingency table

- TP : true positives
- FN : false negatives
- FP : false positives
- TN : true negatives

- Generalized skill score:

$$SS = \frac{score - score_{reference}}{score_{perfect} - score_{reference}}$$



VALIDATION: BORROWED BY TERRESTRIAL WEATHER FORECASTING

Binary validation: Flare (YES) or No Flare (NO)

	Forecast Flare	Forecast No-flare
Observed Flare	TP	FN
Observed No-flare	FP	TN

2 x 2 contingency table

- TP : true positives
- FN : false negatives
- FP : false positives
- TN : true negatives

Table courtesy: Shaun Bloomfield

- Generalized skill score:

$$SS = \frac{score - score_{reference}}{score_{perfect} - score_{reference}}$$

Tailoring according to different end user needs

- Heidke skill score (ref: random prediction):

$$HSS = \frac{2(TP + TN) - N}{N}$$

- Appleman skill score (ref: climatology [\bar{v}]):

$$ApSS = \frac{TP - FP}{N}$$

- True skill statistic (ref: weighting POD w. POFD):

$$TSS = POD - POFD$$

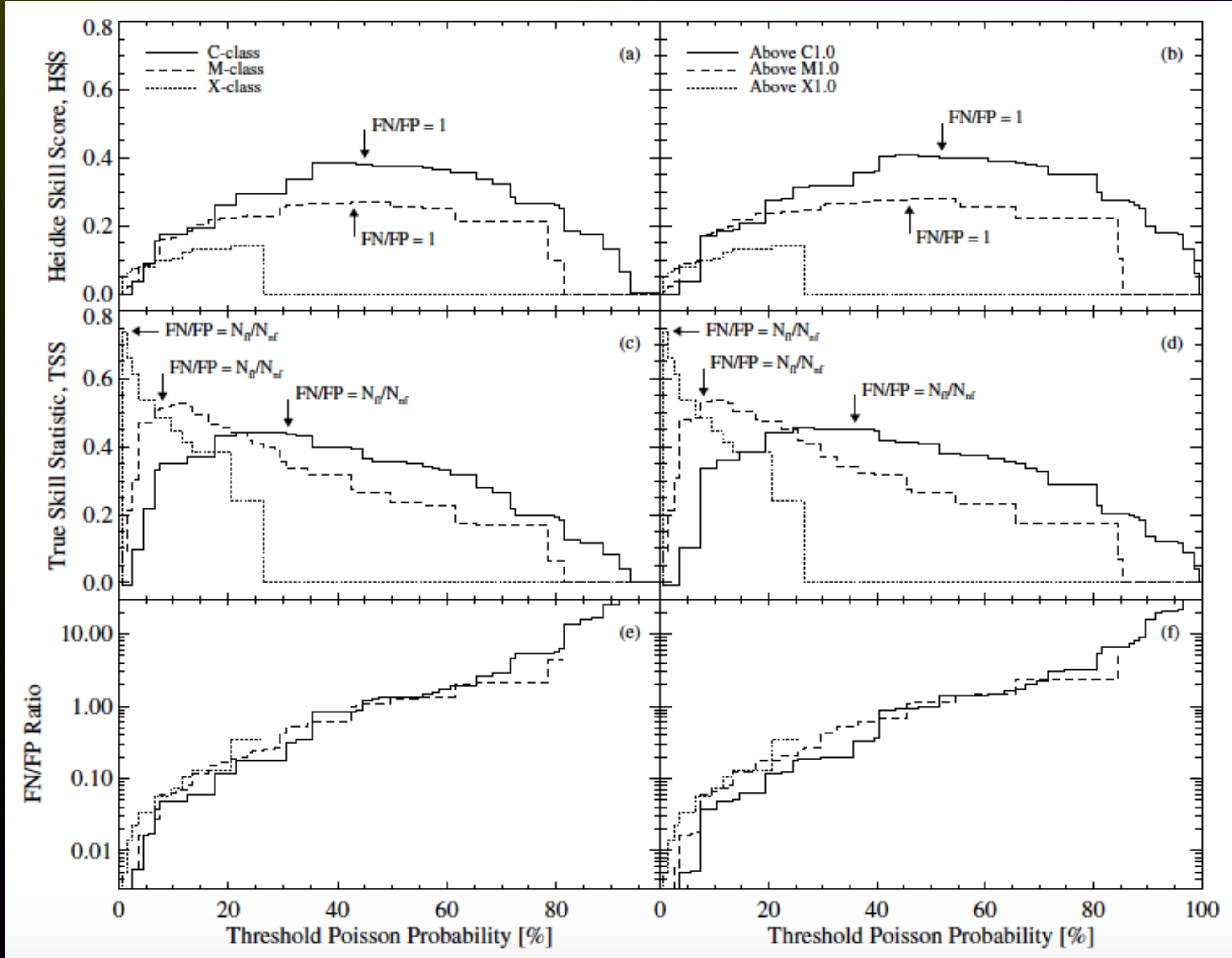


(SOME) BINARY FORECAST VERIFICATION METRICS

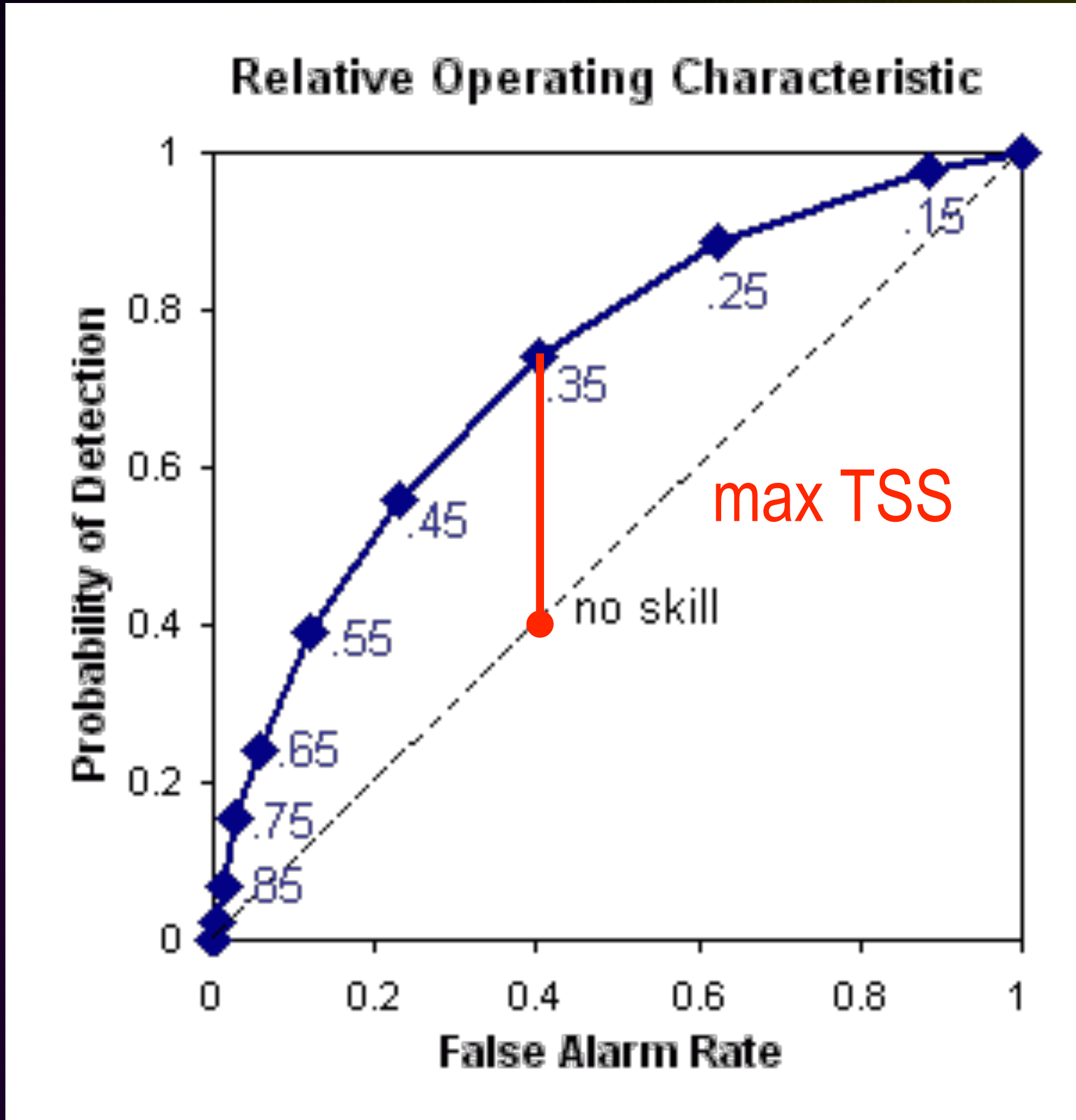
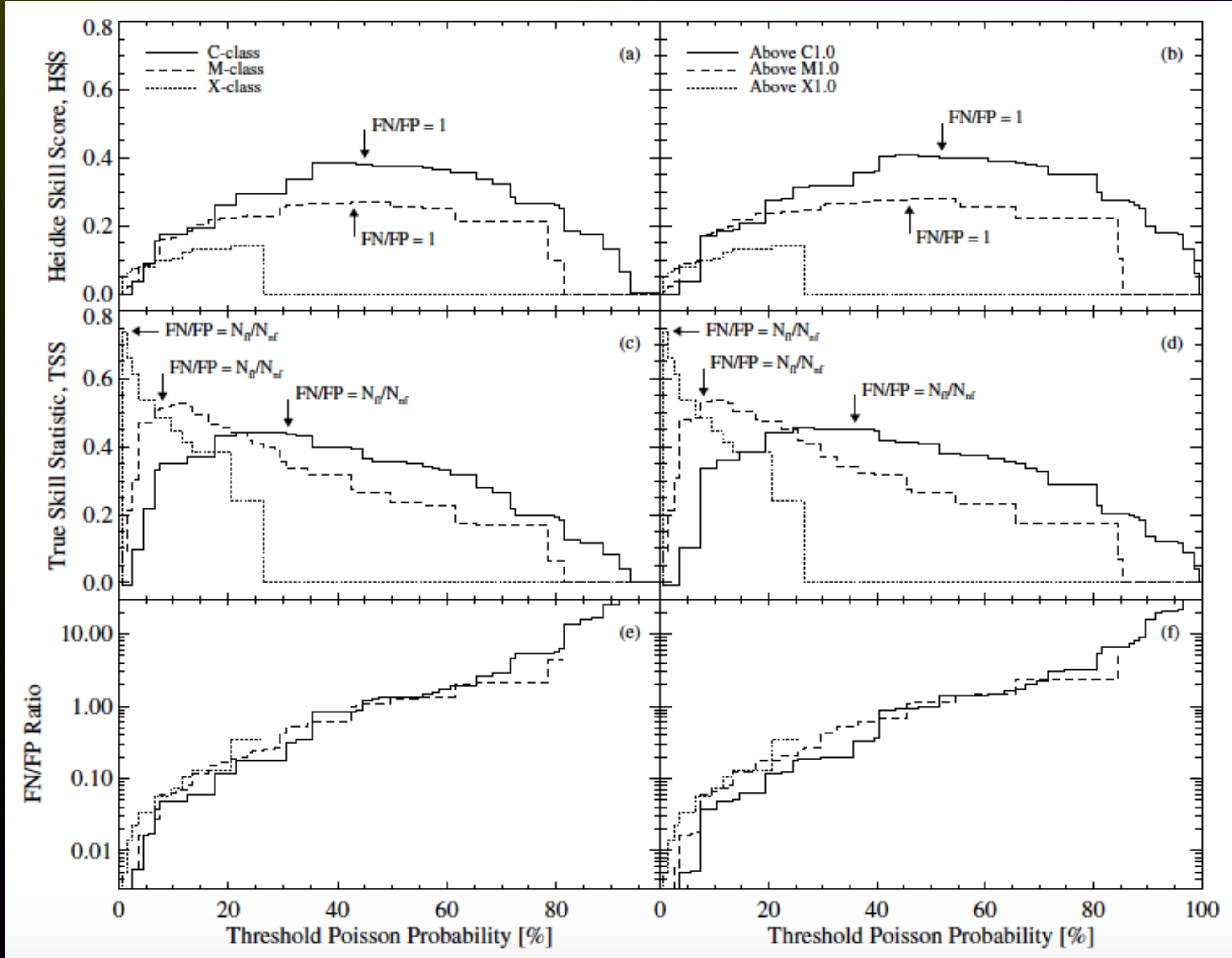
Metric Name	Short Name	Format	Worst Score	"No skill" Score	Perfect Score
Accuracy	ACC	$(TP + TN) / N$	0	...	1
Probability of detection	POD	$TP / (TP + FN)$	0	...	1
Probability of false detection (false alarm rate)	POFD	$FP / (FP + TN)$	1	...	0
False alarm ratio	FAR	$FP / (TP + FP)$	1	...	0
True skill statistic	TSS	$POD - POFD$	-1	0	1
Heidke skill score	HSS	$(TP + TN - E_{\text{random}}) / (N - E_{\text{random}})$	-1	0	1

Slide courtesy: Shaun Bloomfield

SOME INDICATIVE RESULTS



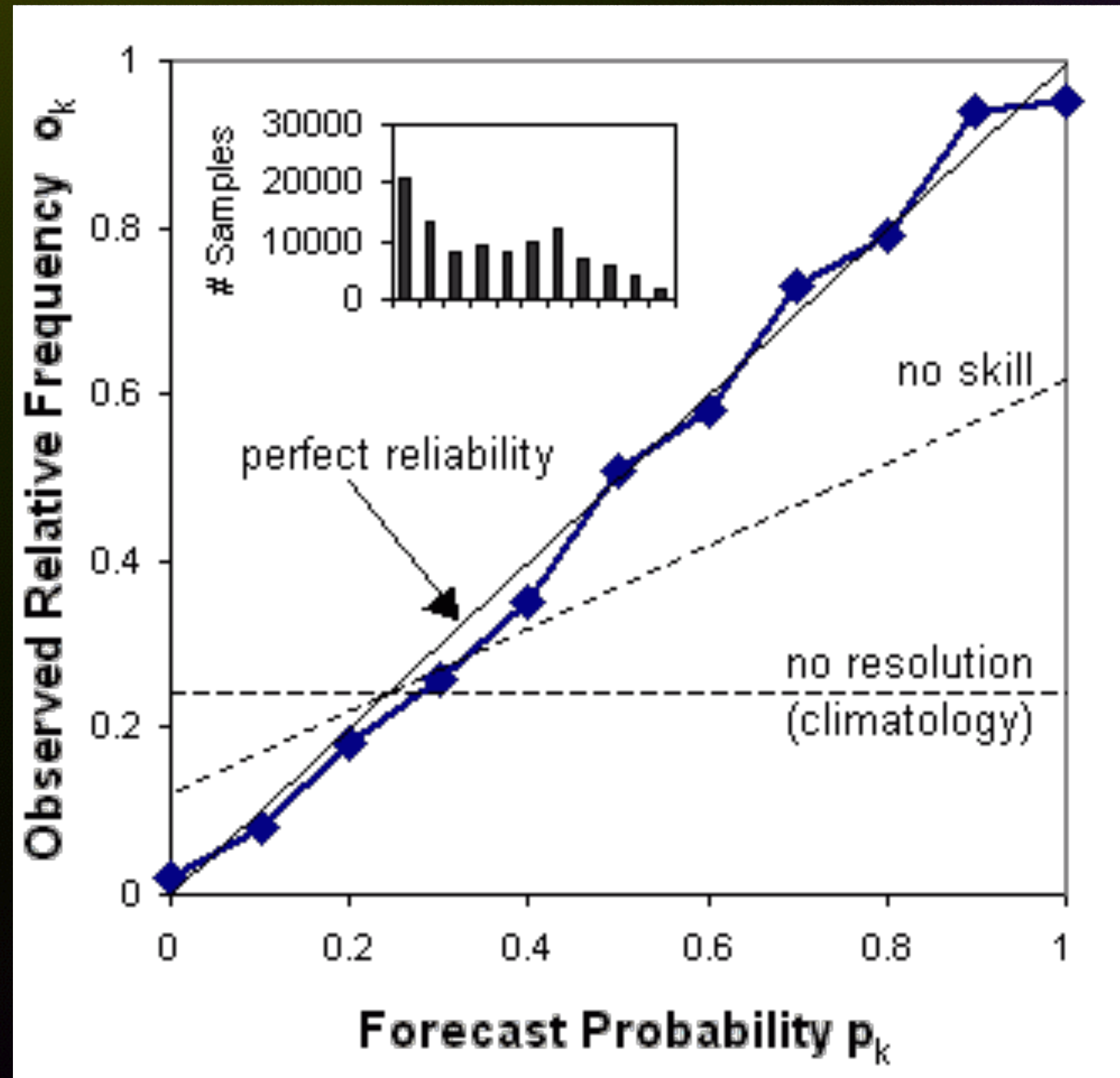
SOME INDICATIVE RESULTS



Example ROC curve (TSS vs. p_{thres})

PROBABILISTIC VALIDATION

Accept that a probability $0 < p < 1$ is assigned to each prediction

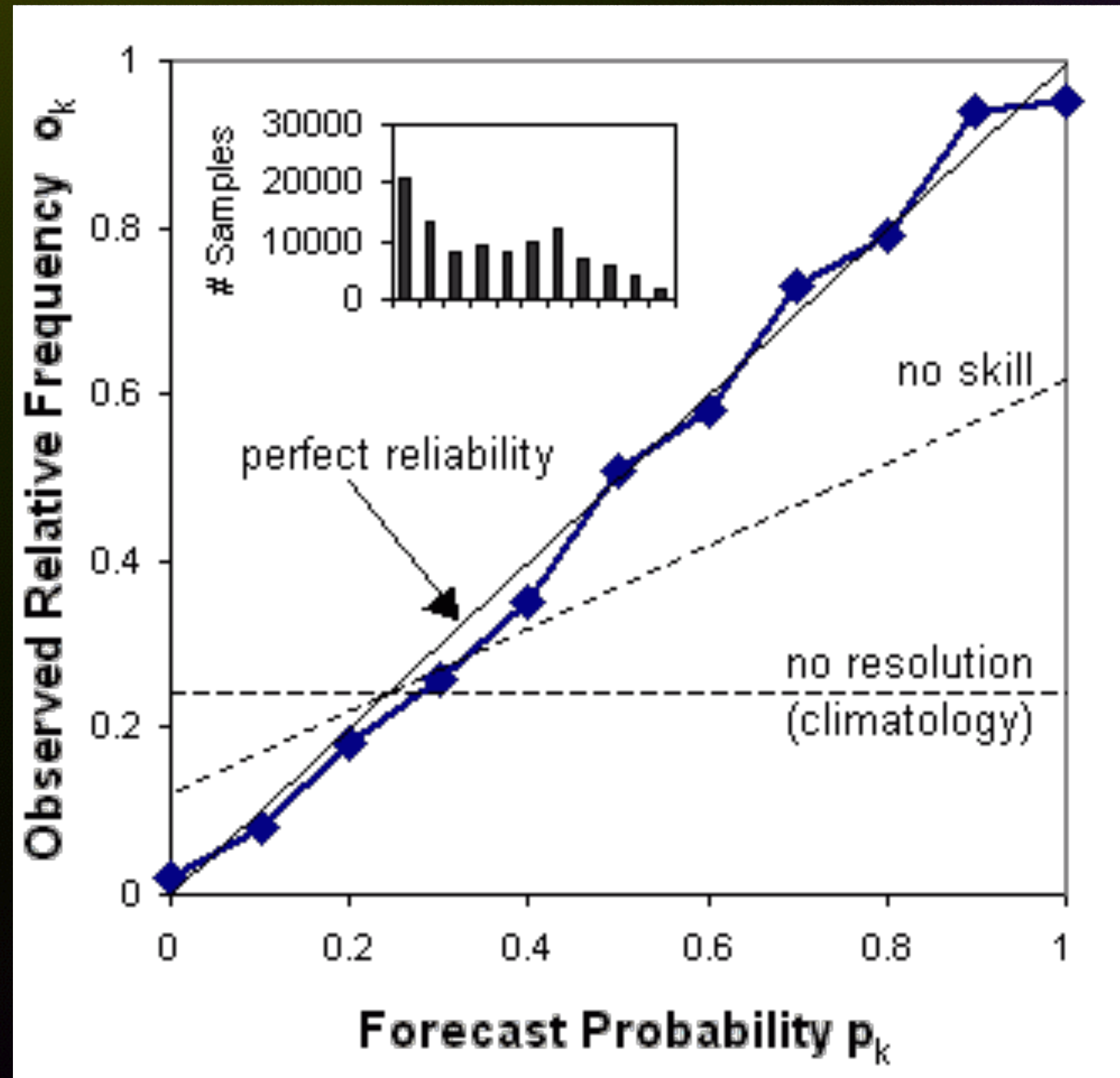


Reliability diagram

$$SS = 1 - \frac{MSE_{forecast}}{MSE_{reference}}$$

PROBABILISTIC VALIDATION

Accept that a probability $0 < p < 1$ is assigned to each prediction



Reliability diagram

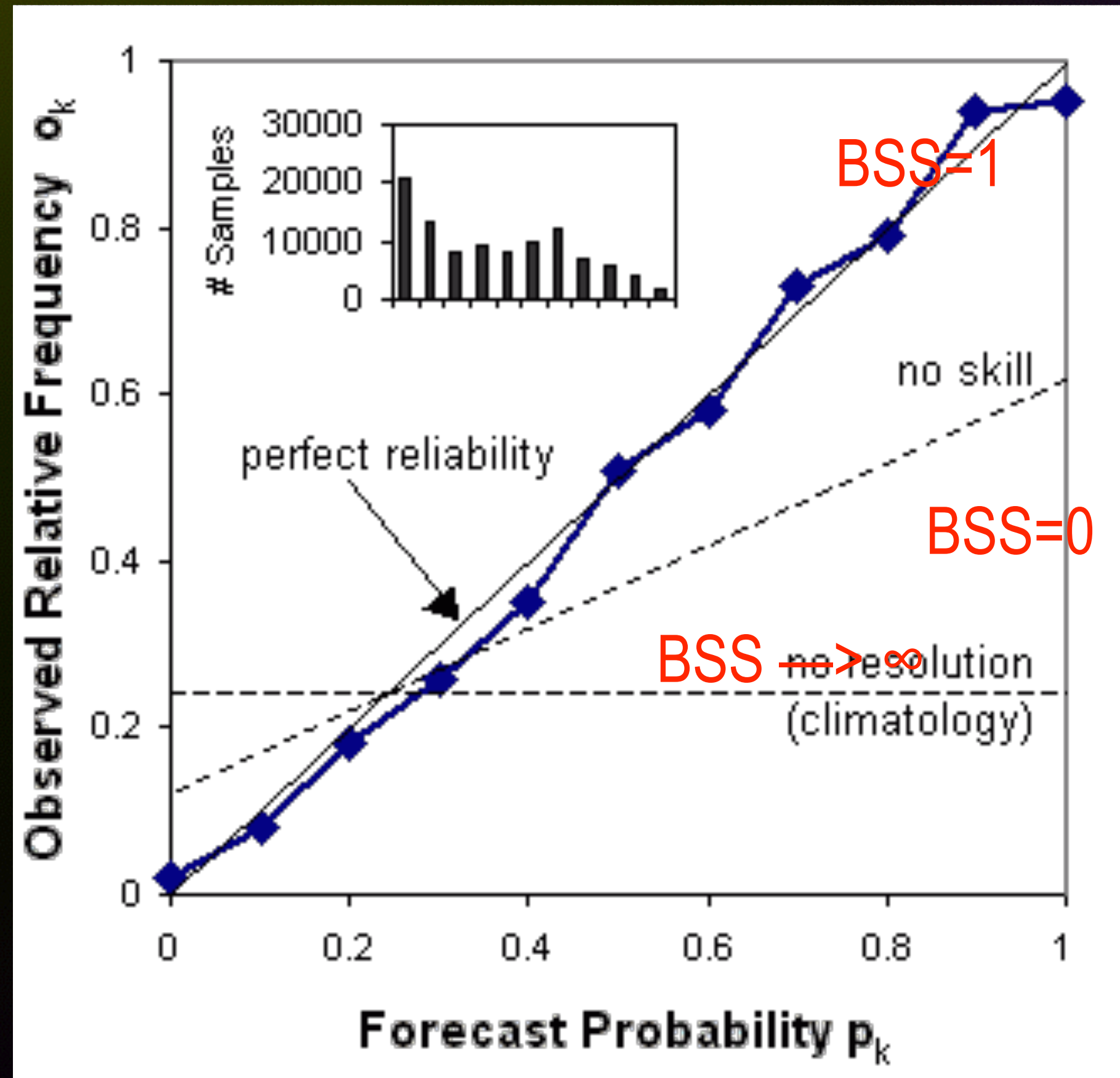
- Correlate forecast probability with observed frequency
- Compare your skill against climatology (mean flaring rate within forecast window)
- Generalized skill score:

$$SS = 1 - \frac{MSE_{forecast}}{MSE_{reference}}$$

$$MSE = \langle (o - p)^2 \rangle$$

PROBABILISTIC VALIDATION

Accept that a probability $0 < p < 1$ is assigned to each prediction



Reliability diagram

- Correlate forecast probability with observed frequency
- Compare your skill against climatology (mean flaring rate within forecast window)
- Generalized skill score:

$$SS = 1 - \frac{MSE_{forecast}}{MSE_{reference}}$$

$$MSE = \langle (o - p)^2 \rangle$$

- Brier skill score (reference: climatology):

$$BSS = 1 - \frac{\langle (o - p)^2 \rangle}{\langle (o - \bar{o})^2 \rangle}$$

$$BSS \in (-\infty, 1)$$

FIRST EFFORT TO COMPARE METHOD PERFORMANCES ON COMMON DATA SETS

Recently published (Barnes et al., 2016)

Parameter/ Method	Statistical Method	C1.0+, 24 hr		M1.0+, 12 hr		M5.0+, 12 hr	
		ApSS	BSS	ApSS	BSS	ApSS	BSS
B_{eff}	Bayesian	0.12	0.06	0.00	0.03	0.00	0.02
ASAP	Machine	0.25	0.30	0.01	-0.01	0.00	-0.84
BBSO	Machine	0.08	0.10	0.03	0.06	0.00	-0.01
WL_{SG2}	Curve fitting	N/A	N/A	0.04	0.06	0.00	0.02
NWRA MAG 2-VAR	NPDA	0.24	0.32	0.04	0.13	0.00	0.06
$\log(\mathcal{R})$	NPDA	0.17	0.22	0.01	0.10	0.02	0.04
GCD	NPDA	0.02	0.07	0.00	0.03	0.00	0.02
NWRA MCT 2-VAR	NPDA	0.23	0.28	0.05	0.14	0.00	0.06
SMART2	CCNN	0.24	-0.12	0.01	-4.31	0.00	-11.2
Event Statistics, 10 prior	Bayesian	0.13	0.04	0.01	0.10	0.01	0.00
McIntosh	Poisson	0.15	0.07	0.00	-0.06	N/A	N/A

Event List	Event No	Event Rate	Event No	Event Rate	Event No	Event Rate	Event No	Event Rate	
	AD		MCD#1		MCD#2				
C1.0+, 24 hr	2609	10356	0.201	789	3751	0.174	249	128	0.660
M1.0+, 12 hr	400	12565	0.031	102	3162	0.031	70	220	0.241
M5.0+, 12 hr	93	12872	0.007	26	3633	0.007	21	270	0.072



FIRST EFFORT TO COMPARE METHOD PERFORMANCES ON COMMON DATA SETS

Recently published (Barnes et al., 2016)

Parameter/ Method	Statistical Method	C1.0+, 24 hr		M1.0+, 12 hr		M5.0+, 12 hr	
		ApSS	BSS	ApSS	BSS	ApSS	BSS
B_{eff}	Bayesian	0.12	0.06	0.00	0.03	0.00	0.02
ASAP	Machine	0.25	0.30	0.01	-0.01	0.00	-0.84
BBSO	Machine	0.08	0.10	0.03	0.06	0.00	-0.01
WL_{SG2}	Curve fitting	N/A	N/A	0.04	0.06	0.00	0.02
NWRA MAG 2-VAR	NPDA	0.24	0.32	0.04	0.13	0.00	0.06
$\log(\mathcal{R})$	NPDA	0.17	0.22	0.01	0.10	0.02	0.04
GCD	NPDA	0.02	0.07	0.00	0.03	0.00	0.02
NWRA MCT 2-VAR	NPDA	0.23	0.28	0.05	0.14	0.00	0.06
SMART2	CCNN	0.24	-0.12	0.01	-4.31	0.00	-11.2
Event Statistics, 10 prior	Bayesian	0.13	0.04	0.01	0.10	0.01	0.00
McIntosh	Poisson	0.15	0.07	0.00	-0.06	N/A	N/A

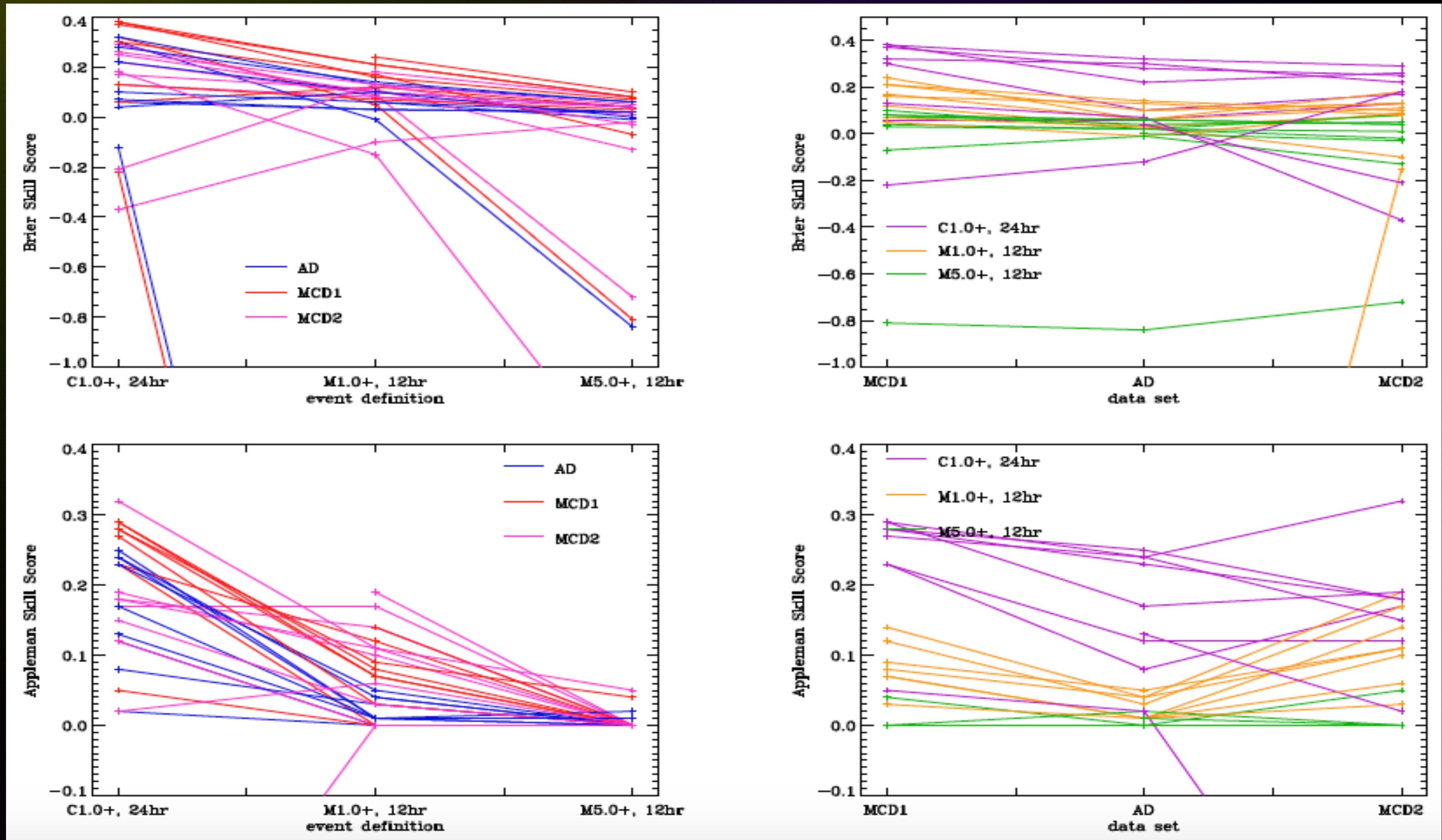
Event List	Event Event	No Event	Event Rate	Event Event	No Event	Event Rate	Event Event	No Event	Event Rate
	AD			MCD#1			MCD#2		
C1.0+, 24 hr	2609	10356	0.201	789	3751	0.174	249	128	0.660
M1.0+, 12 hr	400	12565	0.031	102	3162	0.031	70	220	0.241
M5.0+, 12 hr	93	12872	0.007	26	3633	0.007	21	270	0.072

Apparently worse BSS for scarcer (i.e., increasing flare class) events

Typically a bit - but not much - better than climatology (> 0) / quite often worse than climatology (< 0)



FIRST EFFORT TO COMPARE METHOD PERFORMANCES ON COMMON DATA SETS



Generally, there is no method clearly outperforming the others

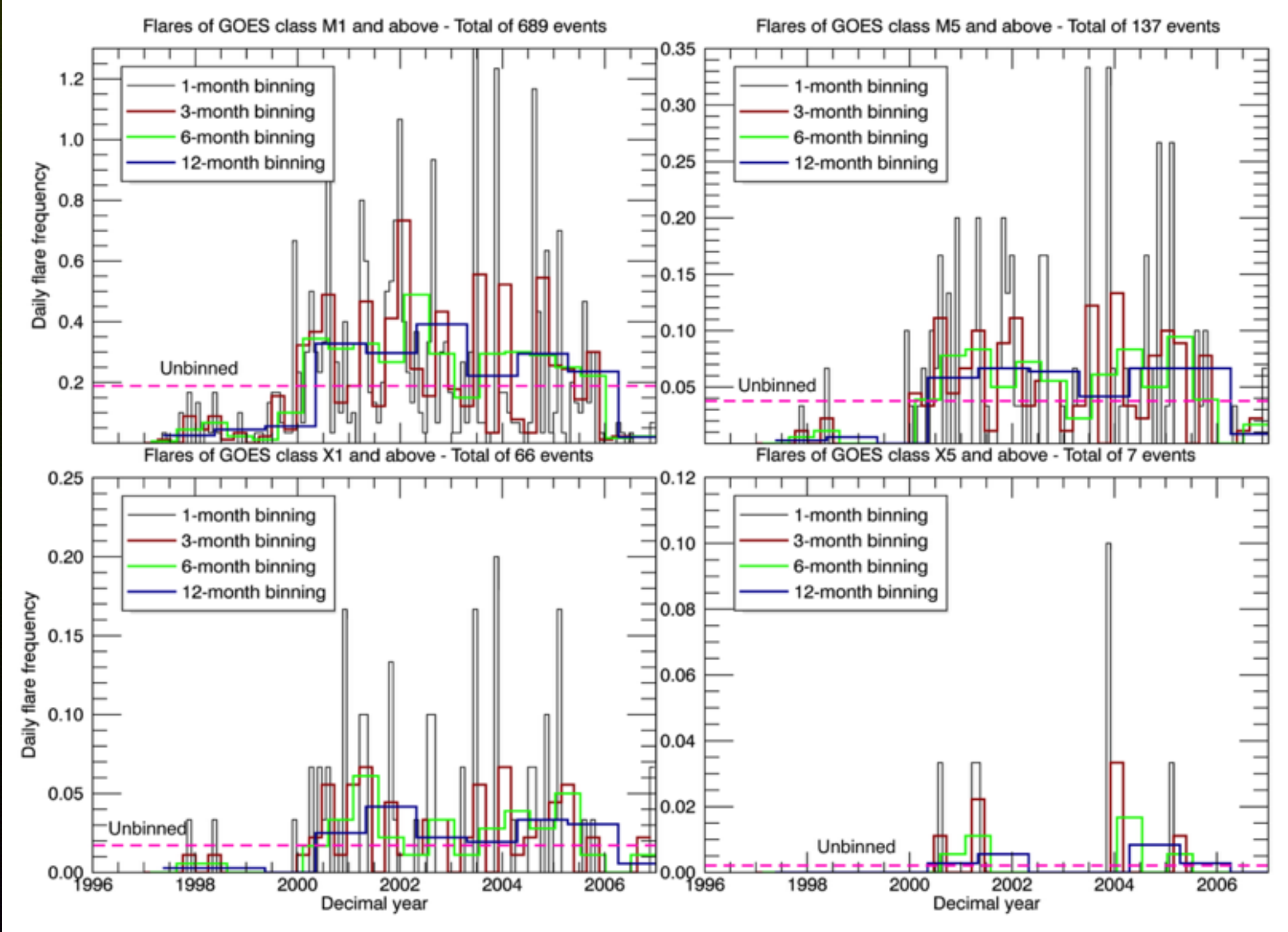


VALIDATION REQUIREMENTS

- Balanced dataset of flaring and non-flaring populations (correct flaring rates)

VALIDATION REQUIREMENTS

- Balanced dataset of flaring and non-flaring populations (correct flaring rates)

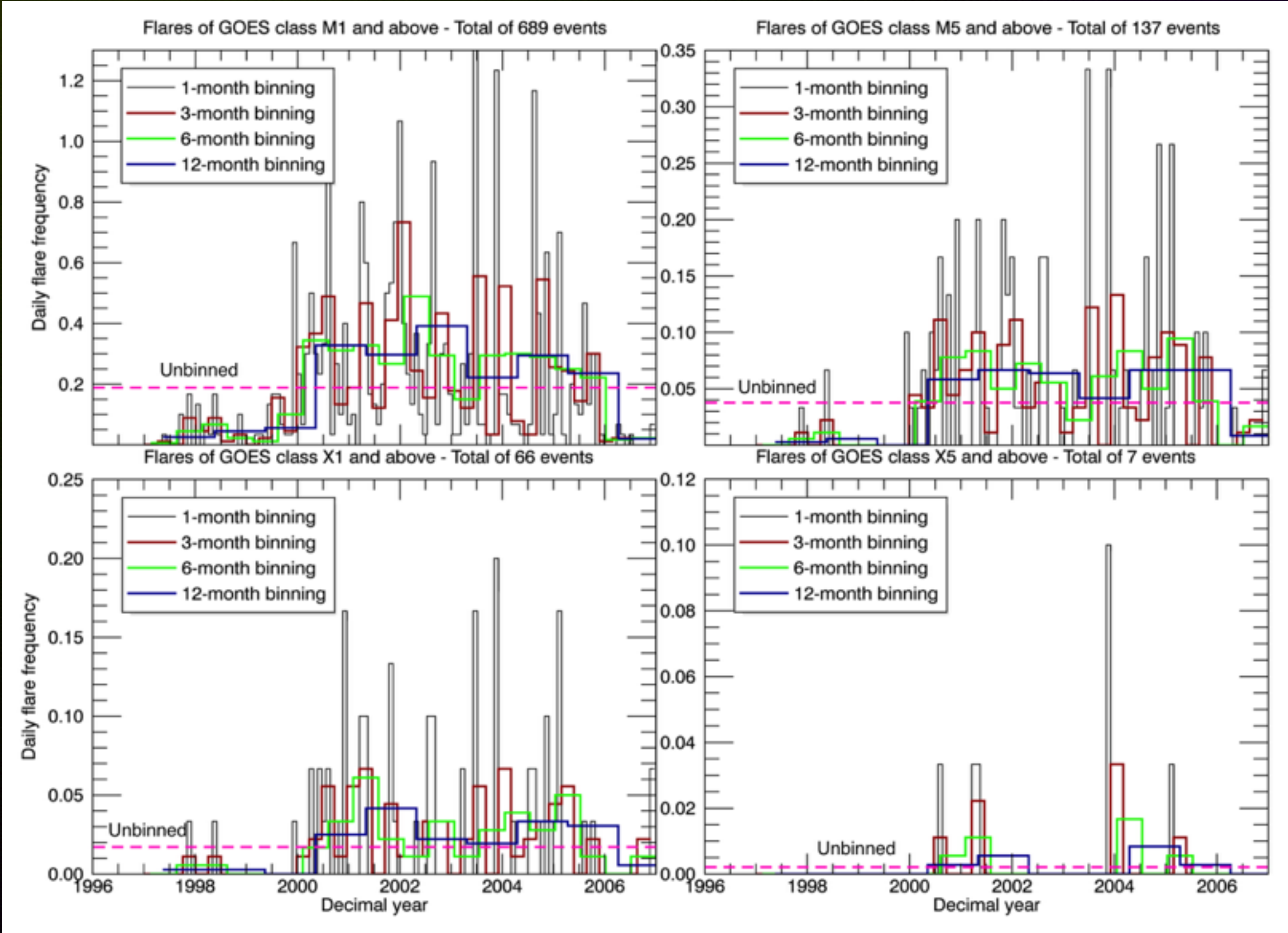


Flaring rates over solar cycle 23 (M1+, M5+, X1+, X5+)



VALIDATION REQUIREMENTS

- Balanced dataset of flaring and non-flaring populations (correct flaring rates)
- Large number of validation tests, using randomly chosen training and test sets



Flaring rates over solar cycle 23 (M1+, M5+, X1+, X5+)

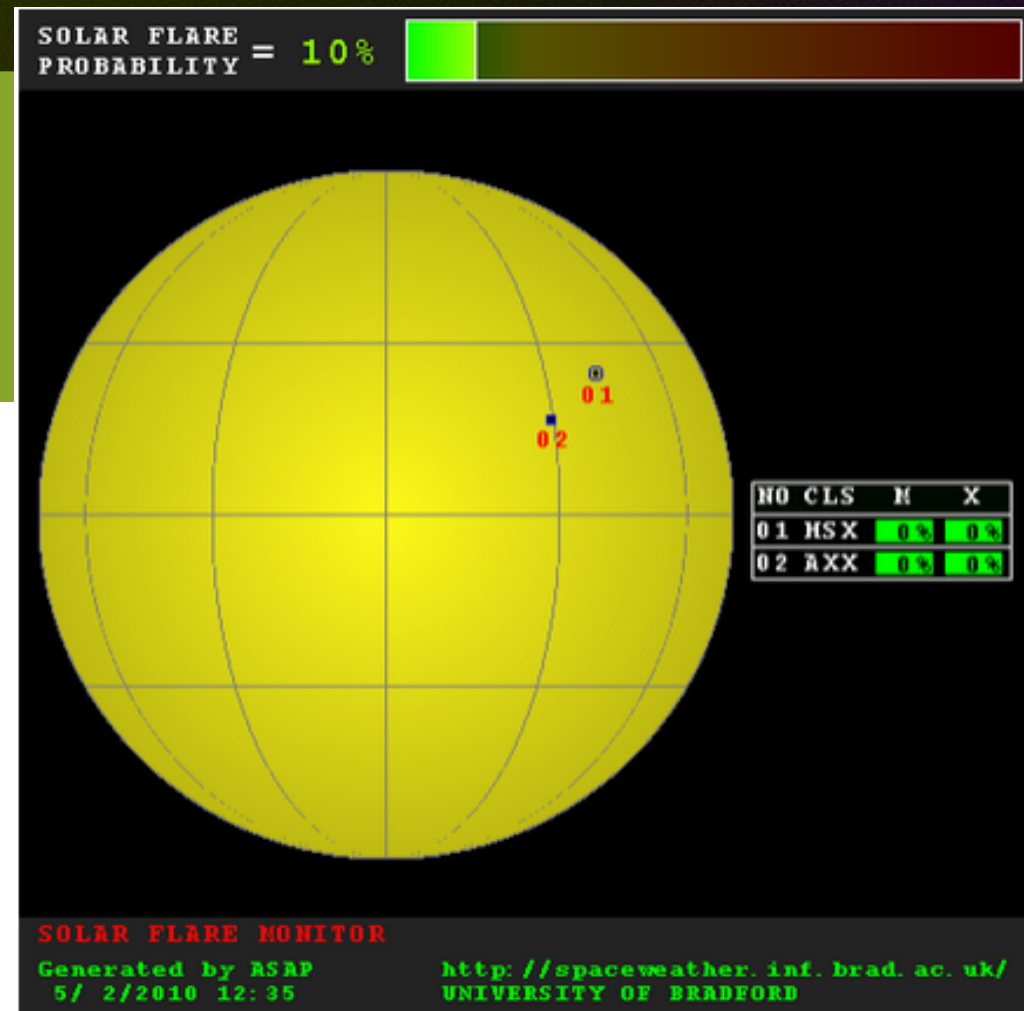


Random selection of training (white) and testing (red dots) subsets



FROM PREDICTION METHODS TO OPERATIONAL FLARE FORECASTING SERVICES

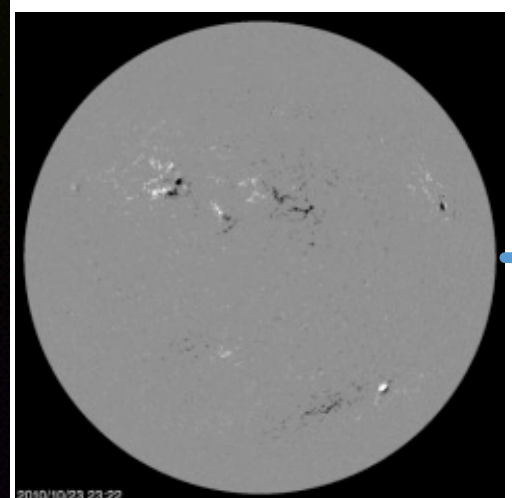
ASAP



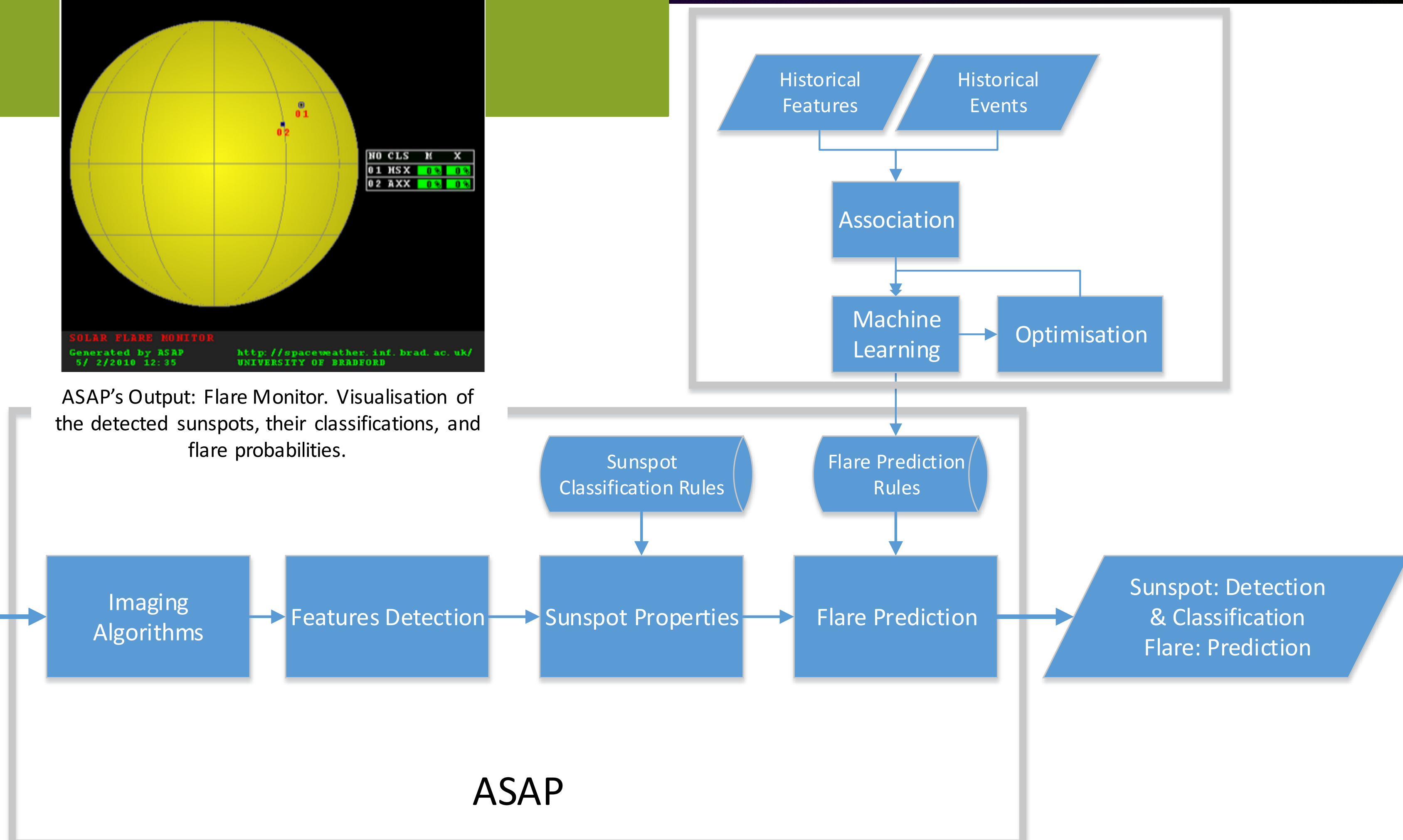
ASAP's Output: Flare Monitor. Visualisation of the detected sunspots, their classifications, and flare probabilities.



MDI Continuum



MDI Magnetogram



ASAP: The first flare prediction service utilizing machine learning methods

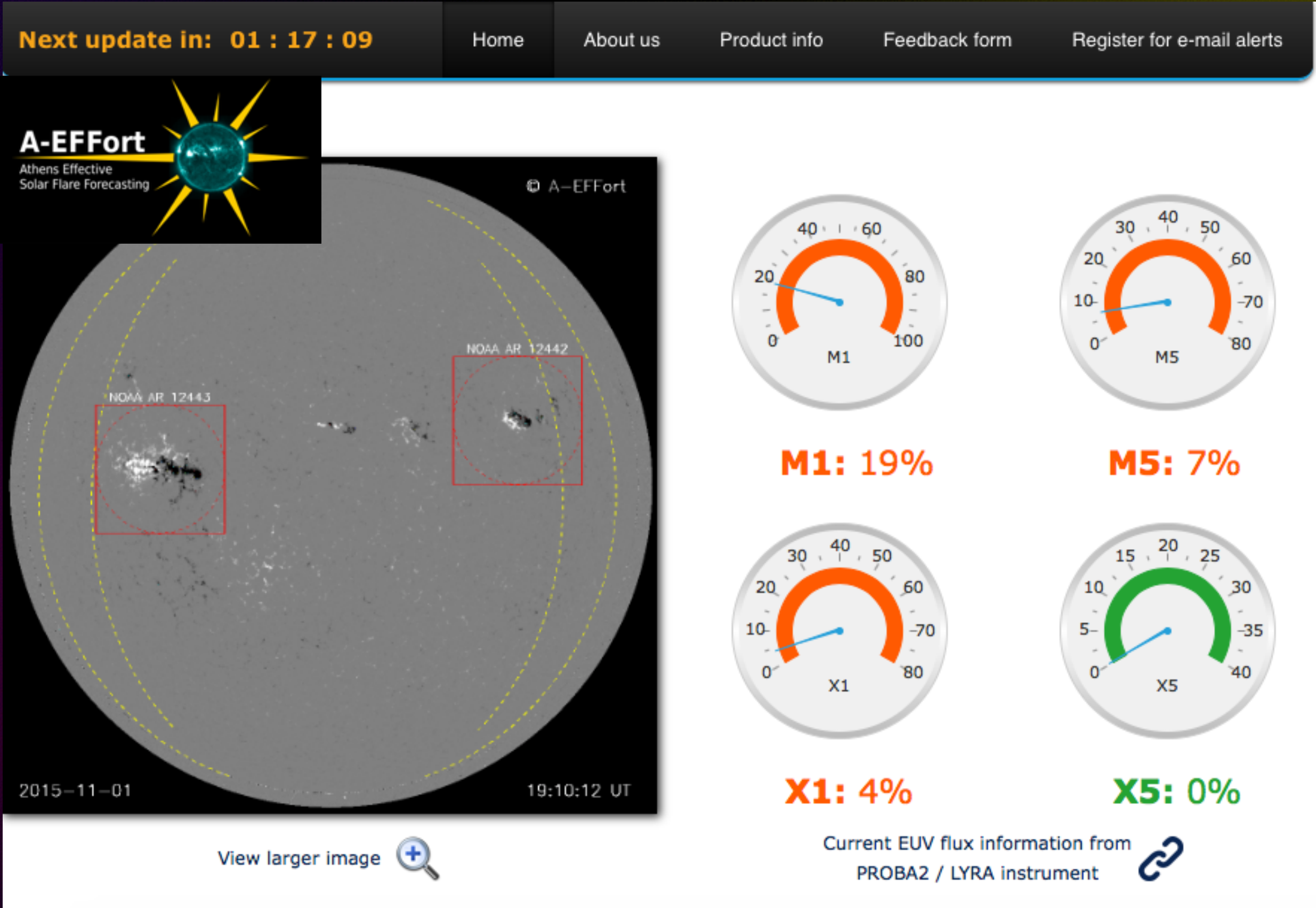
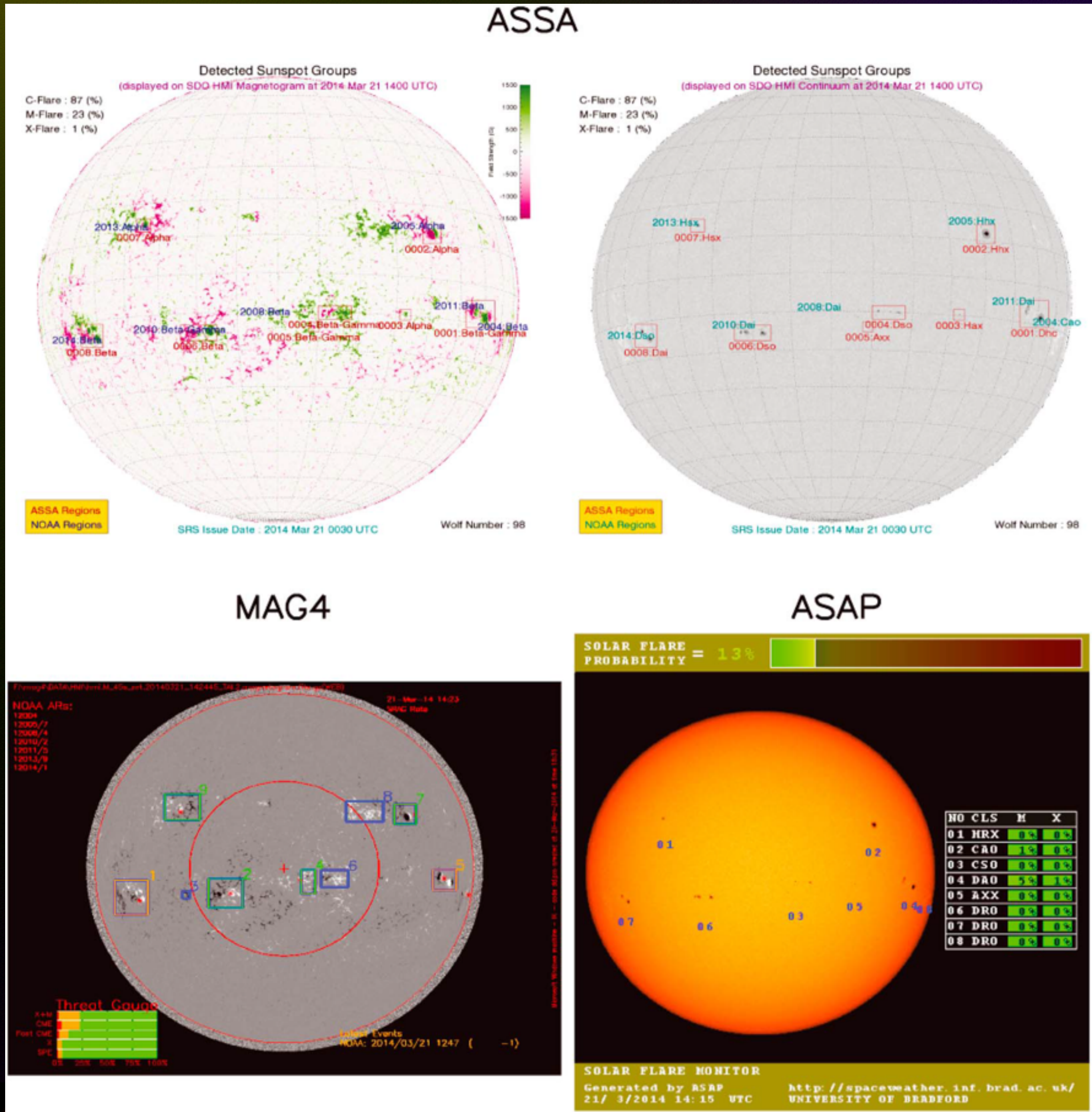
Besides the idea (prediction method), an infrastructure is also needed

Complete automation means:

- Ease of calculations
- Ease of maintenance
- Resilience
- Modularity, for improvement



EXISTING FLARE PREDICTION SERVICES AROUND THE WORLD



www.SolarMonitor.org



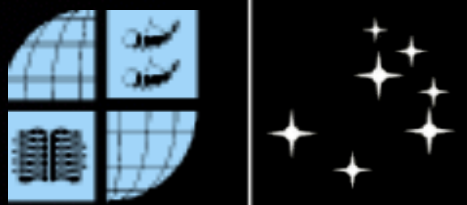
Guerra et al., (2015)

M. K. Georgoulis & R. Qahwaji

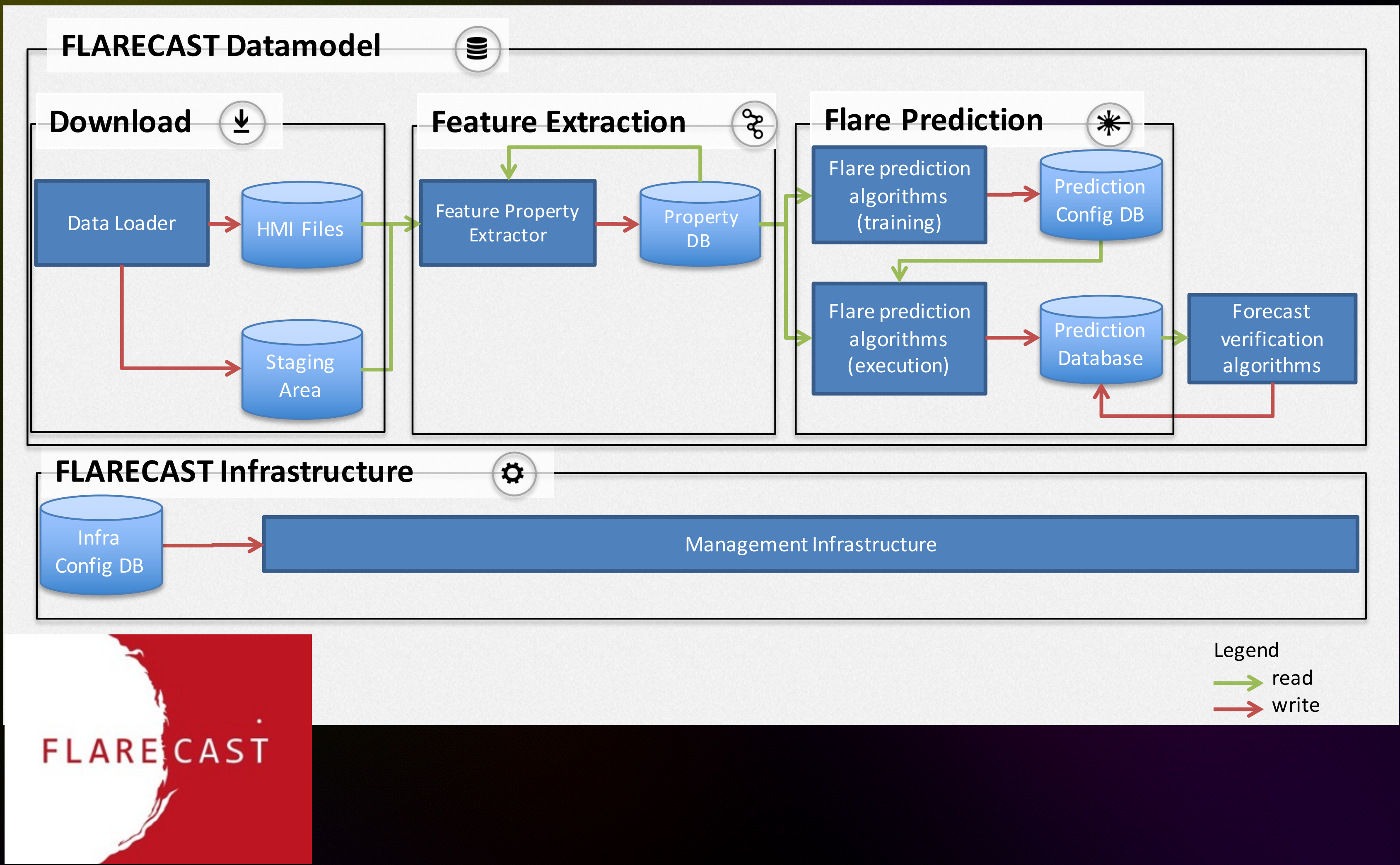
Oostende, November 18, 2016



ESWW13



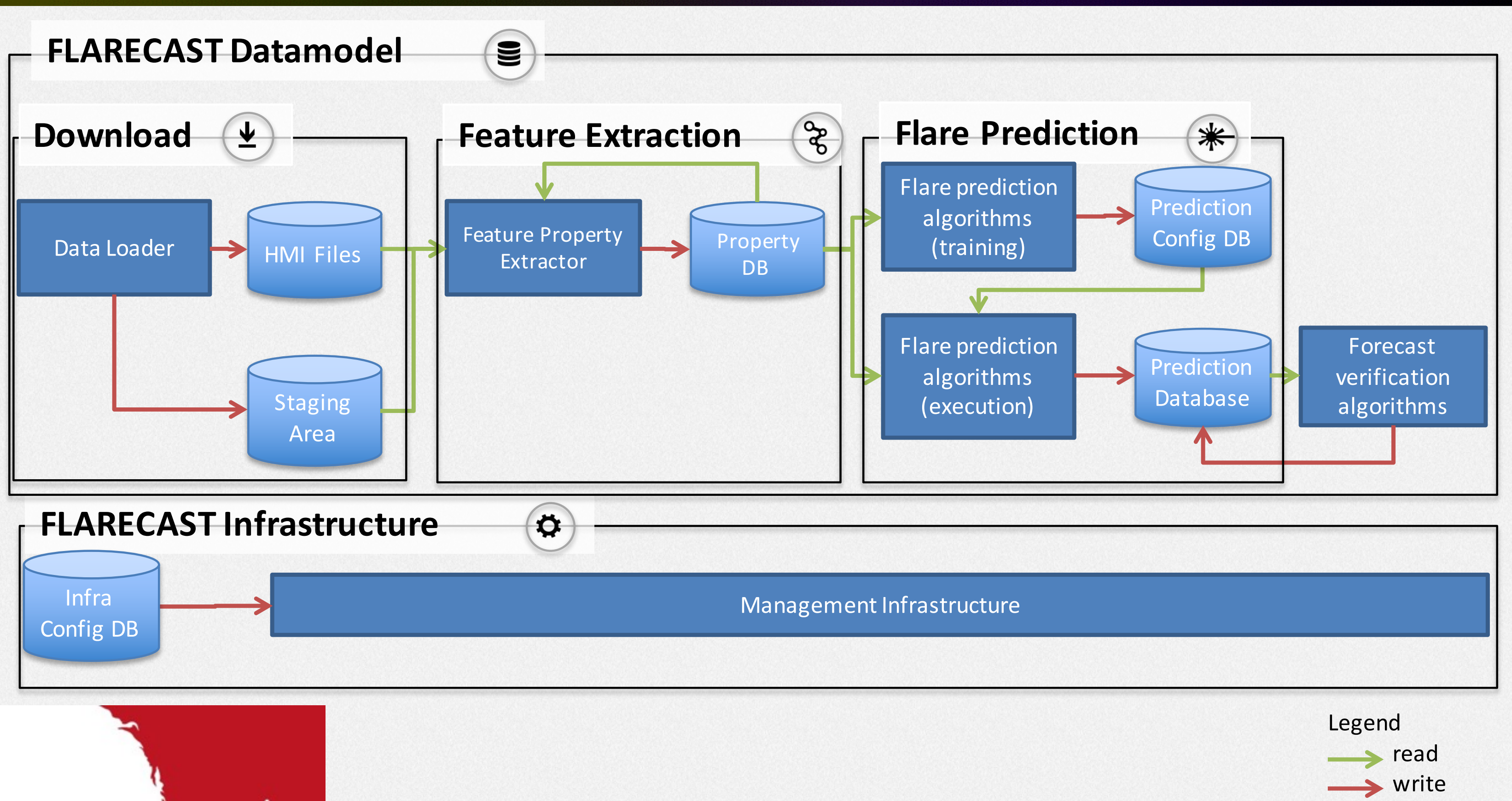
A NUMBER OF FORTHCOMING SERVICES



Europe, USA, Japan



A NUMBER OF FORTHCOMING SERVICES



DAFFS



Europe, USA, Japan

- **Fact:** Virtually all planned services rely essentially on multivariate predictors
- **Aphorism:** validation, validation, validation ...



CONCLUSIONS

- ★ Consensus that reliable, automated solar flare prediction should be an asset of our SWE forecasting efforts
- ★ Can flares be predicted, however?
 - Quite likely, major flare prediction will remain probabilistic in the future
 - But is this due to the nature of the problem, or due to lack of crucial information or a flawed approach?
 - How far along we can go remains TBS — the goal of various flare forecasting efforts is to bring probabilistic flare prediction as close as possible to a binary (YES / NO one)
- ★ Customized, but always unbiased, validation : its importance cannot be stressed enough
- ★ Multivariate forecasting, enabled by machine-learning and other methods (i.e., PCA, DA) seems to be the norm for future services — we can do it nowadays, can't we?
- ★ However, we need to raise Occam's razor : how many / which parameters do we need for a sufficient forecasting? The answer will drive developments in our physical understanding of flare triggering



CONCLUSIONS

- ★ Consensus that reliable, automated solar flare prediction should be an asset of our SWE forecasting efforts
- ★ Can flares be predicted, however?
 - Quite likely, major flare prediction will remain probabilistic in the future
 - But is this due to the nature of the problem, or due to lack of crucial information or a flawed approach?
 - How far along we can go remains TBS — the goal of various flare forecasting efforts is to bring probabilistic flare prediction as close as possible to a binary (YES / NO one)
- ★ Customized, but always unbiased, validation : its importance cannot be stressed enough
- ★ Multivariate forecasting, enabled by machine-learning and other methods (i.e., PCA, DA) seems to be the norm for future services — we can do it nowadays, can't we?
- ★ However, we need to raise Occam's razor : how many / which parameters do we need for a sufficient forecasting? The answer will drive developments in our physical understanding of flare triggering

Diverse expertise and ways of thinking are generally needed





All these issues and challenges referring to flare prediction ...



All these issues and challenges referring to flare prediction ...



... we haven't even touched CME and SEP prediction yet!

BACKUP SLIDES